

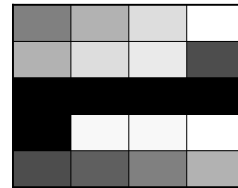
digital image processing

a digital image is a grid of sample color values

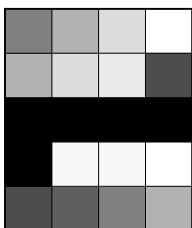
digital image example

.38	.22	.1	.009
.28	.17	.18	.58
.99	.99	.99	.98
.97	.07	.07	.009
.5	.48	.38	.21

conventional representation



digital image creation



synthesize



sample an analog image

fidelity

- discrete samples
- quantized colors

discrete samples



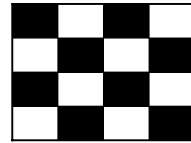
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nyquist criteria

sample at more than twice the highest frequency to avoid aliasing



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fidelity

- discrete samples
- **quantized colors**

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color quantization

- number of channels
- bits per channel

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channels



1 channel



3 channel

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three channel color models

- RGB: red, green, blue
- HSV: hue, saturation, value

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RGB model

- In a b -bit image, each channel is represented by
 - an integer in the range $[0, 2^{b-1}]$
 - one of 2^{b-1} rational numbers in the range $[0,1]$
- We'll use the latter method with 0=no color and 1=full color

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bits per channel



1 channel,
1 bit per channel



1 channel,
8 bits per channel

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Quiz

- In a 3-channel image what color is a pixel with value
 - (1,0,0)
 - (0,1,0)
 - (1,0,1)
 - (1,1,1)
 - (0,0,0)
 - (0.5,0.5,0.5)

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digital image processing

- avoid/correct errors
- restore
- enhance
- analyze
- synthesize

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types of techniques

- simple pixel modification
- interpolation/extrapolation
- compositing
- convolution
- dithering
- warping
- morphing
- misc. effects

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types of techniques

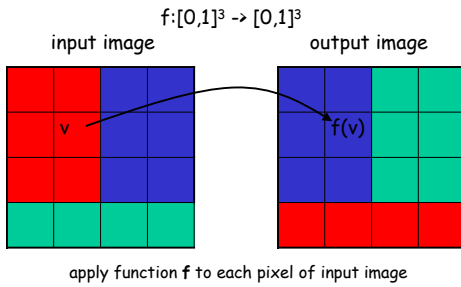
- **simple pixel modification**
- interpolation/extrapolation
- compositing
- convolution
- dithering
- warping
- morphing
- misc. effects

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simple pixel modification

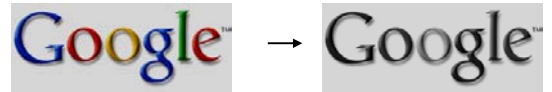


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convert to gray



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convert to gray

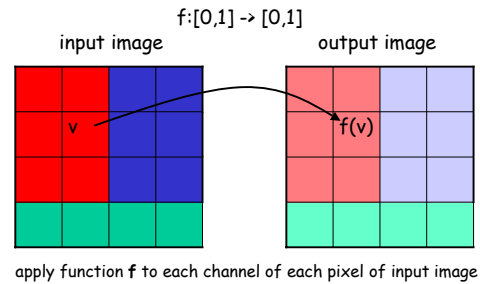
$$f(r,g,b) = .3r + .59g + .11b$$

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simple pixel modification

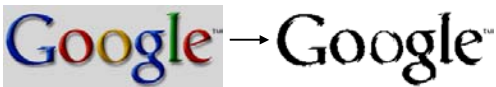


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threshold



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threshold

$$\begin{aligned} \text{if } v > t \text{ then } f(v) &= 1 \\ \text{else } f(v) &= 0 \end{aligned}$$

