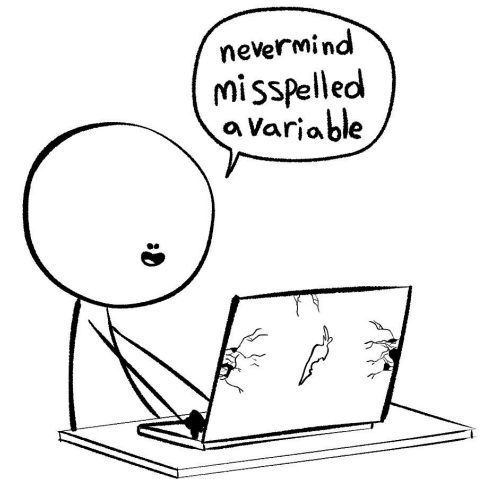
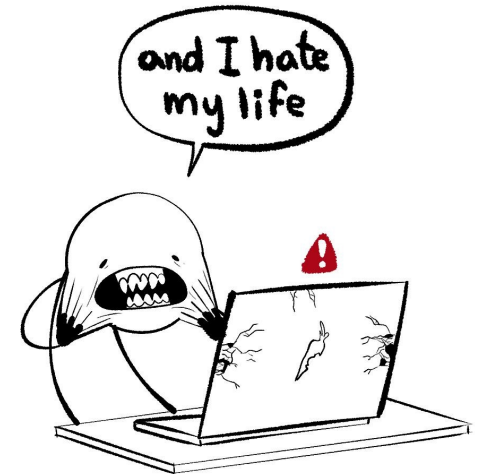


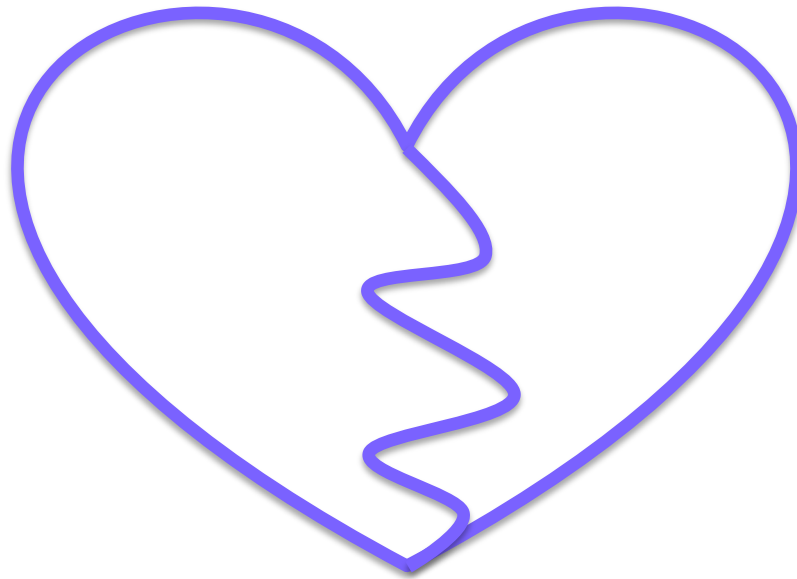
*me who just removed an error from my code

*my code:-



Reminders

It's my last lecture!



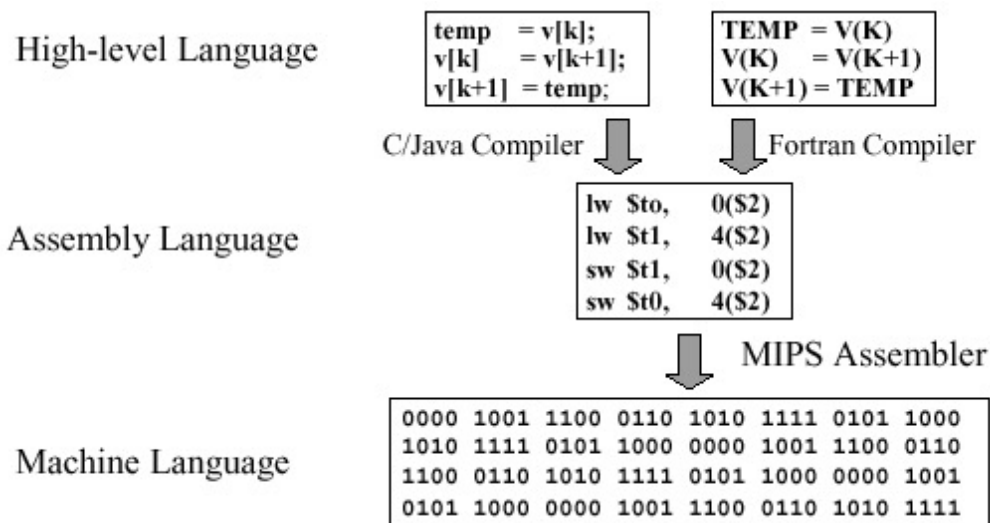
Reminders

Next week: Prof. Dodds comes to CS5 Green!

