

HMC Summer Research Celebration

Curious about research opportunities at HMC?

Want to learn more about your friend's summer project?

Come to the poster session to learn about projects happening across campus!



Thursday Sept 23
Drop by anytime between
4:30 - 6:30 pm

Attendees are eligible to
win raffle prizes

Zoom Meeting 868 2909 2950, Passcode D5sDRH
Make sure you have the latest version of Zoom

Common Mistakes

IT'S **OK** TO MAKE MISTAKES.



Common Mistakes (HW1)

```
def myFunction(input):  
    """This is a docstring. It should  
    describe the function as a whole."""  
  
    # this is a comment  
    print("Hello world!")  
  
    # comments should explain important lines or blocks  
    return 42
```

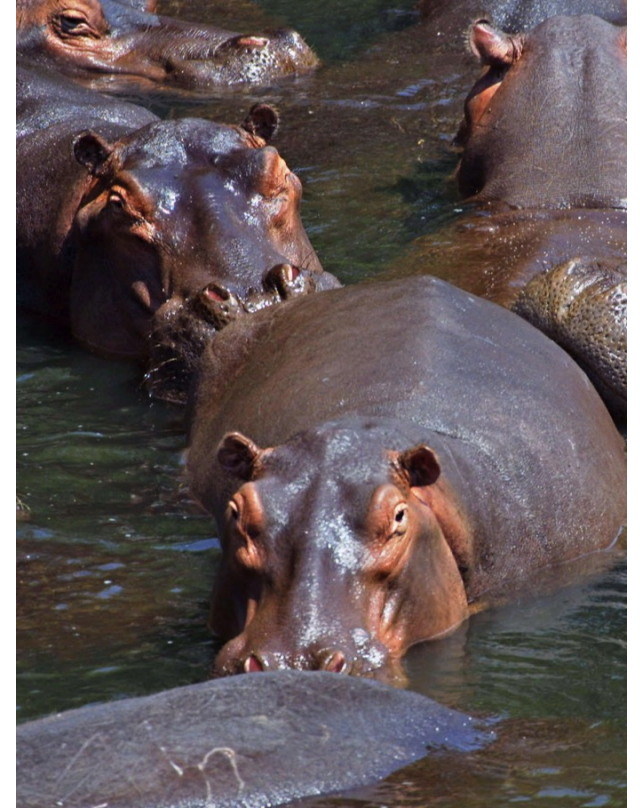
You **will** be graded on style and readability.

Docstrings

Comments

Purposeful variable names

Evolution of sex determination systems



http://en.wikipedia.org/wiki/American_alligator
<http://en.wikipedia.org/wiki/Amphiprioninae>
http://commons.wikimedia.org/wiki/File:Male_mallard_duck_3.jpg
<http://en.wikipedia.org/wiki/Hippopotamus>

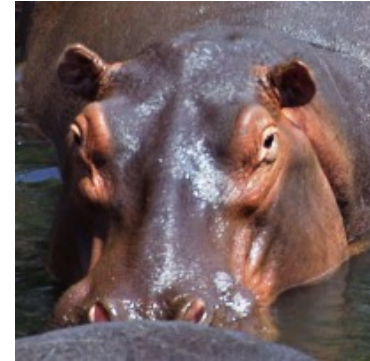
Chromosomal sex determination in birds and mammals



Z Z



Z W



X X



X Y



Do these sex-determination systems share a common ancestor or did they evolve independently???

Characteristics shared by descent are homologous



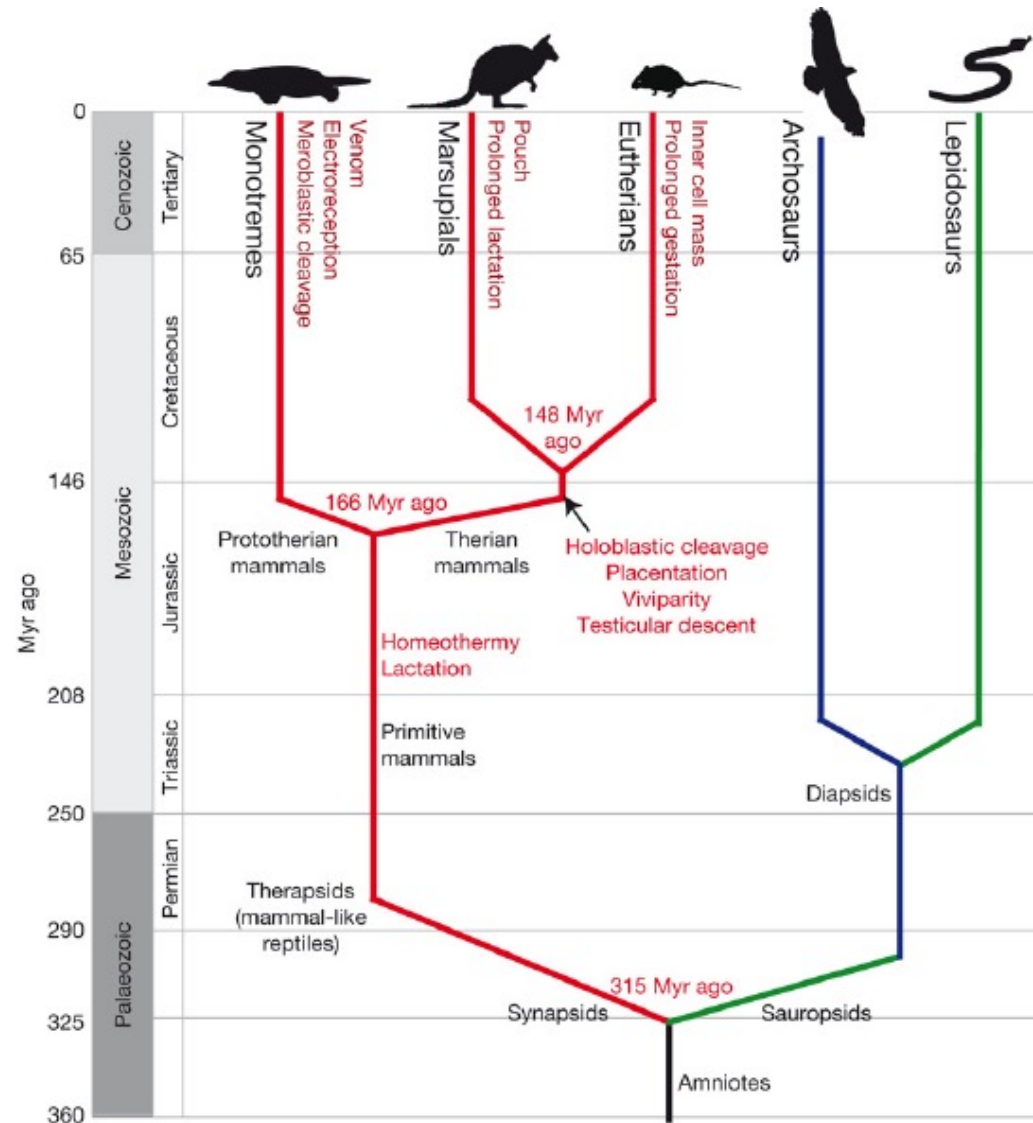
<http://www.flickr.com/photos/sunstones/2664993674/>

<http://www.flickr.com/photos/nycgeo/1065447484/sizes/z/in/photostream/>

<http://www.flickr.com/photos/bbum/98144389/sizes/z/in/photostream/>

http://commons.wikimedia.org/wiki/File:Mother_And_Baby_Elephant.jpg

Is the mammalian X homologous to the avian Z?

