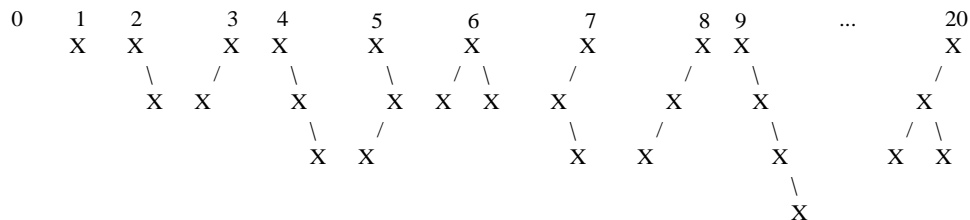


### Problem D: Trees Made to Order

We can number binary trees using the following scheme:

- The empty tree is numbered 0.
- The single-node tree is numbered 1.
- All binary trees having  $m$  nodes have numbers less than all those having  $m + 1$  nodes.
- Any binary tree having  $m$  nodes with left and right subtrees  $L$  and  $R$  is numbered  $n$  such that all trees having  $m$  nodes numbered  $> n$  have either
  - left subtrees numbered higher than  $L$ , or
  - a left subtree =  $L$  and a right subtree numbered higher than  $R$ .

The first 10 binary trees and tree number 20 in this sequence are shown below:



Your job for this problem is to output a binary tree when given its order number.

#### Input

Input consists of multiple problem instances. Each instance consists of a single integer  $n$ , where  $1 \leq n \leq 500,000,000$ . A value of  $n = 0$  terminates input. (Note that this means you will never have to output the empty tree.)

#### Output

For each problem instance, you should output one line containing the tree corresponding to the order number for that instance. To print out the tree, use the following scheme:

- A tree with no children should be output as X.
- A tree with left and right subtrees  $L$  and  $R$  should be output as  $(L')X(R')$ , where  $L'$  and  $R'$  are the representations of  $L$  and  $R$ .
  - If  $L$  is empty, just output  $X(R')$ .
  - If  $R$  is empty, just output  $(L')X$ .

#### Sample Input

```
1
20
31117532
0
```

#### Sample Output

```
X
((X)X(X))X
(X(X((X(X))X(X))X(X)))X((X((X)X((X)X)))X)X
```