cs155 – z sweedyk

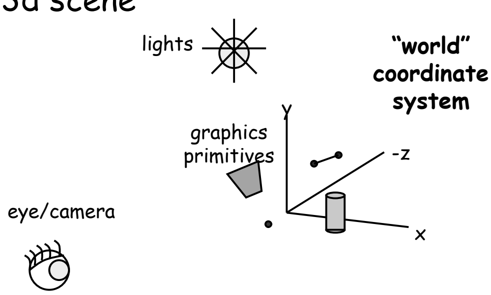
3D graphics

scene graphs

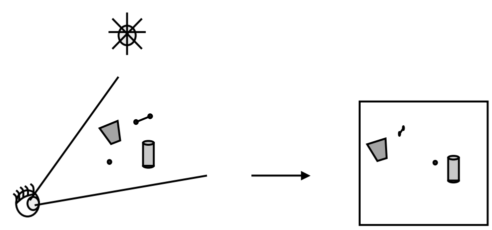
overview

- brief overview of 3D
- modeling transforms & homogenous coordinates
- hierarchical coordinates

3d scene



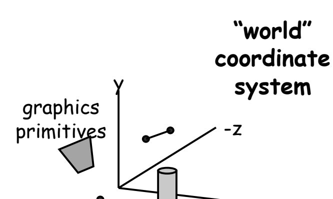
rendering



overview

- brief overview of 3D DONE
- modeling transforms & homogenous coordinates
- hierarchical coordinates

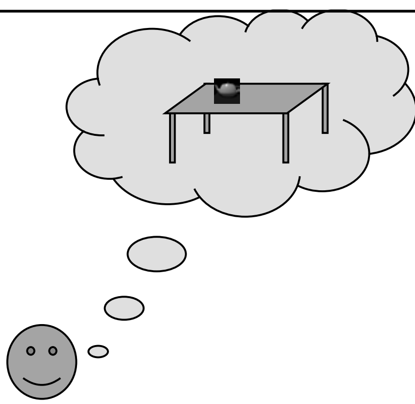
today: composing the scene



geometric primitives

- points
- lines
- triangles
- spheres

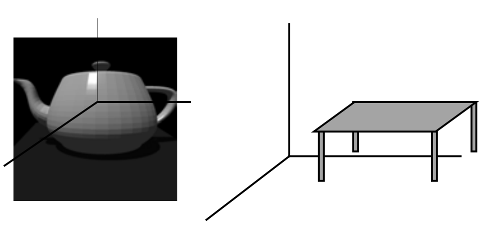
triangle mesh



3d model store

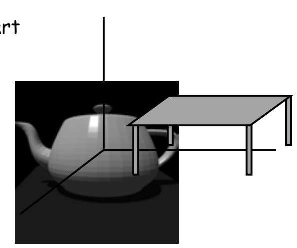
receipt
one triangle mesh teapot
one triangle mesh table

putting it together



putting it together

call Martha Stewart



making it fit

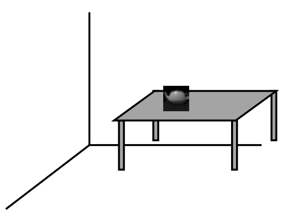
transform teapot
- scale by .1
- translate by (20,10,2)

making it fit

for each triangle in the teapot
- scale by .1
- translate by (20,10,2)

will this work?

scale and translate teapot triangles ...