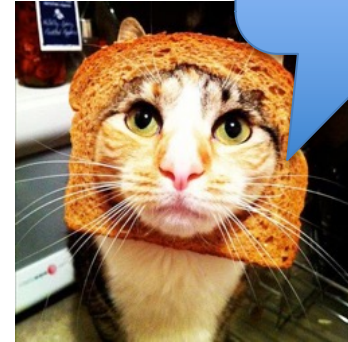


Some things that “require” more than for and while loops

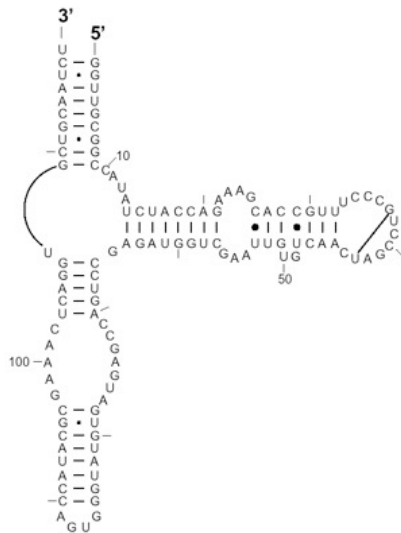
I'd be “toast” if
I had to do this
right now!

Measure similarity of two DNA sequences...

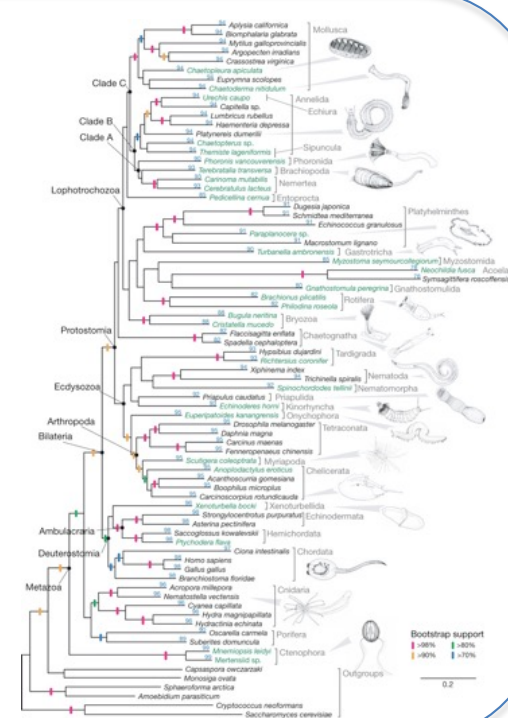
GGGACTCACTCATCAGTT
CACTCATTTGCAGTCATG



Predict how an RNA
sequence will fold...



Compute and
draw
phylogenetic
trees...



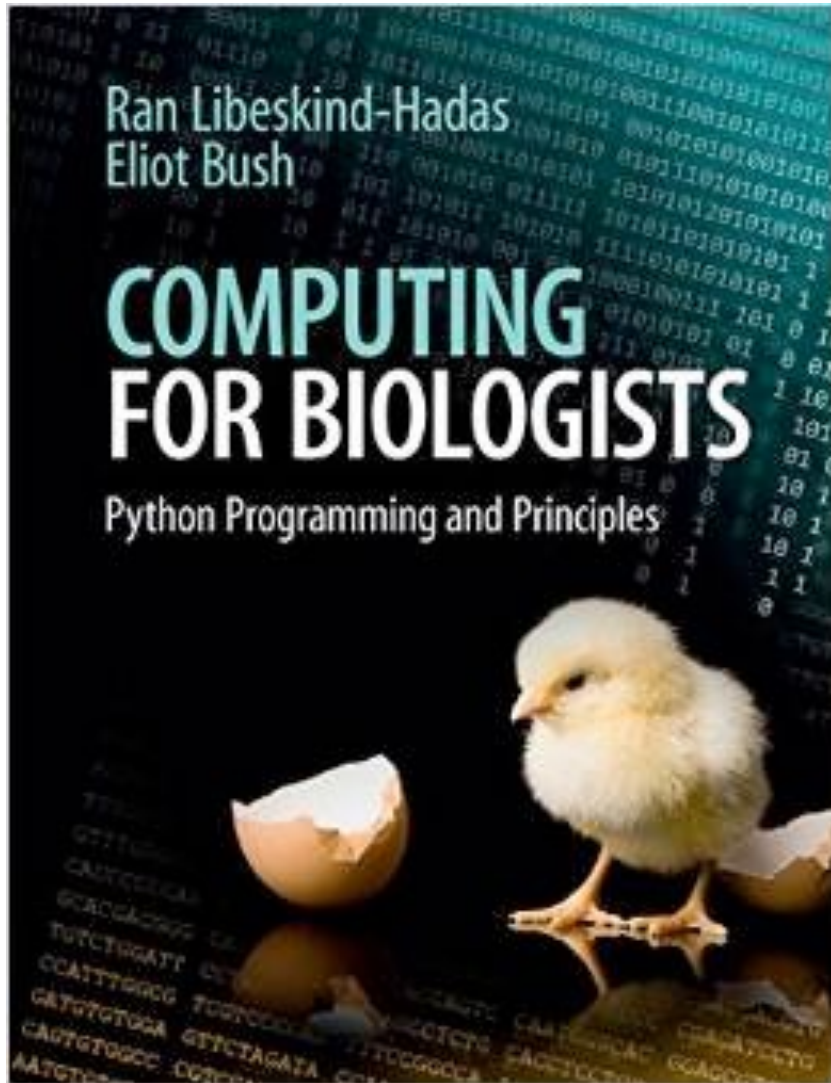


CS 5 Green

Learning Goals

- Describe the concept of recursion
- State the difference between the base case and recursive case
- Practice recursion
- State the tradeoffs between recursion and iteration

This week's reading...