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invert



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invert

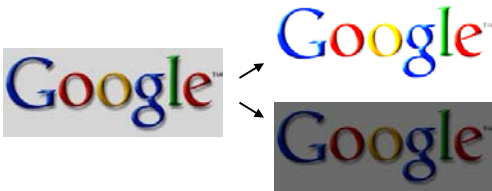
$$f(v) = 1-v$$

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brighten/darken



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brighten/darken

$$f(v) = \alpha v \text{ for } \alpha \geq 0$$

clamp to [0,1]

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types of techniques

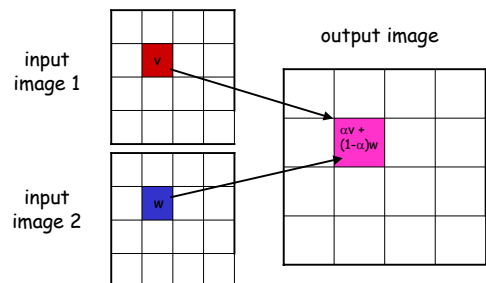
- simple pixel modification
- **interpolation/extrapolation**
- compositing
- convolution
- dithering
- warping
- morphing
- non-photo-realistic effects

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interpolation/extrapolation

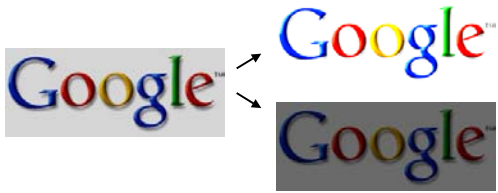


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interpolation/extrapolation



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brighten/darken

interpolate/extrapolate image with

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invert

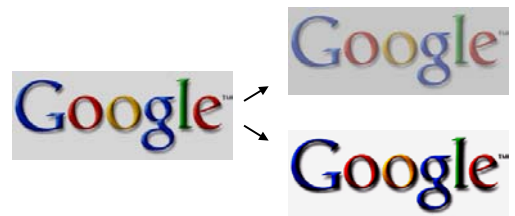
interpolate/extrapolate image with

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change contrast



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change contrast

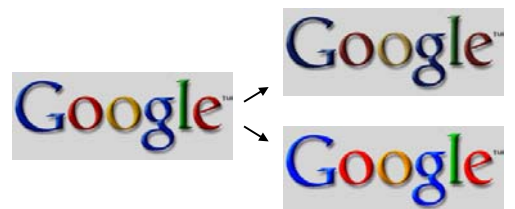
interpolate/extrapolate image with

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change saturation



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change saturation

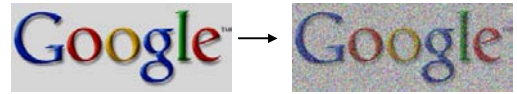
interpolate/extrapolate image with

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noisify



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noisify

interpolate/extrapolate with

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type of techniques

- simple pixel modification
- interpolation/extrapolation
- **compositing**
- convolution
- dithering
- warping
- morphing
- misc. effects

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compositing

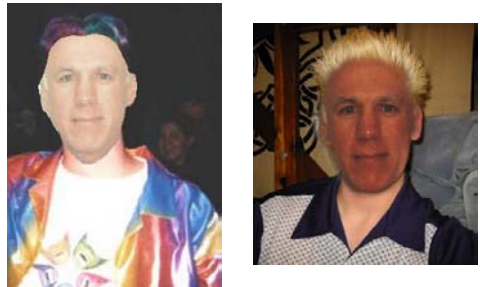


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compositing

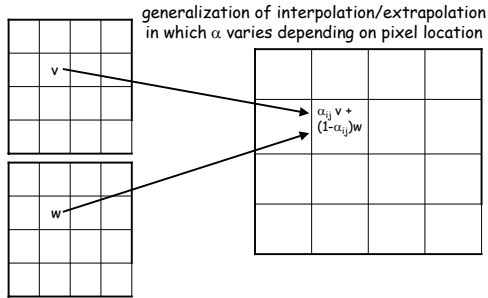


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compositing



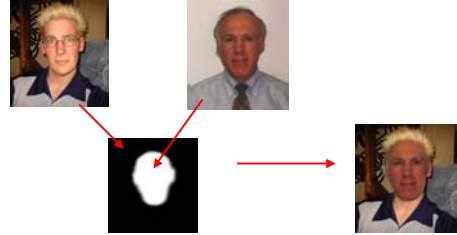
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compositing

typically $\alpha \in [0,1]$ so the array of α values can be represented by a single channel image called a *mask*



