

cs155 - z sweedyk

graphics
pipeline
systems

2/23/2003 CS155 - Subject 1

who's who

```

    graph LR
      end_user[end user] --> app[application program]
      app <--> pipeline[graphics pipeline]
      pipeline --> end_user
  
```

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who's who for today

```

    graph LR
      user[user] <--> pipeline[graphics pipeline]
  
```

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user defined scene description

- models
- lights
- view (eye/camera)

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graphics pipeline

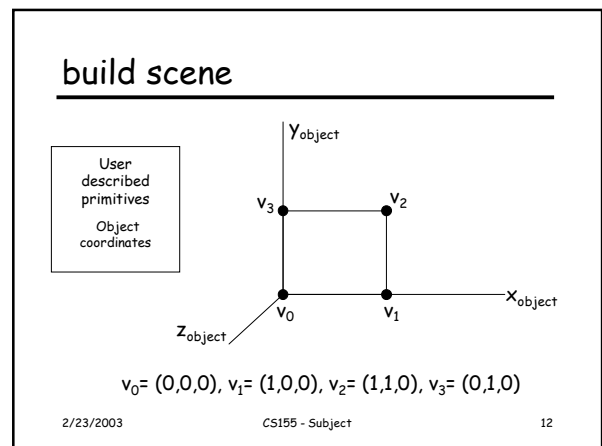
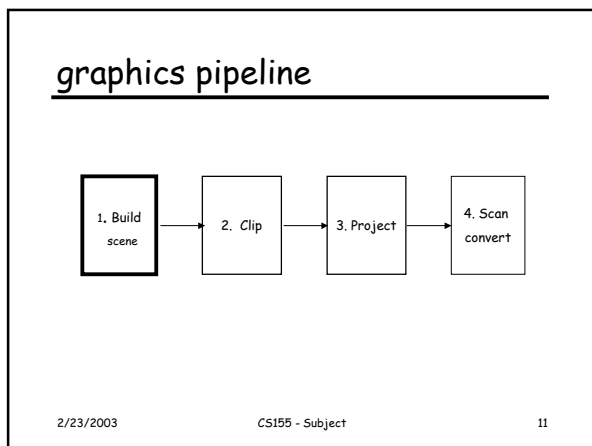
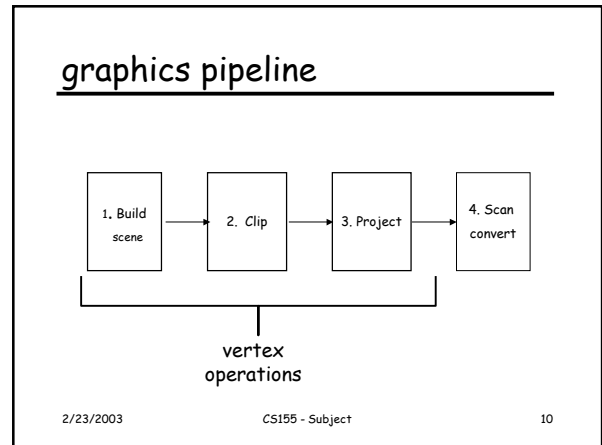
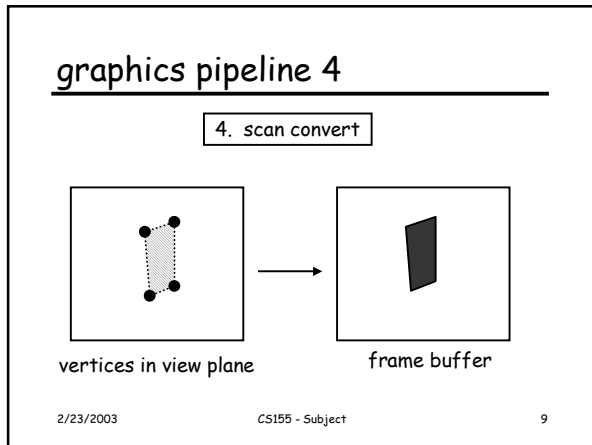
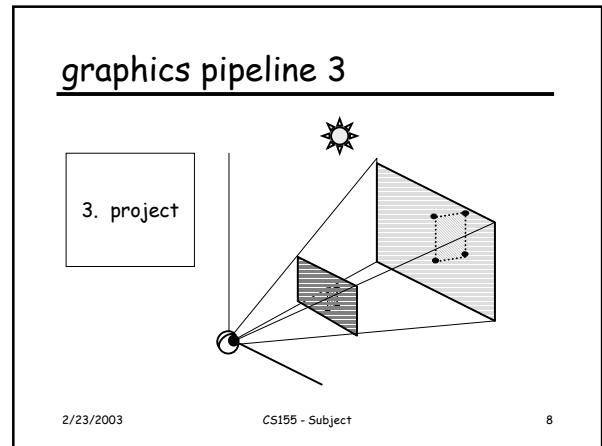
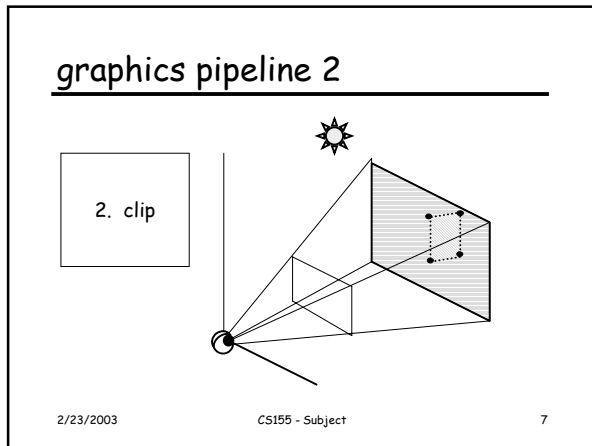
```

    graph LR
      input[user defined scene description] --> 1[1. Build scene]
      1 --> 2[2. Clip]
      2 --> 3[3. Project]
      3 --> 4[4. Scan convert]
  