Chapter 5: Recursion

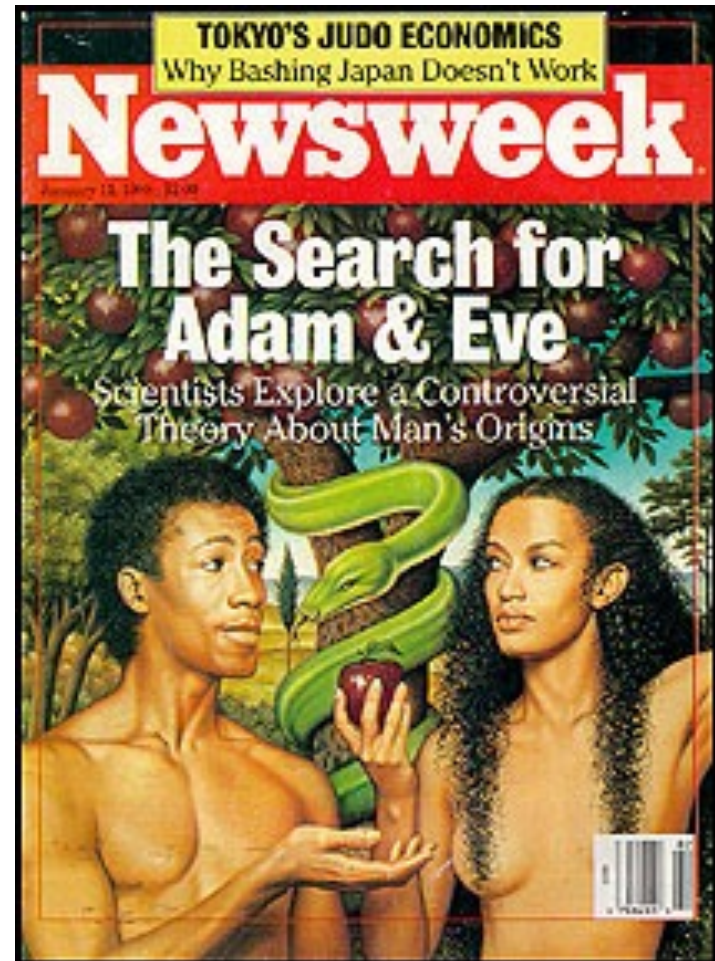
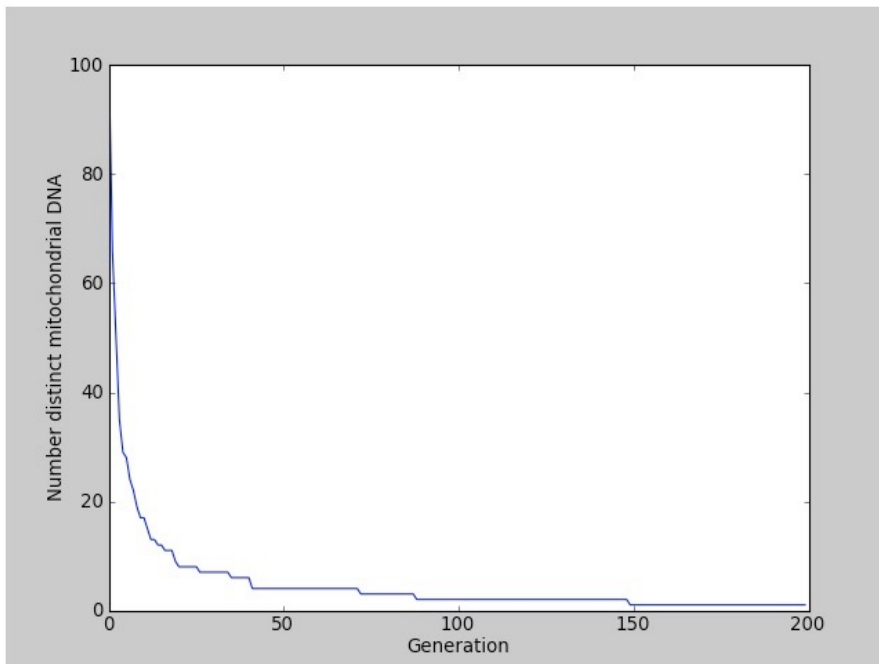
only 11 pages (dbl spaced!)



<https://2.flexiple.com/free-illustrations/reading-newspaper>

This week's homework...

Mitochondrial Eve!



This week's homework...

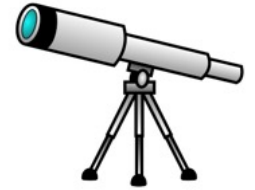
Got Milk?



Recursion! (Lab and Bonus)



A word about “scope”



```
def joe(x):  
    y = bjorn(x)  
    z = x + y  
    return z
```

```
def bjorn(x):  
    x = 42  
    return 2
```

```
>>> joe(1)
```



What does
joe(1) return?



What Happens Inside a Function?

```
def h(x):  
    return f(x) + x
```

```
def f(x):  
    x = x-1  
    return g(x)+1
```

```
def g(x):  
    return x*2
```

Remember, each
function has its
own private
variables!



Two key points...

- Functions return to where they were called from
- Each function keeps its own values of its variables

Factorial (iterative)

$$n! = n \times (n-1) \times (n-2) \times \dots \times 1$$

```
def factorial(n):  
    # initialize result  
    result = 1  
  
    # multiply each number between 1 and n  
    for curNum in range(1, n+1):  
        result = result * curNum  
  
    return result
```



Using loops to solve problems is called **iteration**.

Factorial (recursive)

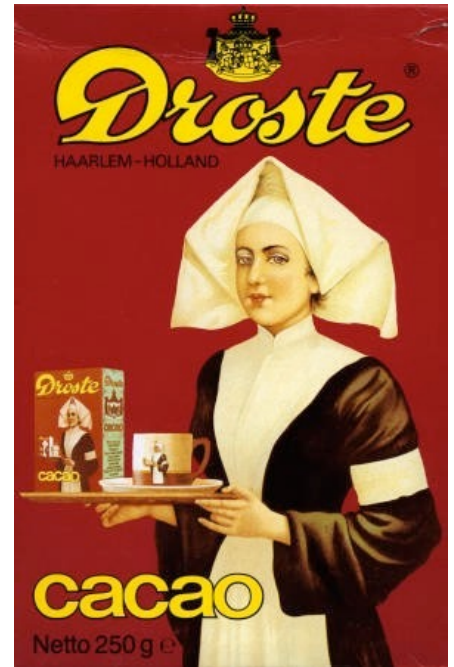
iterative solution

$$n! = n \times (n-1) \times (n-2) \times \dots \times 1$$

$$n! = n \times (n-1)! \quad \text{"recursive case"}$$

$$0! = 1 \quad \text{"base case"}$$

recursive solution



Recursive function: a function which includes **itself** as part of its definition.

Factorial (recursive)

Base case

Math

inductive definition

$$0! = 1$$

$$n! = n \times (n-1)!$$

Recursive case

Python (Functional)

recursive function

```
# recursive factorial  
def factorial(n):
```

```
    # base case: n equals zero  
    if n == 0:  
        return 1
```

```
    # recursive case: n > 0  
    else:  
        return n * factorial(n-1)
```

The input to the recursive call is **simpler** than the original input!!

Is Recursion Magic?

```
factorial(3):
```

```
    return 3 * factorial(2)
```

```
factorial(2):
```

```
    return 2 * factorial(1)
```

```
factorial(1):
```

```
    return 1 * factorial(0)
```

```
factorial(0):
```

```
    return 1
```

```
# recursive factorial
def factorial(n):
    if n == 0:
        return 1
    else:
        return n*factorial(n-1)
```

Is Recursion Magic?

```
factorial(3):
```

```
    return 3 * factorial(2)
```

```
factorial(2):
```

```
    return 2 * factorial(1)
```

```
factorial(1):
```

```
    return 1 * (1)
```

```
# recursive factorial
def factorial(n):
    if n == 0:
        return 1
    else:
        return n*factorial(n-1)
```


Is Recursion Magic?

```
factorial(3):
```

```
    return 3 * factorial(2)
```

```
factorial(2):
```

```
    return 2 * (1)
```

2



```
# recursive factorial
def factorial(n):
    if n == 0:
        return 1
    else:
        return n*factorial(n-1)
```

Is Recursion Magic?