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type of techniques

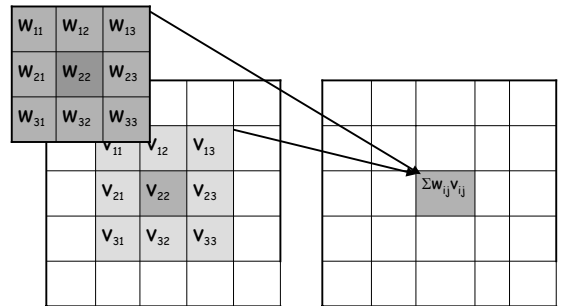
- simple pixel modification
- interpolation/extrapolation
- compositing
- **convolution**
- dithering
- warping
- morphing
- misc. effects

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convolution

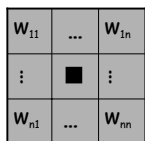


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kernel



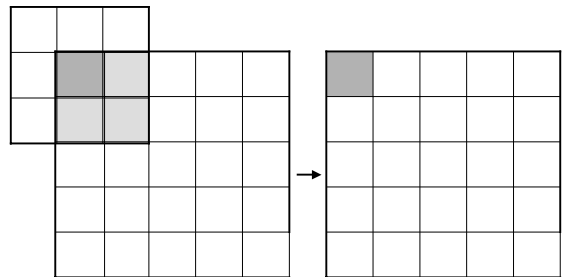
n odd

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boundaries?



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edge detect



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edge detect kernel

-1	-1	-1
-1	8	-1
-1	-1	-1

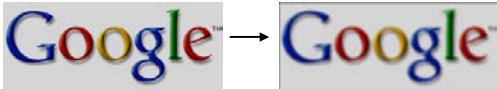
need to clamp values to [0,1]

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blur



why blur?

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anti-aliasing



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3x3 box blur

1/9	1/9	1/9
1/9	1/9	1/9
1/9	1/9	1/9

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nXn box blur

w	...	w
⋮	■	⋮
w	...	w

$$w=1/n^2$$

why is it important that the sum of the weights is 1?

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box blur vs. triangle blur



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3x3 triangle blur

1/16	1/8	1/16
1/8	1/4	1/8
1/16	1/8	1/16

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separability

1/4	1/16	1/8	1/16
1/2	1/8	1/4	1/8
1/4	1/16	1/8	1/16
	1/4	1/2	1/4

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separability

a kernel is separable if $W_{ij} = w_i w_j$

is the box filter separable?

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$n \times n$ triangle blur kernel

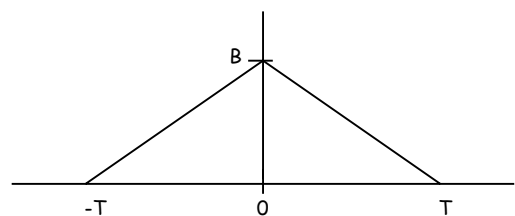
- Compute sample values for 1D triangle function: $s_{-T+1}, \dots, s_0, \dots, s_{T-1}$
- Compute kernel $W_{ij} = s_{i-T+1} s_{j-T+1}$