Python

```
>>> print("Hello World!")  
Hello World!
```

Assembly



Shan 2460

Reminders

Next week: Prof. Dodds comes to CS5 Green!



Shan 2460

Reminders

It's my last lecture!

6	10/12/21 - Lec 12: Hmmm 1 (Z)	10/14/21 - Lec 13: Hmmm 2 (Z)	No HW over fall break	12
7	10/19/21 - Happy fall break!	10/21/21 - Lec 14: Recursion on Trees (E)	Homework 6/7	9
8	10/26/21 - Lec 15: UPGMA (E)	10/28/21 - Lec 16: More trees! (E)	Homework 8	10, 11
9	11/02/21 - Lec 17: RNA Folding (E)	11/04/21 - Midterm	Homework 9	
10	11/09/21 - Lec 18: Oops (E)	11/11/21 - Lec 19: Oops etc. (E)	Homework 10	CS For All Chapter 6
11	11/16/21 - Lec 20: Shapes! (E)	11/18/21 - Lec 21: Finishing up Oops (E)	Homework 11	CS For All Chapter 6
12	11/23/21 - Lec 22: Projects! (MJE)	11/25/21 - Happy Thanksgiving!	Project Descriptions	
13	11/30/21 - Theory 1 (G)	12/02/21 - Theory 2 (G)	Work on Projects	
14	12/07/21 - Theory 3 (G)	12/09/21 - Finale (MJE)	Work on projects	



CS 5 Green

Learning Goals

- Motivate the need for “care packages” in recursion



Care packages with change

```
def change(target, coinsL):  
    '''Accepts an integer and a list as inputs. Returns the fewest  
    number of coins needed to make the target integer.'''  
    # base case 1: no coins required  
    if target == 0: return 0  
  
    # base case 2: impossible to make change  
    elif coinsL == []: return float('inf')  
    else:  
        # discard coin if it exceeds the target  
        if coinsL[0] > target:  
            return change(target, coinsL[1:])  
  
        # try both using and losing a coin; return minimum req'd  
        else:  
            useIt = 1 + change(target - coinsL[0], coinsL)  
            loseIt = change(target, coinsL[1:])  
            return min(useIt, loseIt)  
  
>>> change(42, [25, 21, 1])  
2  
  
>>> showChange(42, [25, 21, 1])  
[2, [21, 21]]
```