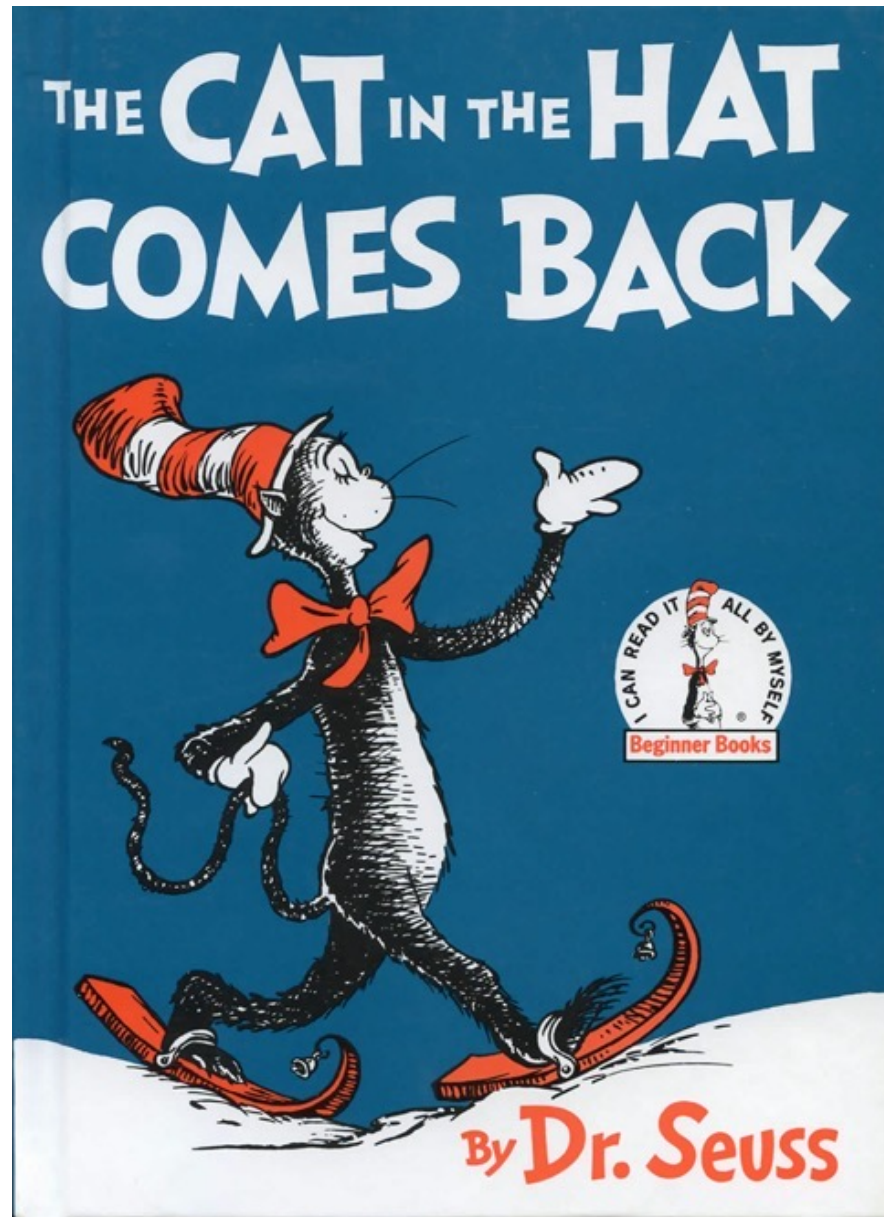
```
factorial(3):
```

```
    return 3 * (2)
```

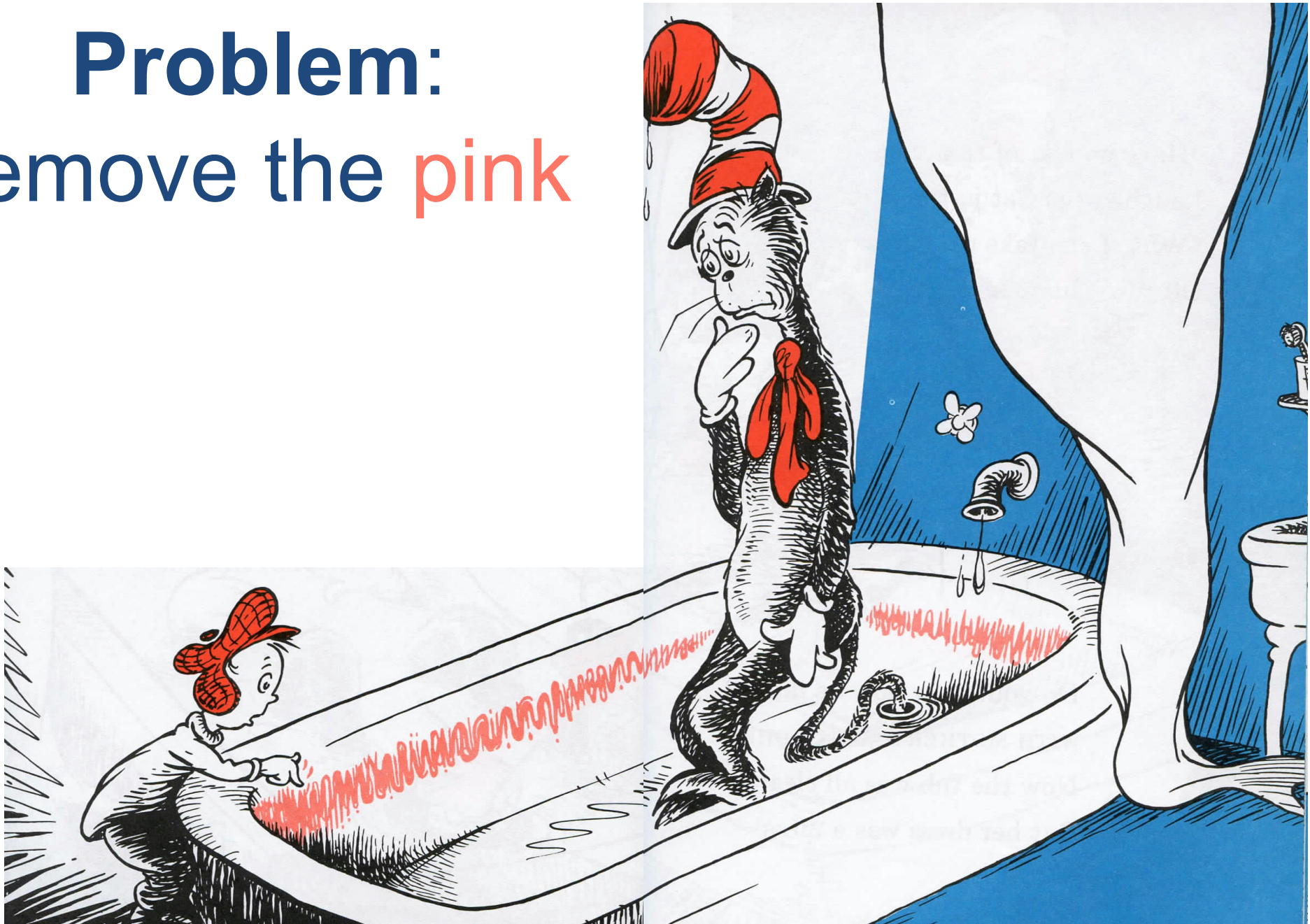
→ 6

```
# recursive factorial
def factorial(n):
    if n == 0:
        return 1
    else:
        return n*factorial(n-1)
```