```

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graphics pipeline 1

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build scene

pipeline representation is in homogeneous coordinates

$v_0 = (0,0,0,1)$, $v_1 = (1,0,0,1)$, $v_2 = (1,1,0,1)$, $v_3 = (0,1,0,1)$

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primitives

- points
- line segments
- polygons

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build scene

User described modeling transforms
World coordinates

Vertex in world coordinates: M_{WV}

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modeling transforms

- scale
- rotate
- translate

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build scene

User described lights
World coordinates

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Lights

- Ambient
- Directional
- Point
- Spot

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build scene

User defined viewpoint
View coordinates

vertex in view coordinates:
 $M_v M_w v$

lights in view coordinates:
 $M_l p, M_l d$

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view in world coordinates

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world ↔ view coordinates

translate & rotate: $M_v = M_R M_T$

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world ↔ view coordinates

M_T : translate by $(-p_x, -p_y, -p_z)$

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world ↔ view coordinates

rotation

$M_R r = (1, 0, 0)^T$
 $M_R u = (0, 1, 0)^T$
 $M_R t = (0, 0, -1)^T$

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world ↔ view coordinates

rotation

$r = M_R^{-1}(1, 0, 0)^T$
 $u = M_R^{-1}(0, 1, 0)^T$
 $t = M_R^{-1}(0, 0, -1)^T$

$$M_R^{-1} = \begin{bmatrix} r_x & u_x & -t_x \\ r_y & u_y & -t_y \\ r_z & u_z & -t_z \end{bmatrix}$$

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build scene

vertex in view coordinates: $M_v M_w v$

lights in view coordinates: $M_v p, M_v d$

viewpoint

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geometric primitives

object coordinates: v description of vertex

world coordinates: $M_w v$ description of vertex situated in world

view coordinates: $M_v M_w v$ description of vertex in world as seen from a particular viewpoint

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lights

world coordinates: p, d description of light position/direction in world

view coordinates: $M_v p, M_v d$ description of light position/direction in world as seen from a particular viewpoint

note: $M_v d$ is shorthand for the "multiply vector" operation we've used before!