now rotate it a little

transforms

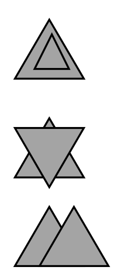
- scale
- rotate
- translate

triangle

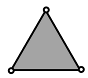
scale

rotate

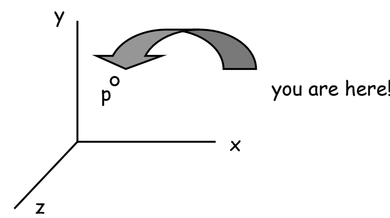
translate



triangle

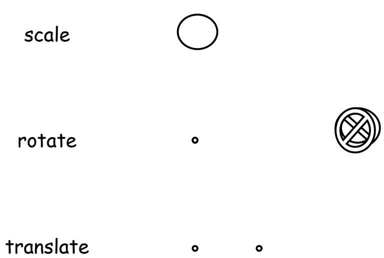


points



point

call prof gu



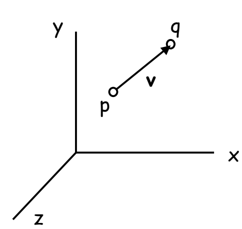
linear algebra

- scalars
- vectors

scalars: real numbers

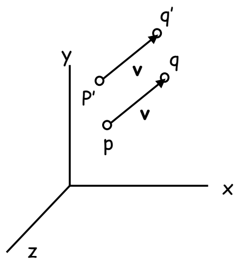
3.8
2.7
4.1
-1000.2
5

vector: magnitude & direction in (3d) space



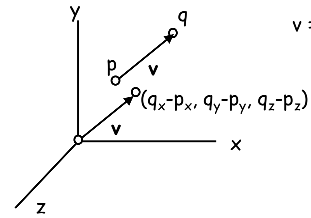
v: the way you get from p to q

vector: magnitude & direction in (3d) space



A vector does not have a position in space !

naming vectors

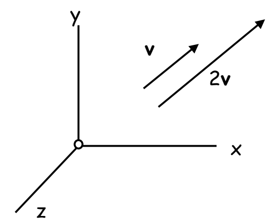


$v = \langle q_x-p_x, q_y-p_y, q_z-p_z \rangle$

linear spaces

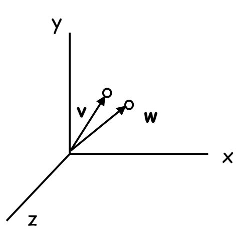
- scalars
- vectors
- scalar multiplication
- vector addition

scalar multiplication



$2v = \langle 2v_x, 2v_y, 2v_z \rangle$

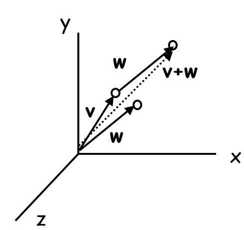
vector addition



$v = \langle v_x, v_y, v_z \rangle$

$w = \langle w_x, w_y, w_z \rangle$

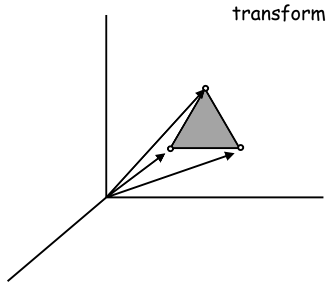
vector addition



$v+w = \langle v_x+w_x, v_y+w_y, v_z+w_z \rangle$

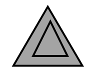
triangle

transform vectors!

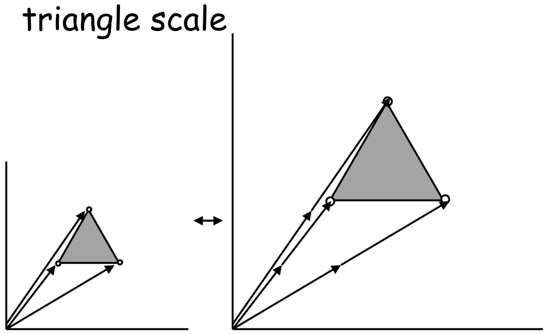


triangle

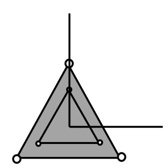
scale



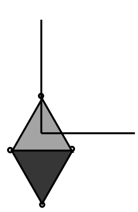
triangle scale



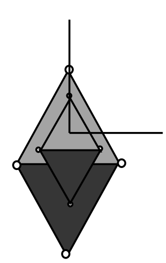
triangle scale



triangle scale



triangle scale

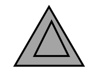


scale

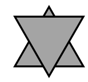
$$\begin{bmatrix} s & 0 & 0 \\ 0 & t & 0 \\ 0 & 0 & u \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} sx \\ ty \\ uz \end{bmatrix}$$