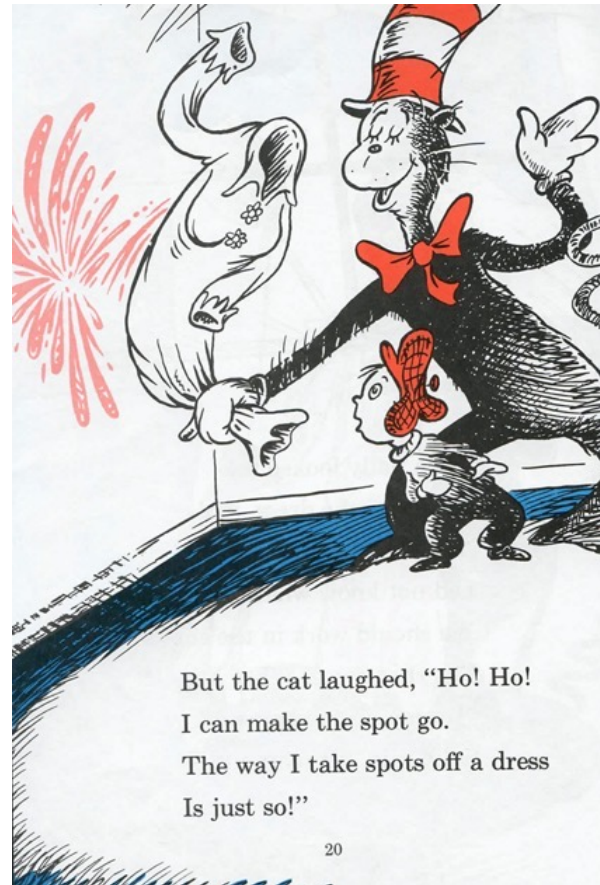
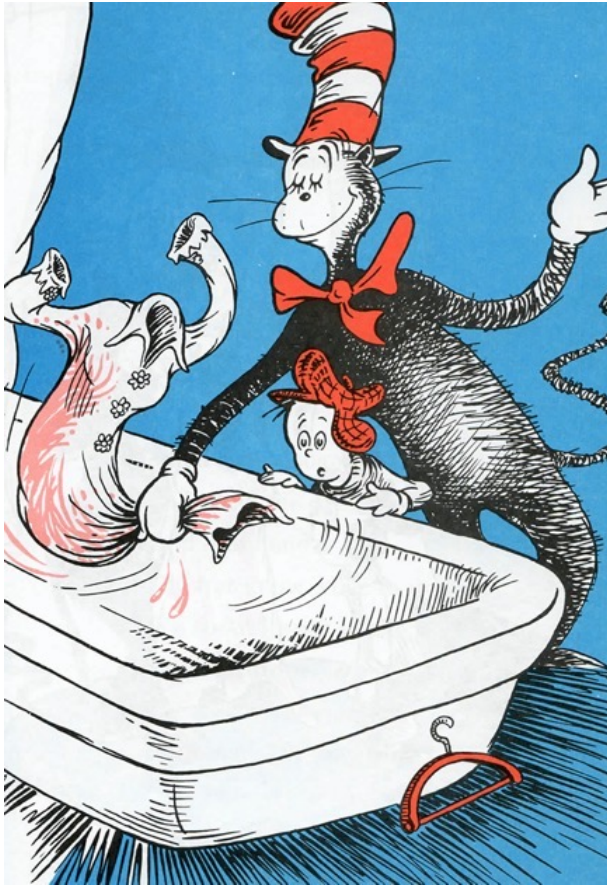
Recursion in a children's book