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graphics pipeline

Done

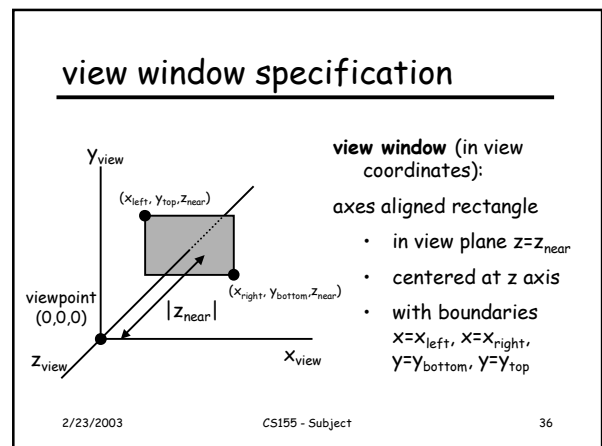
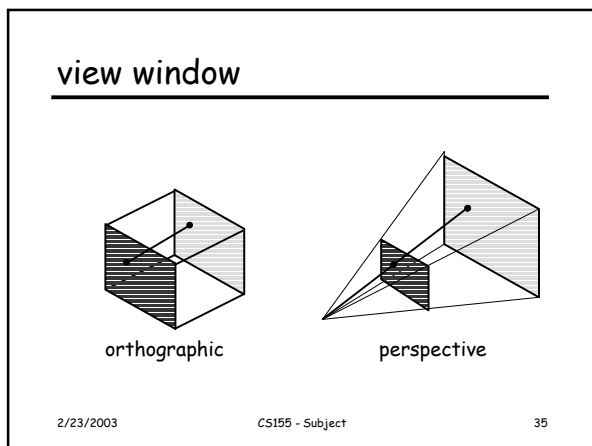
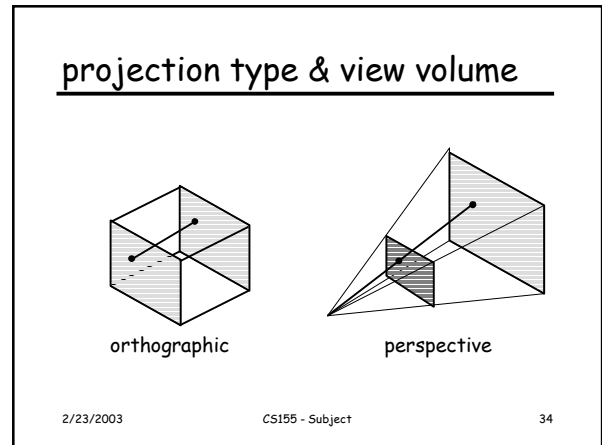