showChange

Answer will be added
to slides after class

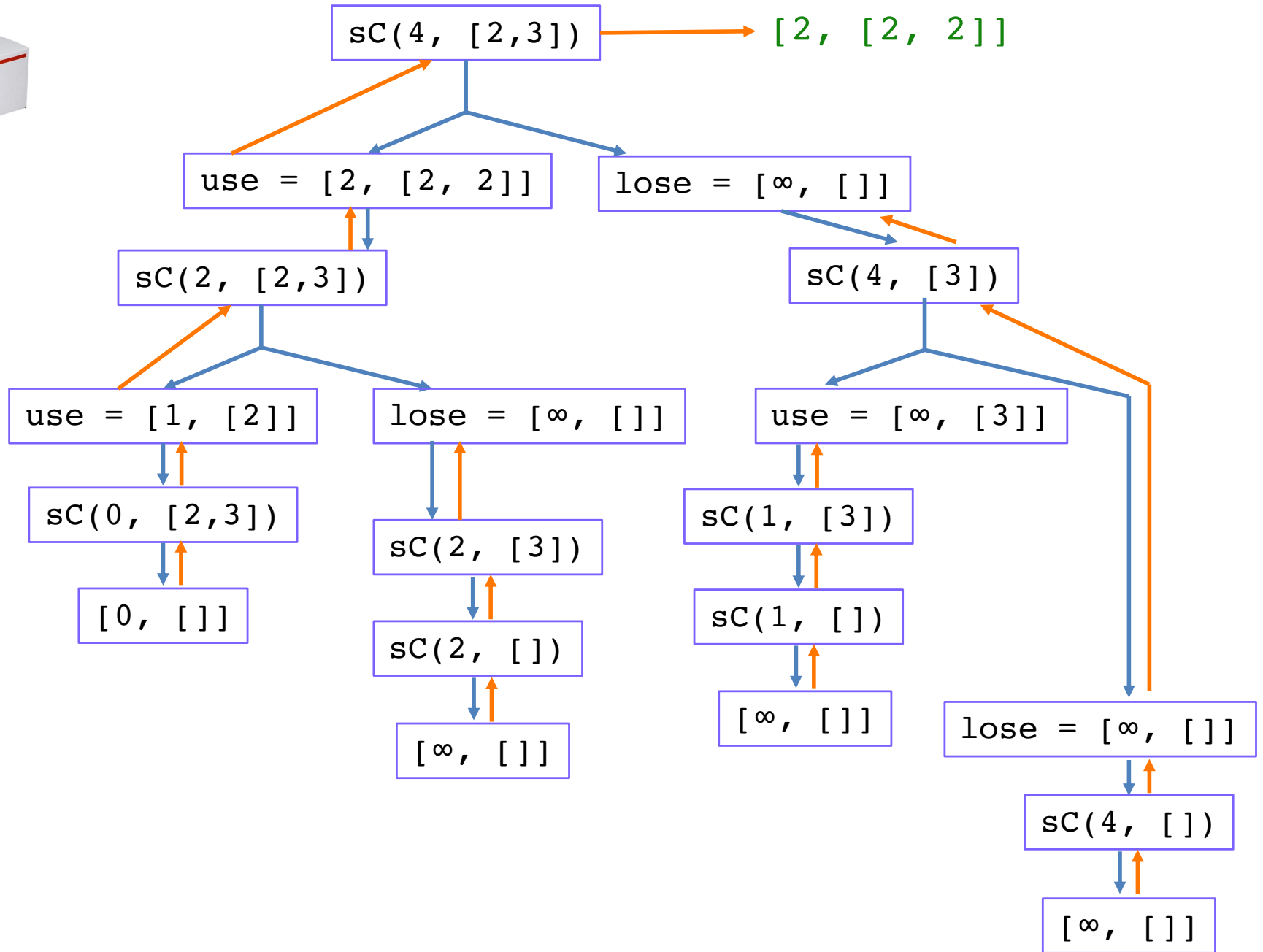
```
def showChange(target, coinsL):  
    """Accepts a target integer and a list of coins as inputs. Returns a list  
    containing two elements: the first element is the fewest number of coins  
    required, and second element is a list of the actual coins used."""
```




Answer will be added
to slides after class

showChange

```
def showChange(target, coinsL):  
    """Accepts a target integer and a list of coins as inputs. Returns a list  
    containing two elements: the first element is the fewest number of coins  
    required, and second element is a list of the actual coins used."""  
    # bc1: no coins needed  
    if target == 0: return [0, []]  
  
    # bc2: impossible to make change  
    elif coinsL == []: return [float("inf"), []]  
  
    # discard coin if it exceeds the target  
    elif coinsL[0] > target: return showChange(target, coinsL[1:])  
  
    else:  
        # try using a coin  
        useIt = showChange(target - coinsL[0], coinsL)  
        useIt[0] += 1 # update the number of coins used  
        useIt[1].append(coinsL[0]) # update the list with the coin used  
  
        # try losing a coin  
        loseIt = showChange(target, coinsL[1:])  
  
        # return the care package with the fewest coins used  
        if useIt[0] < loseIt[0]: return useIt  
        else: return loseIt
```



change and showChange return different *types*

```
>>> change(42, [25, 21, 1])  
2
```

```
>>> showChange(42, [25, 21, 1])  
[2, [21, 21]]
```

Another example with subset

```
def subset(target, inputL):  
    """Accepts an integer and a list of integers as inputs. Returns a  
    boolean indicating whether or not there exists a subset of numbers  
    in the list that adds up to the target."""  
    # bc1: if our target reaches 0, then a subset exists  
    if target == 0: return True  
  
    # bc2: if our list becomes empty, then a subset does not exist  
    elif inputL == []: return False  
  
    # discard a number if it exceeds the target; check remaining  
    elif inputL[0] > target: return subset(target, inputL[1:])  
  
    # otherwise, try both using and losing the first number  
    else:  
        useIt = subset(target - inputL[0], inputL[1:])  
        loseIt = subset(target, inputL[1:])  
        return useIt or loseIt
```

hw5pr1: memoSubset (10pts)