Problem:
remove the pink



Non-recursive attempts fail



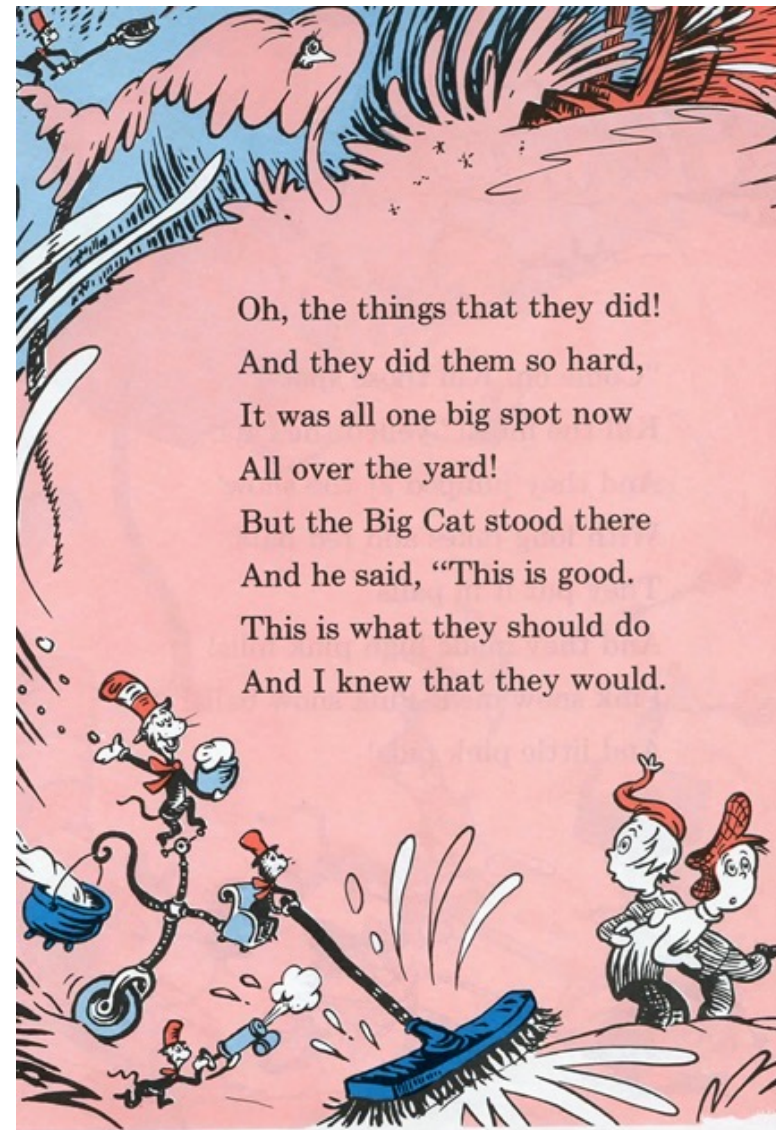
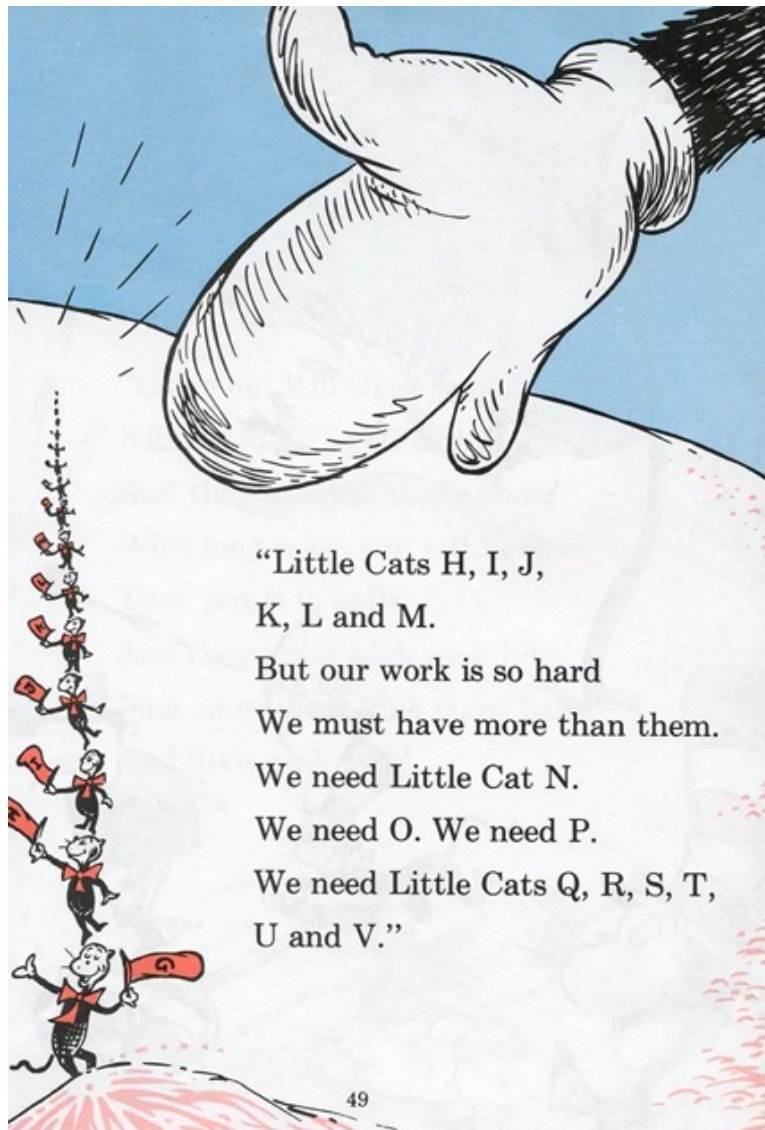
Non-recursive attempts fail



The Cat implements recursion



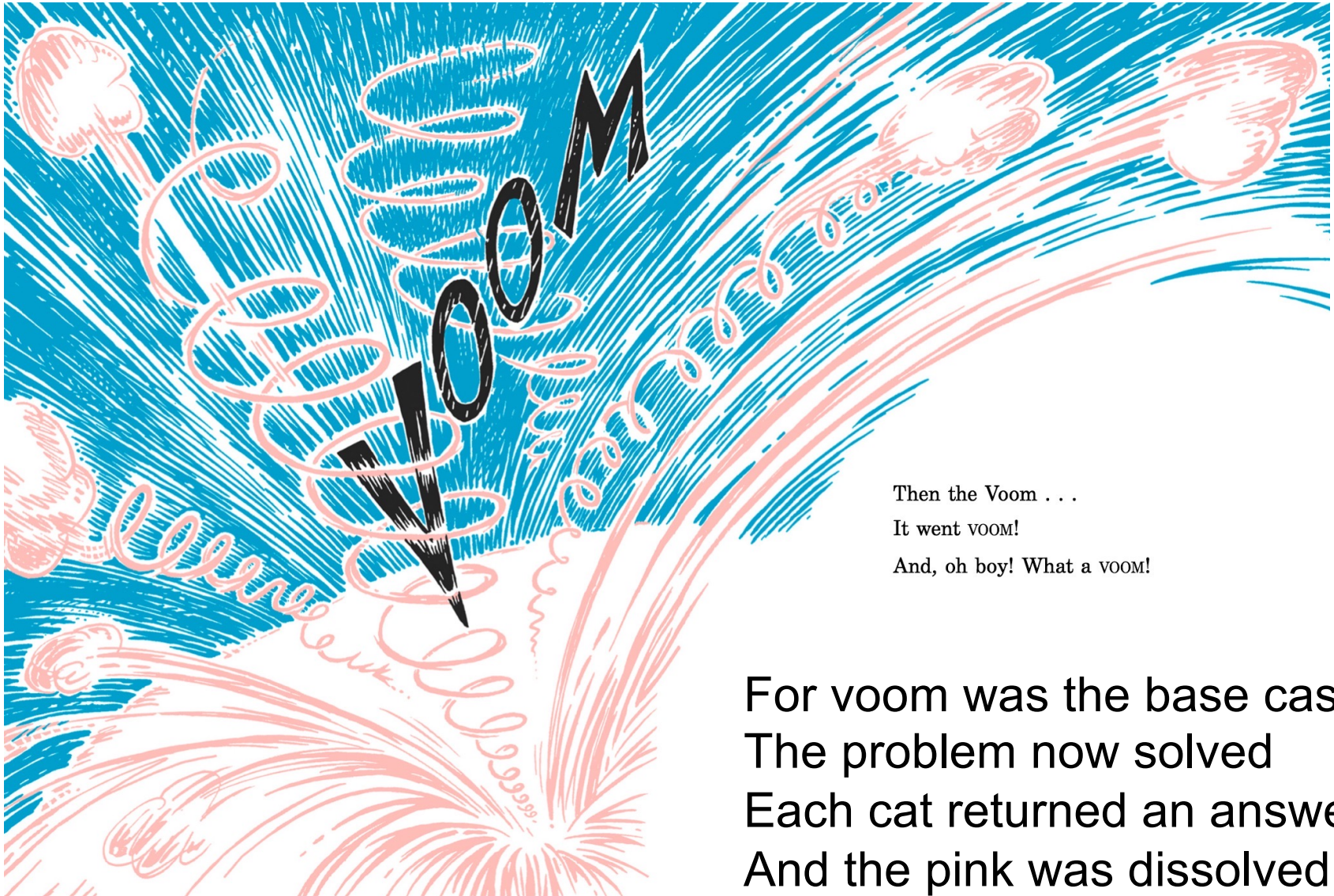
The Cat implements recursion



Cat Z reaches the base case

“Now here is the Z
You can’t see,” said the Cat.
“And I bet you can’t guess
What he has in HIS hat!”