triangle

scale

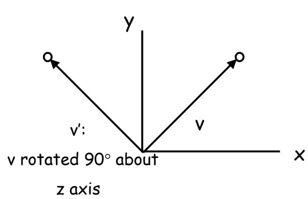


rotate



translate

rotating a vector



v'= ________________

rotation

$$\begin{bmatrix} \cos 90 & -\sin 90 & 0 \\ \sin 90 & \cos 90 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} v_x \\ v_y \\ v_z \end{bmatrix} = \begin{bmatrix} v_x \cos 90 - v_y \sin 90 \\ v_x \sin 90 + v_y \cos 90 \\ v_z \end{bmatrix}$$

rotate about z axis

$$\begin{bmatrix} \cos \phi & -\sin \phi & 0 \\ \sin \phi & \cos \phi & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

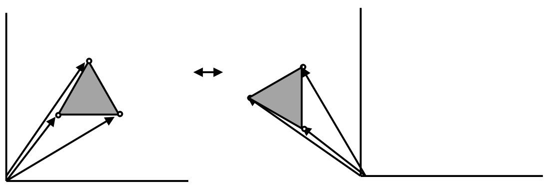
- the first column specifies what happens to (1,0,0)
- the second column specifies what happens to (0,1,0)
- the third column specifies what happens to (0,0,1)

rotation in 3D about x axis

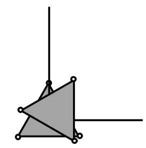
$$\begin{bmatrix} \quad & \quad & \quad \\ \quad & \quad & \quad \\ \quad & \quad & \quad \end{bmatrix}$$

fill in the blanks

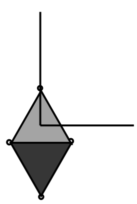
triangle rotate



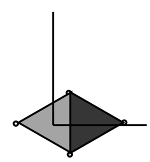
triangle rotate



triangle rotate

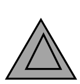


triangle rotate

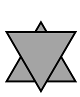


triangle

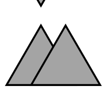
scale



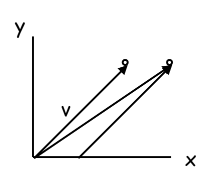
rotate



translate



translating a point



p translated 2 units to the right

$f(\langle x,y,z\rangle)=\langle x+2,y,z\rangle$

operators

- scale
- rotate

} linear

- translate — non-linear

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linear transformation

- f(**v**) is linear if
  f(α**u**+β**v**) = αf(**u**)+βf(**v**)

- translation is not a linear transform: define $T(v) = v+w_0$ where w_0 is a non-zero vector
  $T(u+v) = u + v +w_0$
  $T(u)+T(v) = u+v+2w_0$

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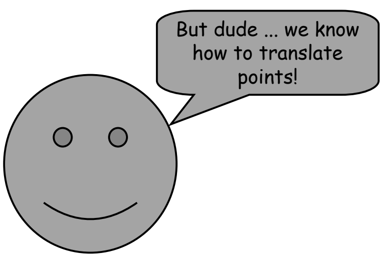

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composite transform

$M_1v \longrightarrow M_2(M_1v)$

$\Updownarrow$

$(M_2M_1)v$

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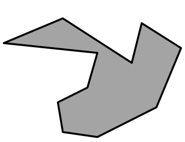
transform polygon mesh



1,000,000 vertices

10 transforms

→ 10,000,000 computations

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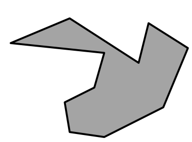
transform polygon mesh