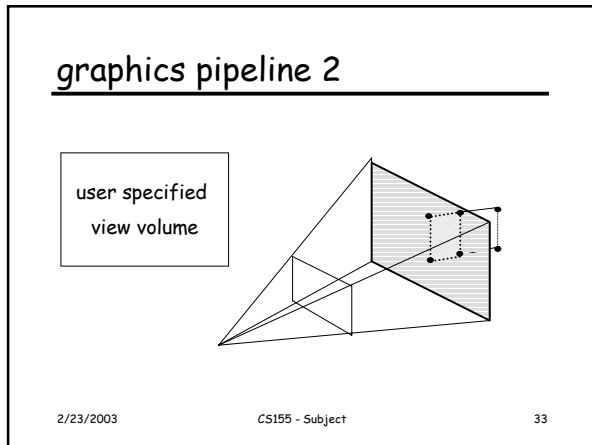
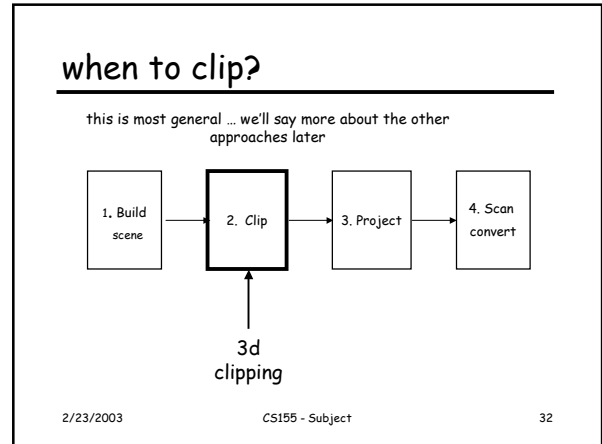
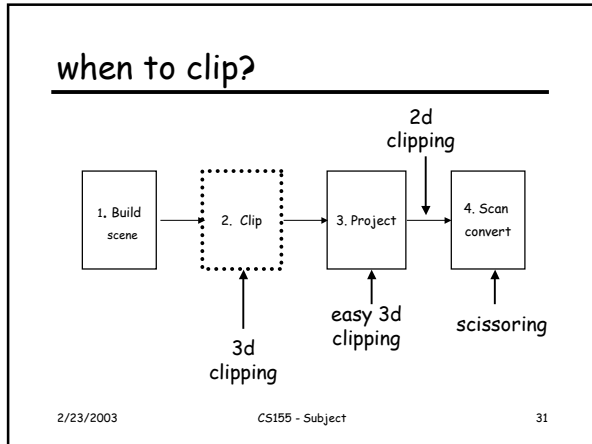
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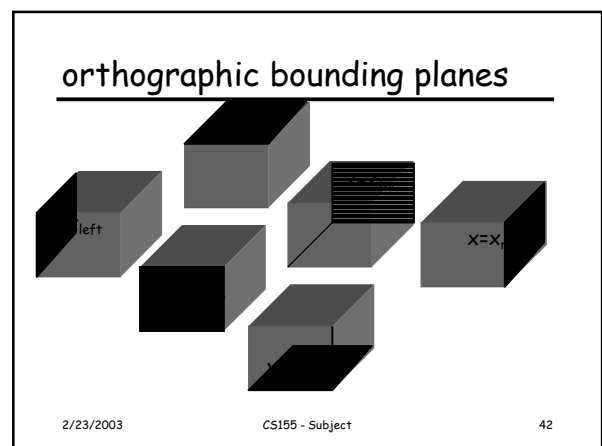