Then the Voom . . .
It went voom!
And, oh boy! What a voom!

For voom was the base case
The problem now solved
Each cat returned an answer
And the pink was dissolved

Computing the length of a list

```
>>> len([1, 42, "spam"])
```

```
3
```

```
>>> len([1, [2, [3, 4]]])
```

```
2
```

Python has
this built-in!



```
def len(inputL):
```

```
    '''Returns the length of a list'''
```

Summing up the numbers in a list

Q

```
>>> sum([1, 42, 7])
```

```
50
```

```
>>> sum([42])
```

```
42
```

```
>>> sum([])
```

```
0
```

```
def sum(inputL):
```

```
    '''Returns the sum of numbers in a list'''
```



Python has
this built-in
too!

No new variables required!

```
def len(inputL):  
    '''RECURSIVE VERSION'''  
    if inputL == []:  
        return 0  
    else:  
        return 1 + len(inputL[1:])
```



Intermediate values
stored in “stack
frames” instead!

```
def lenV2(inputL):  
    '''ITERATIVE VERSION'''  
    counter = 0    # a new variable!  
    for x in inputL: # another new variable  
        counter += 1  
    return counter
```

[🐢, 🐢, 🐢] Reversing a list



```
>>> reverse([1, 2, 3, 4])  
[4, 3, 2, 1]
```

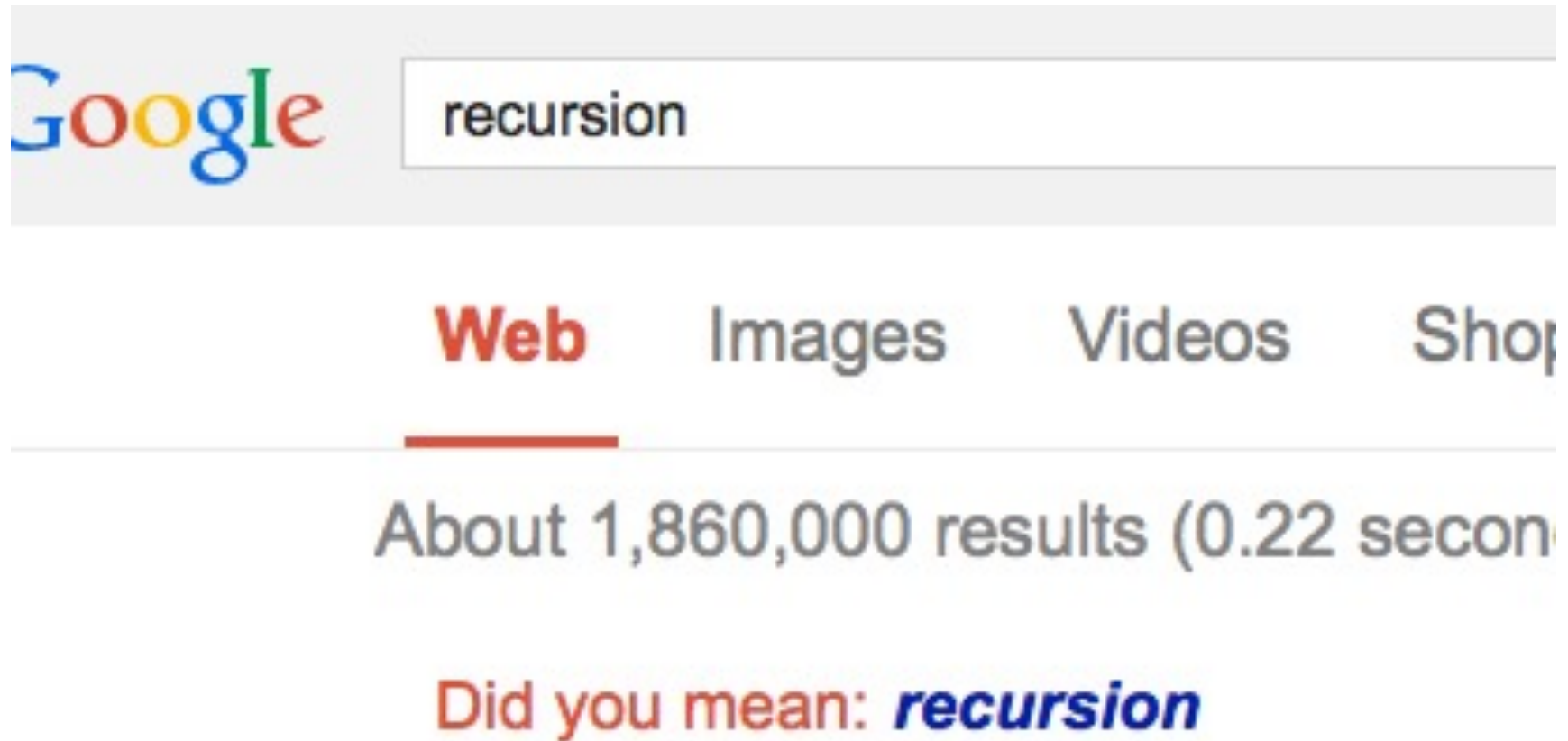
```
def reverse(inputL):  
    '''reverses the order of a list'''
```

Recursion <(°ε°<)