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triangle function

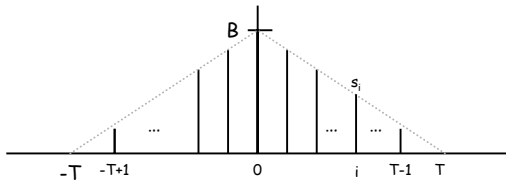


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discrete triangle



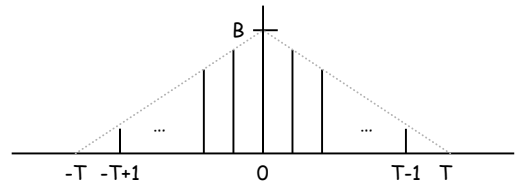
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normalized, discrete triangle

1. $T = (n+1)/2$ chosen to give n non-zero samples
2. $B = 2/(n+1)$ chosen so that $\sum_{i=-T+1}^{T-1} s_i = 1$



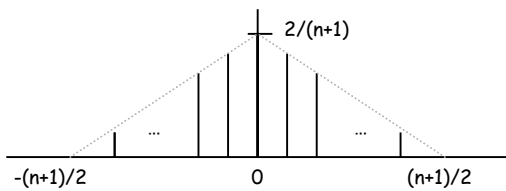
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normalized, discrete triangle

N is odd so samples are taken at integer values

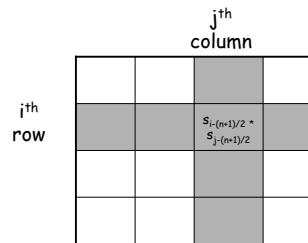


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triangle blur filter



for row $i=1, \dots, n$ and column $j=1, \dots, n$

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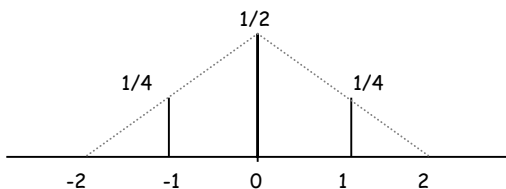
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example: $n=3$

$$T = (n+1)/2 = 2$$

$$B = 2/(n+1) = 1/2$$



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3x3 triangle blur filter

1/4	1/16	1/8	1/16
1/2	1/8	1/4	1/8
1/4	1/16	1/8	1/16
	1/4	1/2	1/4

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box, triangle and gaussian blurs



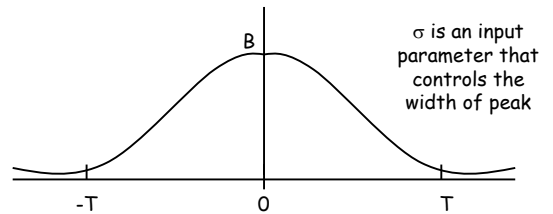
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gaussian function

$$f(x) = Be^{-x^2/\sigma^2}$$



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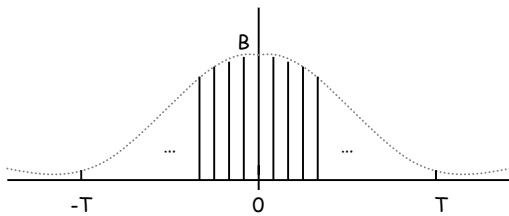
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normalized, discrete version

$T = (n+1)/2$ gives n samples

$B = 1/(\sum_{i=-T+1}^{T-1} e^{i^2/\sigma^2})$ is the normalizing constant

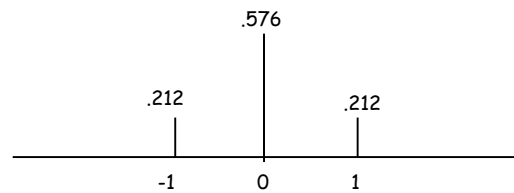


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example: $n=3, \sigma=1$



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3x3 gaussian blur, $\sigma = 1$

.212	.045	.122	.045
.576	.122	.332	.122
.212	.045	.122	.045
	.212	.576	.212

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type of techniques

- simple pixel modification
- interpolation/extrapolation
- compositing
- convolution
- **dithering**
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