1,000,000 vertices

~~10 transforms~~

1 composite transform

→ 1,000,000

~~10,000,000~~ computations

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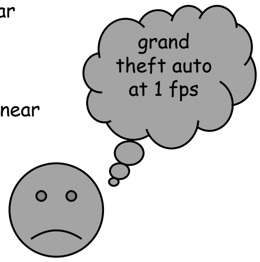
operators

- scale
- rotate

} linear

- translate non-linear

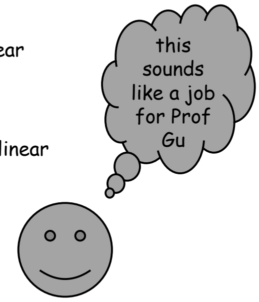


operators

- scale
- rotate

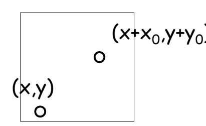
} linear

- translate non-linear

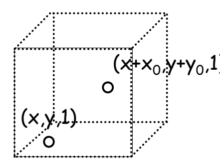


let's step back into 2D for a moment

hold onto your hat ...



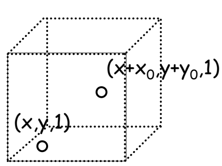
not a 2D linear xfm



3D linear xfm

linear transform

$$\begin{bmatrix} 1 & 0 & x_0 \\ 0 & 1 & y_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x+x_0 \\ y+y_0 \\ 1 \end{bmatrix}$$



NOTE: this only works as a translate for points in the plane z=1!

2D homogenous coordinates

$(x,y) \Leftrightarrow (x,y,1)$

Can we do scale and rotate in homogenous coordinates?

scale

$$\begin{pmatrix} s & 0 & 0 \\ 0 & t & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} = \begin{pmatrix} sx \\ ty \\ 1 \end{pmatrix}$$

rotate

$$\begin{pmatrix} \cos\phi & -\sin\phi & 0 \\ \sin\phi & \cos\phi & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} = \begin{pmatrix} x\cos\phi - y\sin\phi \\ x\sin\phi + y\cos\phi \\ 1 \end{pmatrix}$$

translate

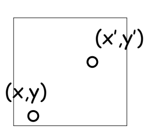
$$\begin{pmatrix} 1 & 0 & x_0 \\ 0 & 1 & y_0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} = \begin{pmatrix} x+x_0 \\ y+y_0 \\ 1 \end{pmatrix}$$

transform form

$$\begin{pmatrix} ? & ? & ? \\ ? & ? & ? \\ \hline 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} = \begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix}$$

we are not alone…

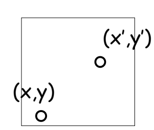
the parallel universe view of homogenous coordinates



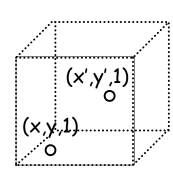
we live in this universe

we are not alone…

the parallel universe view of homogenous coordinates



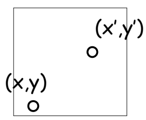
we live in this universe



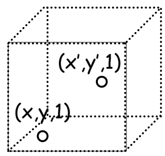
it's not the only one, but it is the only one we can experience!

and its better not to think about it …

the parallel universe view of homogenous coordinates

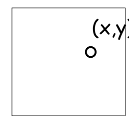


our universe has center (0,0)

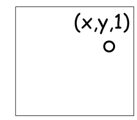


center?

2d and 2d homogenous

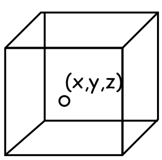


our universe

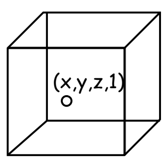


our universe when it comes to computing modeling transforms

3d and 3d homogenous



our universe



our universe when it comes to computing modeling transforms

scale

$$\begin{pmatrix} s & 0 & 0 & 0 \\ 0 & t & 0 & 0 \\ 0 & 0 & u & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} = \begin{pmatrix} sx \\ ty \\ uz \\ 1 \end{pmatrix}$$