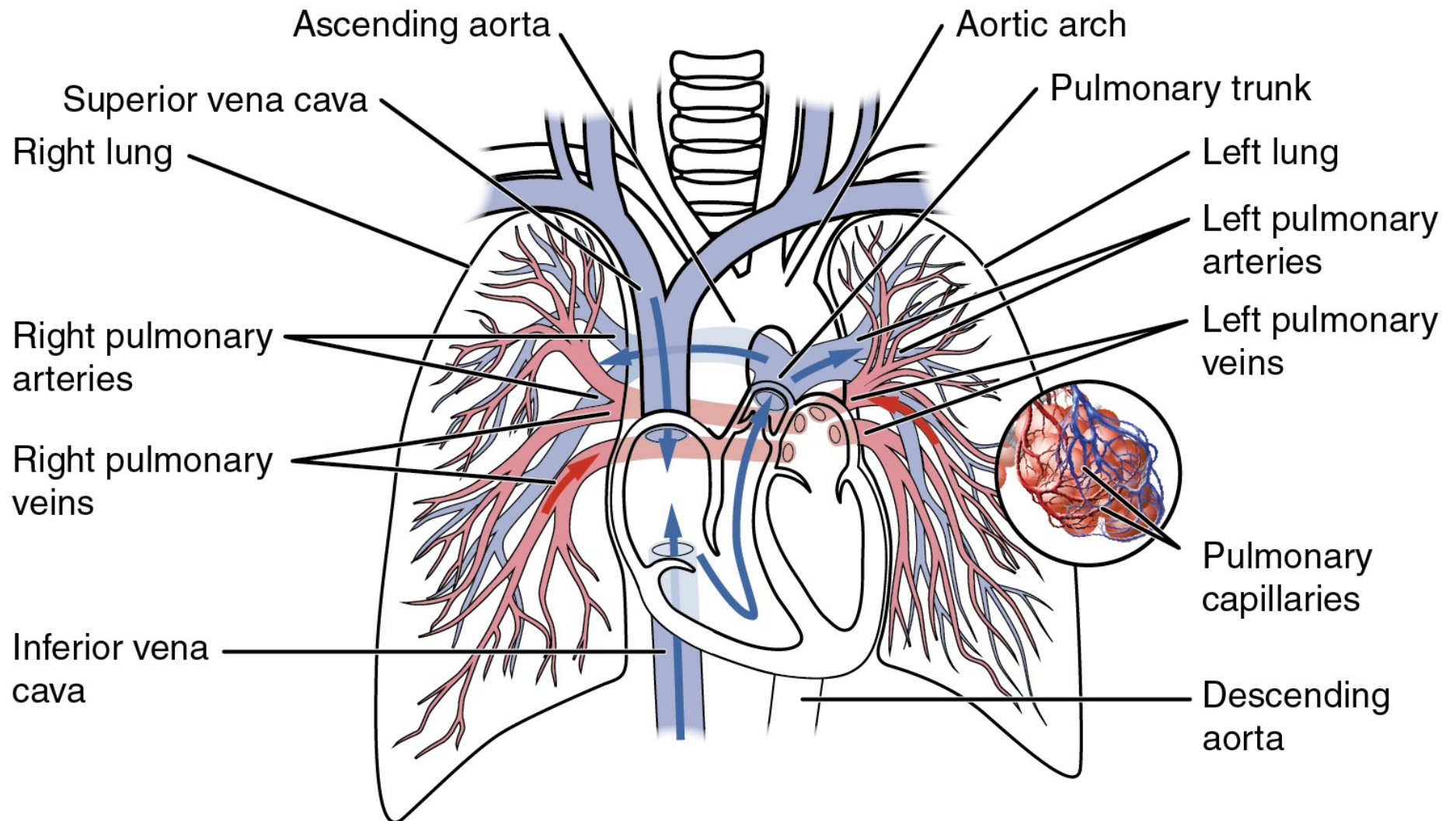
“To understand recursion, you must first understand recursion”
- anonymous Mudd alum



Recursion $\angle(\epsilon\angle)$



Recursion in nature

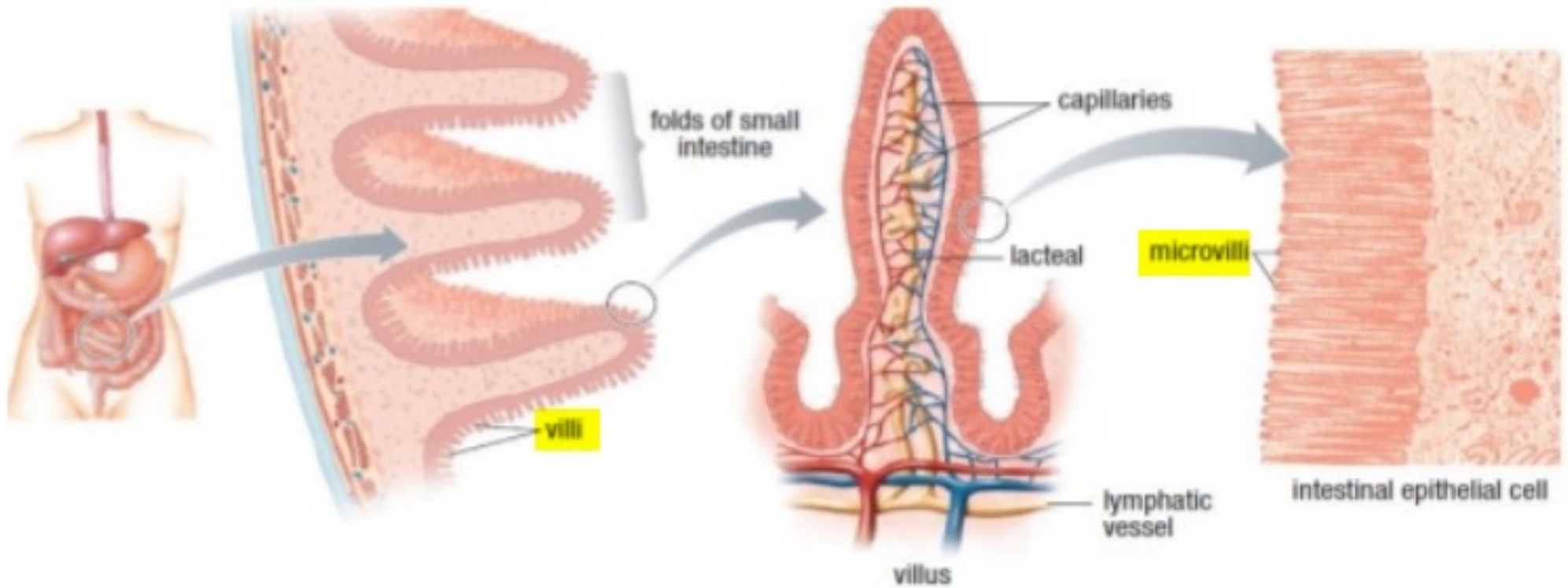


Recursion in nature



<https://commons.wikimedia.org/w/index.php?curid=6777039>

Recursion in nature



Recursion in nature



The following pages have
a number of exercises for
you to do (in your notes).
You're welcome to work at
your own pace.



```
min  
member  
pal
```

```
*insert/sort*
```

[ ,  , ]

Minimum!

Q

```
>>> min([372, 112, 42, 451])
```

```
42
```

```
>>> min([16])
```

```
16
```

Assume that the input list will never be empty!
Use len as a helper function!



```
def min(inputL):
```

```
    '''Returns smallest value in a list'''
```


member

Q

```
>>> member(42, [1, 3, 5, 42, 7])
```

```
True
```

```
>>> member(42, ['spam', 'is', 'yummy'])
```

```
False
```

This is sort of like the “in” thing in Python, but don’t use “in” here. Just list indexing, slicing, and recursion!



```
def member(thing, inputL):  
    '''Return True if thing in inputL  
    and False otherwise.'''
```

Palindrome?



```
>>> pal('radar')
```

```
True
```

```
>>> pal('amanaplanacanalpanama')
```

```
True
```

```
>>> pal('spam')
```

```
False
```

```
def pal(s):
```

```
    '''Returns True if s is a palindrome  
    and False otherwise'''
```

Insertion Sorting



Challenge
Question

```
>>> sort([42, 57, 1, 3])  
[1, 3, 42, 57]
```

The **idea**... Given a list like `L = [42, 57, 1, 3]`

- Slice off the first element. Now we have a shorter list... `[57, 1, 3]`
- Use recursion to sort that list. Now we have... `[1, 3, 57]`
- Now, insert `L[0]` (Which is `42`) into the right place in `[1, 3, 57]`...
`[1, 3, 42, 57]`

```
def insert(x, sorted_list):  
    '''Takes a number and sorted list as input and returns a new list  
    that has x inserted into the right place in the sorted list'''
```

```
def sort(my_list):  
    '''Sorts a list using insert as a helper function'''
```