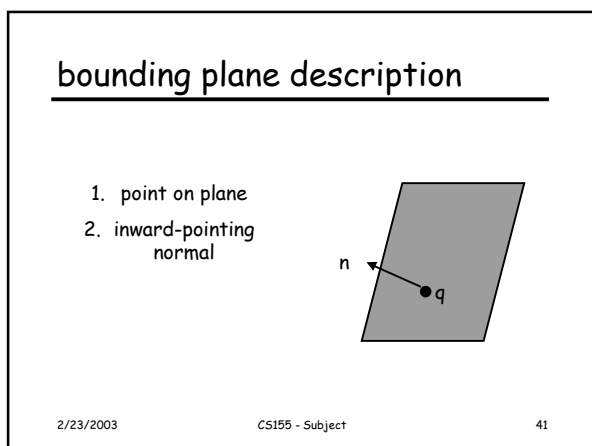
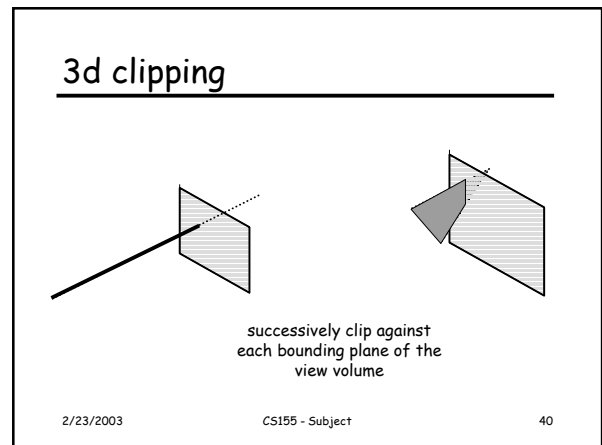
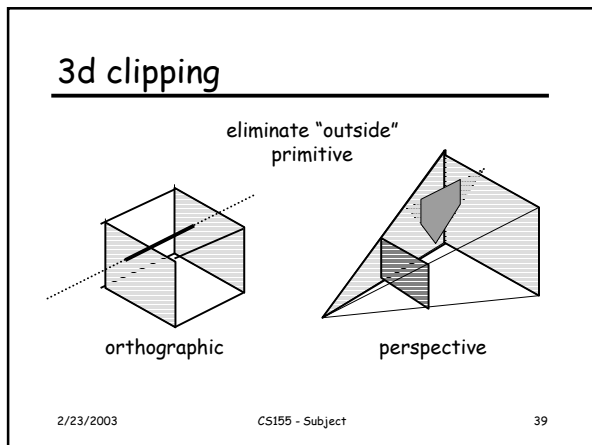
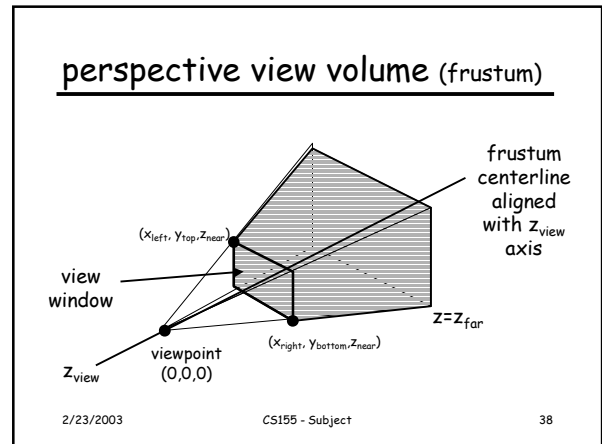
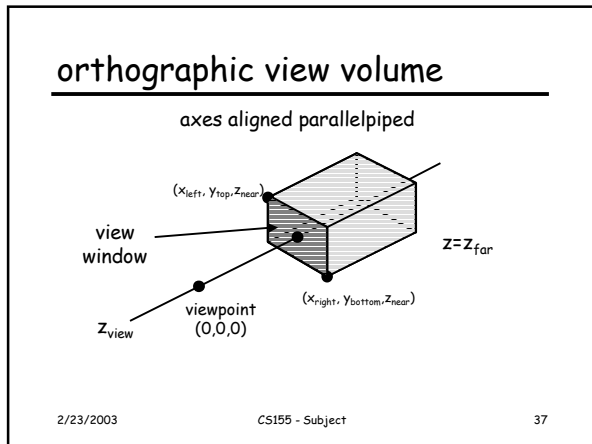
graphics pipeline