rotate about z axis

$$\begin{pmatrix} \cos\phi & -\sin\phi & 0 & 0 \\ \sin\phi & \cos\phi & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} = \begin{pmatrix} x\cos\phi - y\sin\phi \\ x\sin\phi + y\cos\phi \\ z \\ 1 \end{pmatrix}$$

rotate about x & y axes are similar

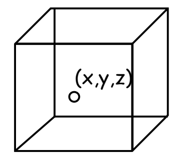
translate

$$\begin{pmatrix} 1 & 0 & 0 & x_0 \\ 0 & 1 & 0 & y_0 \\ 0 & 0 & 1 & z_0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} = \begin{pmatrix} x+x_0 \\ y+y_0 \\ z+z_0 \\ 1 \end{pmatrix}$$

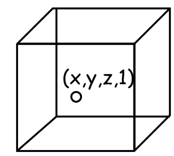
transform form

$$\begin{pmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ \boxed{0 \;\; 0 \;\; 0 \;\; 1} \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} = \begin{pmatrix} x' \\ y' \\ z' \\ 1 \end{pmatrix}$$

3d and 3d homogenous



our universe



our universe when it comes to computing modeling transforms

Composing transforms

$$M_1 M_2 v \neq M_2 M_1 v$$

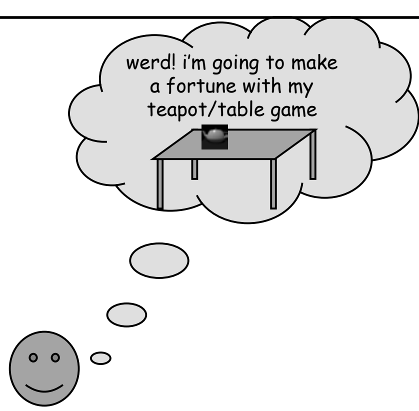
v is transformed by M_2 and then M_1

v is transformed by M_1 and then M_2

last matrix is first applied!

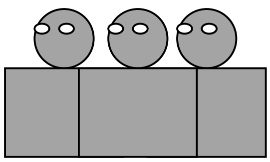
overview

- brief overview of 3D
- modeling transforms & homogenous coordinates DONE
- hierarchical coordinates

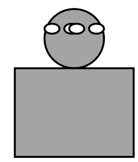


cool action figure

cool action figure



cool action figure

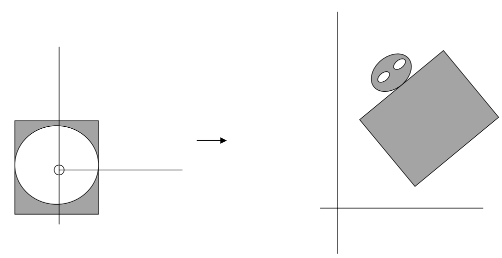


3D model store

receipt	
one orange cube	← body
one orange sphere	← head
two white sphere	← eyes

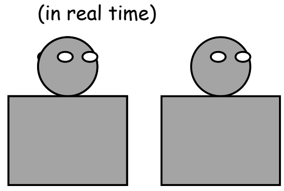
cube has side length one and is centered at the origin
spheres have radius one and are centered at the origin

transformations

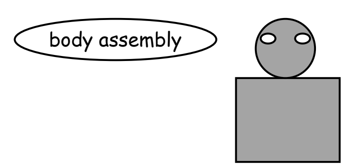


problem

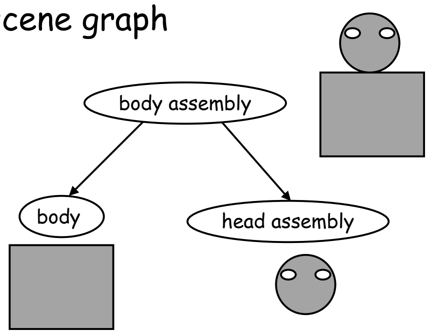
transform components as independently and as one
(in real time)