showSubset

worksheet

Q

```
def showSubset(target, inputL):  
    """Accepts an integer and a list of integers as inputs. Returns a two-item  
    list: the first item is a boolean indicating whether or not there exists a  
    subset of numbers in the list that adds up to the target, the second item is  
    a list of the subset of numbers used."""  
    # bc1:  
    if target == 0:  
  
    # bc2:  
    elif inputL == []:  
  
    elif inputL[0] > target:  
  
    else:
```

```
>>> showSubset(9,[2,3,5])  
[False, []]
```

```
>>> showSubset(10,[2,3,5])  
[True, [2, 3, 5]]
```

showSubset

worksheet

S

```
def showSubset(target, inputL):
    """Accepts an integer and a list of integers as inputs. Returns a two-item
    list: the first item is a boolean indicating whether or not there exists a
    subset of numbers in the list that adds up to the target, the second item is
    a list of the subset of numbers used."""
    # bc1: if our target reaches 0, then a subset exists
    if target == 0: return [True, []]

    # bc2: if our list becomes empty, then a subset does not exist
    elif inputL == []: return [False, []]

    # discard the number if it exceeds the target; check remaining
    elif inputL[0] > target: return showSubset(target, inputL[1:])

    # otherwise, try both using and losing the number
    else:
        useIt = showSubset(target - inputL[0], inputL[1:])
        useIt[1].append(inputL[0])    # keep track of the used number

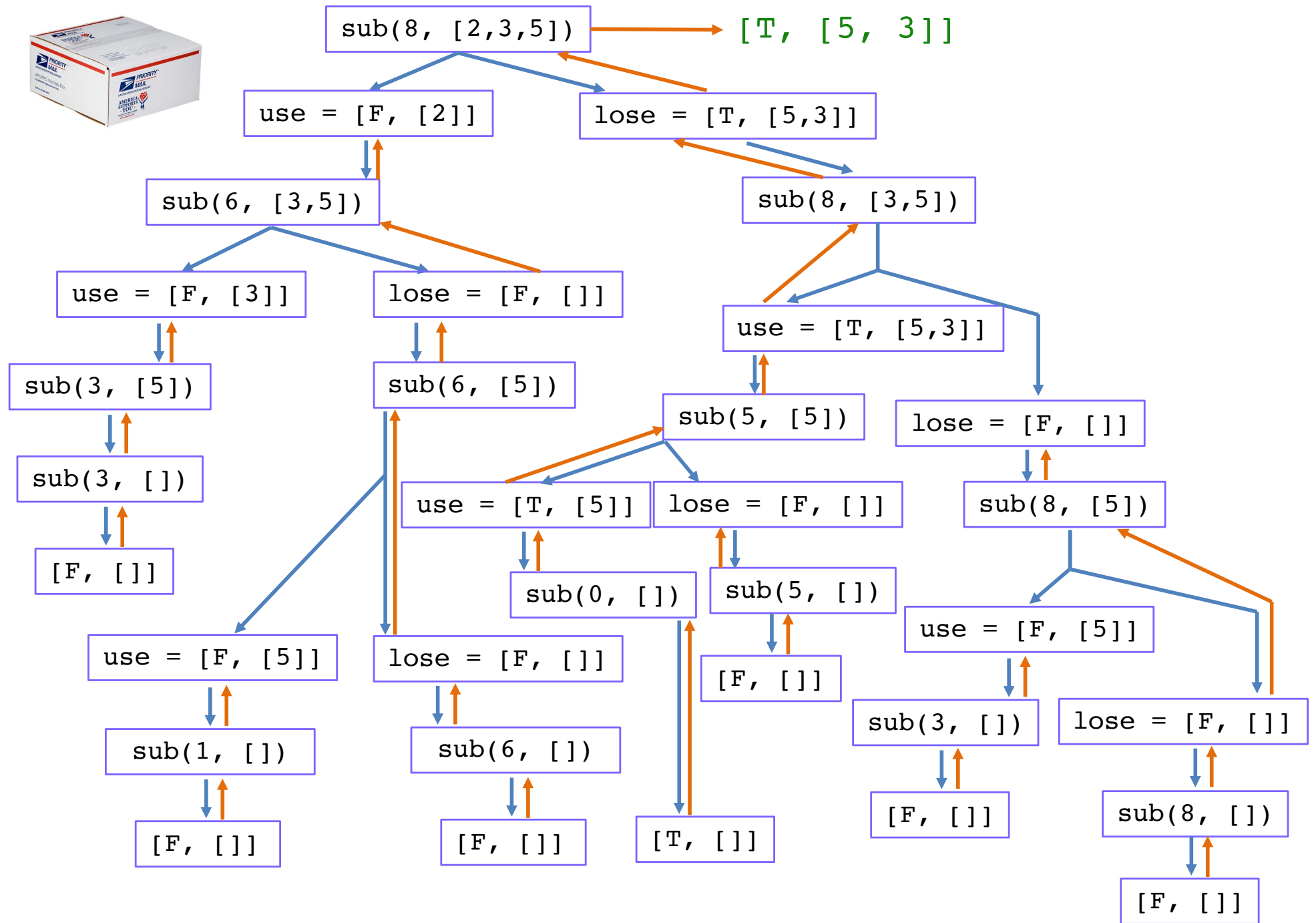
        loseIt = showSubset(target, inputL[1:])

        if useIt[0]: return useIt
        else: return loseIt
```