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graphics pipeline 2

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point on plane

$(x_{left}, y_{top}, z_{near})$

left

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inward-pointing normal

out-space

in-space

left

inward pointing normal $n: \langle 1, 0, 0 \rangle$

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perspective bounding planes

$Z=Z_{near}$

$Z=Z_{far}$

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perspective bounding planes

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view volume bounding plane

plane containing

$(0, 0, 0)$,
 $(x_{left}, y_{bottom}, z_{near})$,
 $(x_{left}, y_{top}, z_{near})$

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inward-pointing normals

plane containing

$(0, 0, 0)$,
 $(x_{left}, y_{bottom}, z_{near})$,
 $(x_{left}, y_{top}, z_{near})$

with inward pointing normal $n = w \times v$

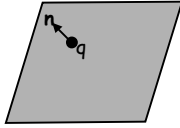
out-side

in-side

$n = w \times v$

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clipping plane



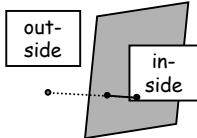
clipping plane specification:

- point q on the plane
- inward pointing normal n

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3d clipping

given a clipping plane and a graphics primitive
return "in-side primitive"



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3d clipping

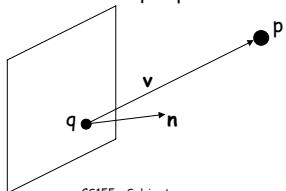
- vertex clipping
- line segment clipping
- polygon clipping

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vertex clipping

p is in with respect to the clipping plane iff $n \cdot v \geq 0$ where

- n is the inward facing normal
- v is the vector from q to p



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3d clipping

- vertex clipping
- **line segment clipping**
- polygon clipping

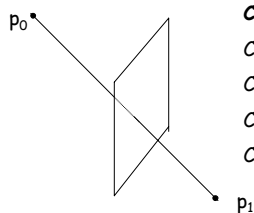
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line segment clipping

use test for vertex clipping

Classify endpoint p_0 & p_1

- Case: p_0 & p_1 in _____
- Case: p_0 & p_1 out _____
- Case: p_0 in & p_1 out _____
- Case: p_0 out & p_1 in _____



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line segment clipping

Case p_0 & p_1 in:
return (p_0, p_1)

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line segment clipping

Case p_0 & p_1 out:
return null

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line segment clipping

Case p_0 in & p_1 out:
return (p_0, p')

Case: p_0 out & p_1 in:
return (p', p_1)

do you know how to compute p' ?

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line segment clipping

color at p' :
interpolate

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out-code optimization

eliminate unnecessary intersection computations

IN

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out-code optimization

111100 plane 0

101110 plane 1

IN

endpoint p has out-code $b_0b_1\dots b_5$:

- $b_i=0$ if p is inside plane i
- $b_i=1$ else

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out-code optimization

- compute endpoint out-codes B and B'
- if B AND B' ≠ 0 return _____
- if B OR B' = 1 return _____
- else clip against plane j where the ith _____
- restart test

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3d clipping

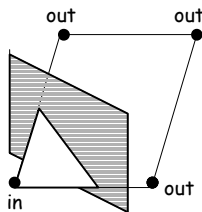
- vertex clipping
- line clipping
- **polygon clipping**

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polygon clipping



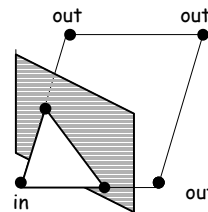
1. classify vertices

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polygon clipping



1. classify vertices
2. compute intersection points of intersecting edges
&
write out new polygon

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polygon clipping

- if v_0 is in then write v_0
- for $i=1..n-1$
 - case v_i & v_{i+1} in: write v_{i+1}
 - case v_i & v_{i+1} out: do nothing
 - case v_i in and v_{i+1} out: write intersection point
 - case v_i out and v_{i+1} in: write intersection point and v_{i+1}

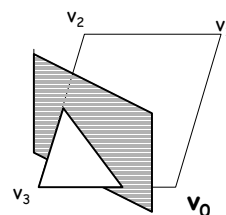
indices taken modulo n

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example



v_0 out: do nothing

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example

v_0 & v_1 out: do nothing

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example

v_1 & v_2 out: do nothing

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example

v_2 out & v_3 in:
write v , v_3

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example

v_3 in & v_0 out:
write v'

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polygon clipping

- if v_0 is in then write v_0
- for $i=1..n-1$
 - case v_i & v_{i+1} in: write v_{i+1}
 - case v_i & v_{i+1} out: do nothing
 - case v_i in and v_{i+1} out: write intersection point
 - case v_i out and v_{i+1} in: write intersection point and v_{i+1}

interpolate along edge to find color at intersection point

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graphics pipeline

1. Build scene → 2. Clip → 3. Project → 4. Scan convert

Done

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