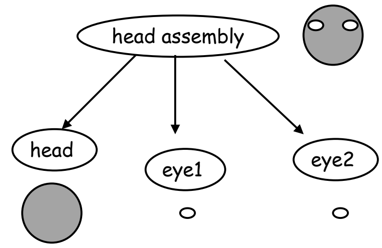
scene graph



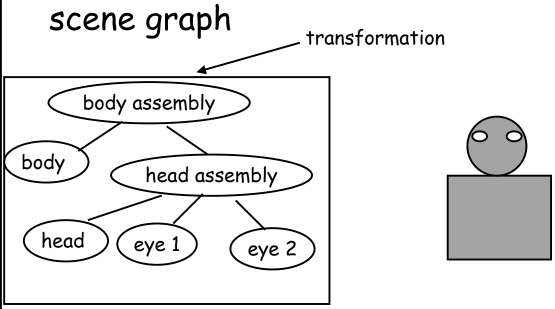
scene graph



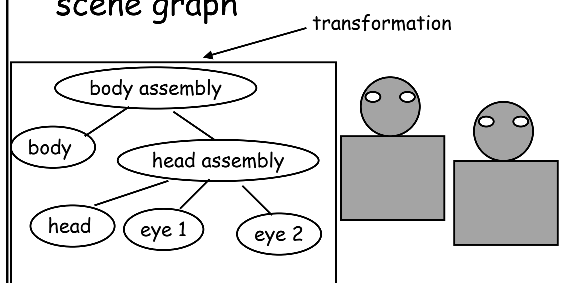
scene graph



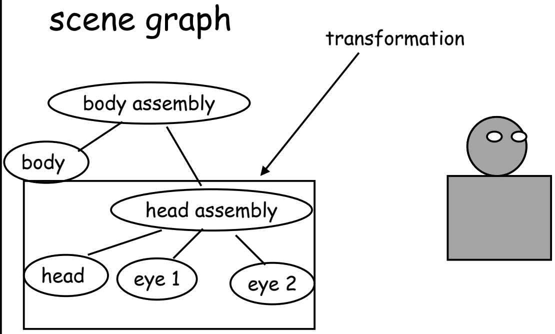
scene graph



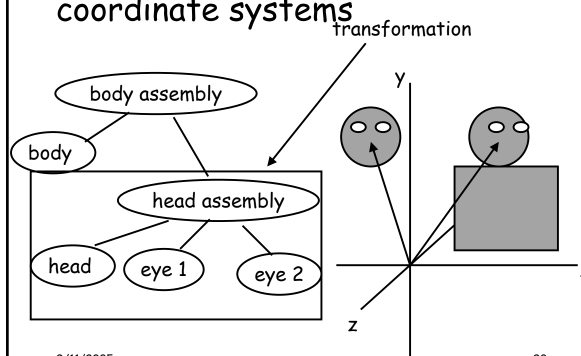
scene graph



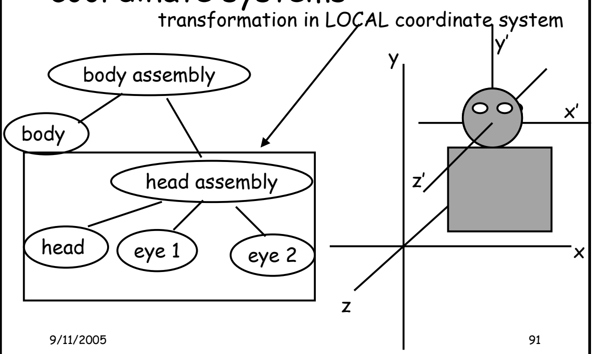
scene graph



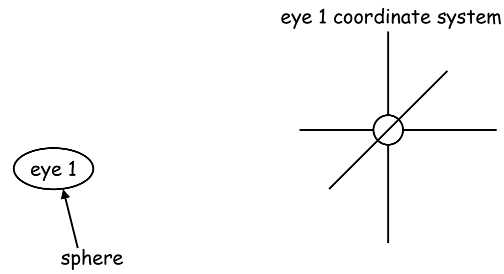
coordinate systems



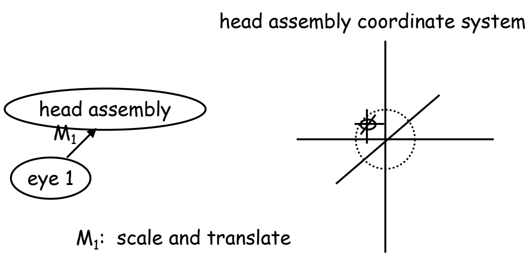
coordinate systems



hierarchical coordinates

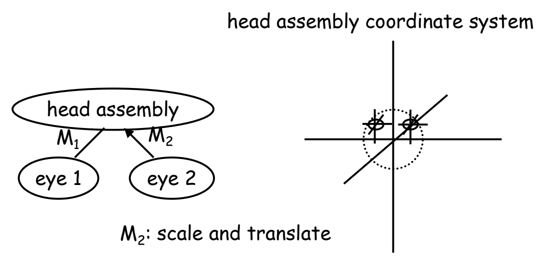


hierarchical coordinates



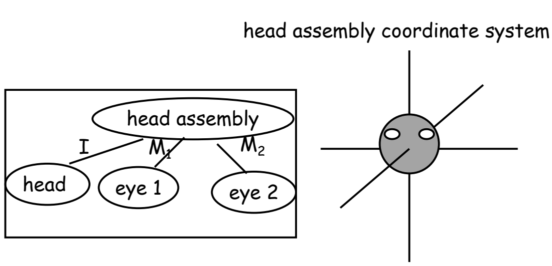
M_1: scale and translate

hierarchical coordinates

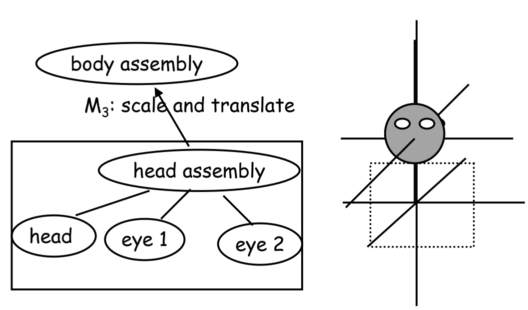


M_2: scale and translate

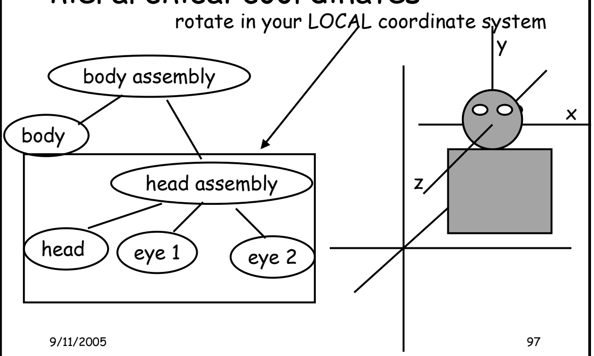
hierarchical coordinates



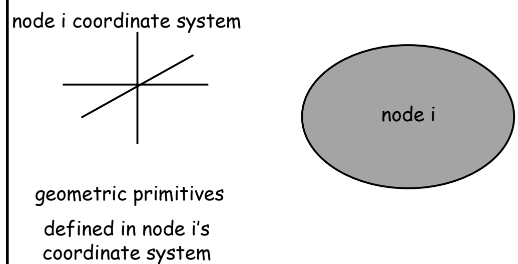
hierarchical coordinates



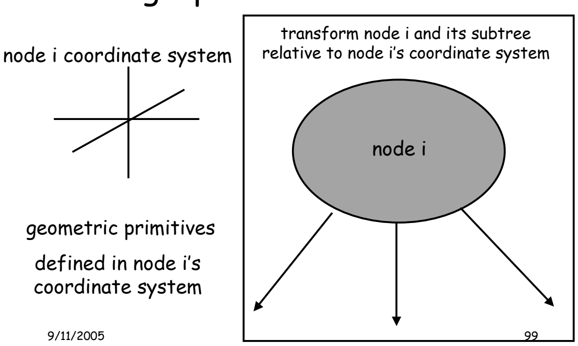