Answer will be added
to slides after class

```
>>> show_subset(9,[2,3,5])
[False, []]
```

```
>>> show_subset(10,[2,3,5])
[True, [2, 3, 5]]
```

A final example with LCS



```
def LCS(stringA, stringB):
    """Accepts two strings as input. Returns the length of
    the Longest Common Substring."""
    # base case
    if stringA == "" or stringB == "": return 0

    # add 1 if first characters match; check remaining
    elif stringA[0] == stringB[0]:
        return 1 + LCS(stringA[1:], stringB[1:])

    # try dropping 1 char from each string; return max
    else:
        option1 = LCS(stringA, stringB[1:])
        option2 = LCS(stringA[1:], stringB)
        return max(option1, option2)
```

```
>>> fancyLCS("human", "chimpanzee")
[4, 'h#man', '#h#m#an###']
```

In your notes...



```
else:
```

In your notes...

S

```
def fancyLCS(S1, S2):  
    """Accepts two strings as inputs. Returns a three item list  
    where the first item is the LCS length (int), and the second  
    and third items are the "pounded out" versions of S1 and S2."""  
    if S1 == "":    return [0, "", len(S2) * "#"]    # bc1  
  
    elif S2 == "": return [0, len(S1) * "#", ""]    # bc2  
  
    elif S1[0] == S2[0]: # if first chars match, then ...  
        match = fancyLCS(S1[1:], S2[1:]) # ... recurse ...  
        match[0] += 1                    # ... update LCS number ...  
        match[1] = S1[0] + match[1]      # ... update pounded S1 ...  
        match[2] = S2[0] + match[2]      # ... update pounded S2.  
        return match  
  
    else: # if first chars mismatch, then ...  
        option1 = fancyLCS(S1[1:], S2) # ... drop char from S1 ...  
        option1[1] = "#" + option1[1]  # ... "pound out" S1 ...  
  
        option2 = fancyLCS(S1, S2[1:]) # ... drop char from S2 ...  
        option2[2] = "#" + option2[2]  # ... "pound out" S2 ...  
  
        # ... return the better option  
        if option1[0] > option2[0]: return option1  
        else: return option2
```

Answer will be added
to slides after class

hw5pr2: superLCS (20pts)

```
>>> superLCS("human", "chimpanzee")  
[4, '-hu-m-an---', 'ch-impanzee']
```

-hu-m-an---
ch-impanzee

```
>>> superLCS("A", "AT")  
[1, 'A-', 'AT']
```

A-
AT

```
>>> superLCS("CG", "G")  
[1, 'CG', '-G']
```

CG
-G

GAC fancyLCS
 → [2 , ' #AC ' , ' AC ']

AC

GAC superLCS
 → [2 , ' GAC ' , ' -AC ']

AC

What is an alignment anyway?

Alignment representation

S1 **G**CC**T**GG-

S2 **A**CC-GG**A**

GCCTGG → **A**CCTGG (change G to A)

(keep the C)

(keep the C)

ACCT**T**GG → ACCGG

(delete the T)

(keep the G)

(keep the G)

ACCGG → ACCGG**A**

(insert A)

hw5pr3 + hw5pr4 (60pts): align and memoAlignScore

```
>>> alignScore("GCCTGG", "ACCGGA", -4, dnamat)  alignScore only  
11                                                returns score
```

```
>>> align("GCCTGG", "ACCGGA", -4, dnamat)        align returns score  
[11, 'gCCtGG-', 'aCC-GGa']                       and alignment
```

Reminder:

- Lecture feedback form
(<https://forms.gle/aPmkpXDUTp4Xo4CV7>)