hierarchical coordinates



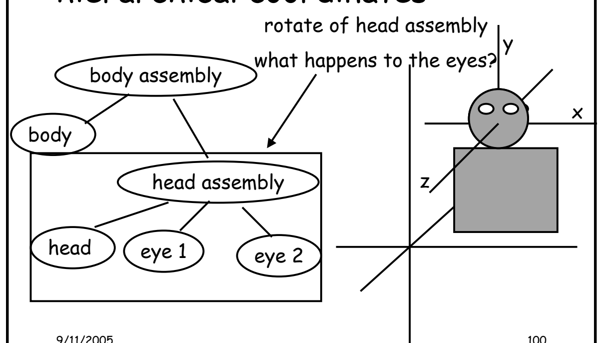
scene graph node

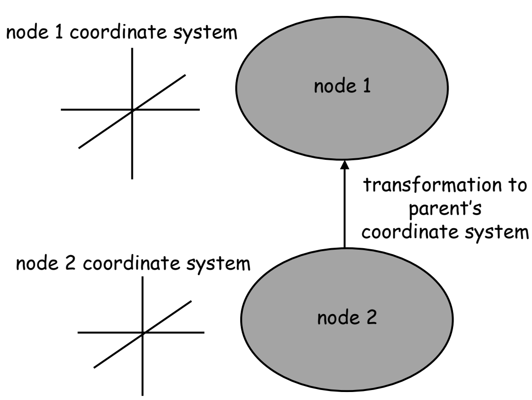


scene graph node



hierarchical coordinates





hierarchical coordinates

// Left eye

- Transform to head assembly coordinate system:
  - translate(-1,1,0) M_1
  - scale(0.2,0.2,0.2) M_2
- Sphere (radius 1, centered at origin)

hierarchical coordinates

// Right eye

- Transform to head assembly coordinate system:
  - translate(1,1,0) M_4
  - scale(0.2,0.2,0.2) M_3
- Sphere (radius 1, centered at origin)

hierarchical coordinates

// Head

- Sphere (radius 1, centered at origin)

hierarchical coordinates

// Head assembly

- Transform to body assembly coordinate system
  - Translate(0,1/2,0) M_7
  - Scale(.4,.4,.4) M_6
- Local transform
  - Rotate(θ,y-axis) M_5
- Children
  - Left eye
  - Right eye
  - Head

hierarchical coordinates

// Body

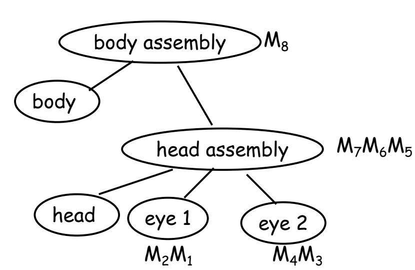
- Cube

hierarchical coordinates

// Body assembly

- Local transform
  - Translate(dx,dy,dz) M_8
- Children
  - Body
  - Head assembly

hierarchical coordinates



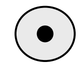
Exercise

What is the composite transform applied to left eye?

What is the composite transform applied to right eye?

Exercise

Suppose we used a texture mapped sphere for the eye:



How would we modify the scene graph so that we could roll the eyes?

Exercise: build the scene graph for a snowman that has a head, middle, bottom, two eyes, nose, and mouth.

snowman: what you can use

- spheres: radius 1, centered at origin (color options: white, black, red)
- scale (s,t,u)
- rotate (theta, vector)
- translate (dx,dy,dz)

download rt & snowman.ray
expand snowman.ray to include your scene graph!
render with rt