



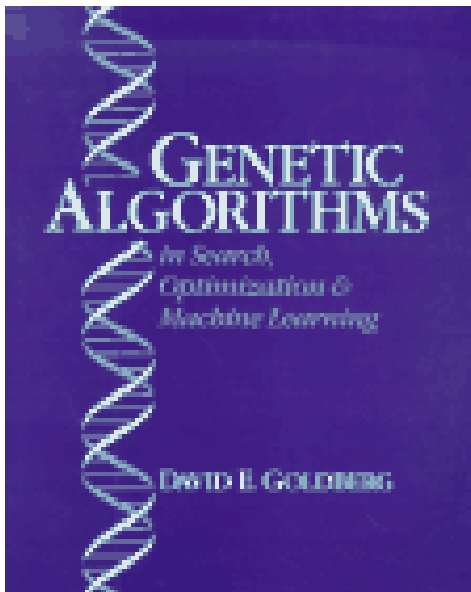
# Evolutionary Computation

Robert Keller  
Harvey Mudd College  
December 2007

# Some References

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David Goldberg

Genetic Algorithms in  
Search,  
Optimization and  
Machine Learning, 1989.



Zbigniew Michalewicz

Genetic Algorithms + Data Structures  
= Evolution Programs  
3rd edition, Springer-Verlag, 1993

# Evolutionary Computation

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- Evolutionary algorithms
- Genetic algorithms
- Genetic programming
- Artificial life (“alife”)

# Historical

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- 1966, Fogel, Owens, and Walsh,  
***Artificial Intelligence through Simulated Evolution***, John Wiley & Sons
- Looked at derivation of
  - finite-state machines
  - controllers
  - data reductionthrough successive mutations

# Historical

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- 1975, John H. Holland  
***Adaptation in natural and artificial systems***, MIT Press
  - Focus was on natural systems, simulation
  - Introduced current genetic algorithm idea
  - Mostly theory, some applications to:
    - game-playing
    - search programs

# Among Mr. Holland's Opuses

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- "A universal computer capable of executing an arbitrary number of programs simultaneously." In Proceedings 1959 Eastern Joint Computer Conference. IEEE. pp108-13.
- See <http://www.pscs.umich.edu/jhhfest/jhh-pub.html> for more.

# Mr. Holland's Progeny

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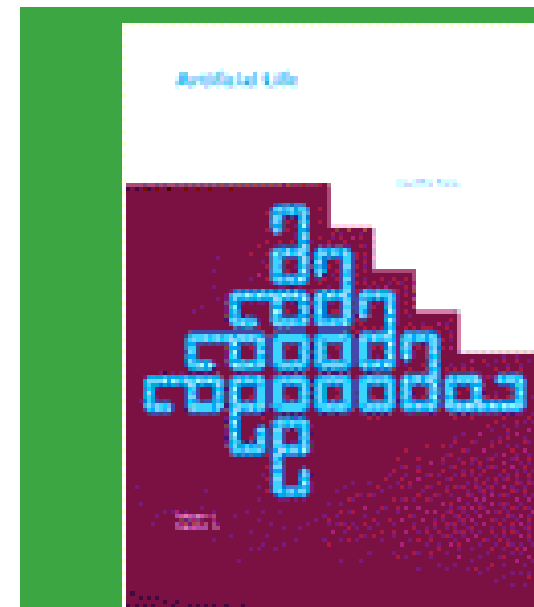
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- David Goldberg
- Stephanie Forrest
- Kenneth DeJong
- Melanie Mitchell
- John Koza
- many others
- See <http://www.pscs.umich.edu/jhhfest/schedule-closed.html> for Festschrift papers.

# Today



 The MIT Press



 IEEE TRANSACTIONS ON  IEEE TRANSACTIONS ON  
**NEURAL NETWORKS** **FUZZY SYSTEMS**

 IEEE TRANSACTIONS ON  
**EVOLUTIONARY  
COMPUTATION**

# Genetic Algorithms

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- An approach to difficult optimization problems (TSP, etc.)
- Heuristic, not guaranteed to find true optima
- Finds good approximations fast

# GA Applications

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- Hundreds, if not thousands
- All manner of optimization problems in engineering, science, finance, etc.
- Application to neural networks:
  - *Evo/ve* the structure and/or weights of a neural network, rather than train it.

# Principles of Natural Selection

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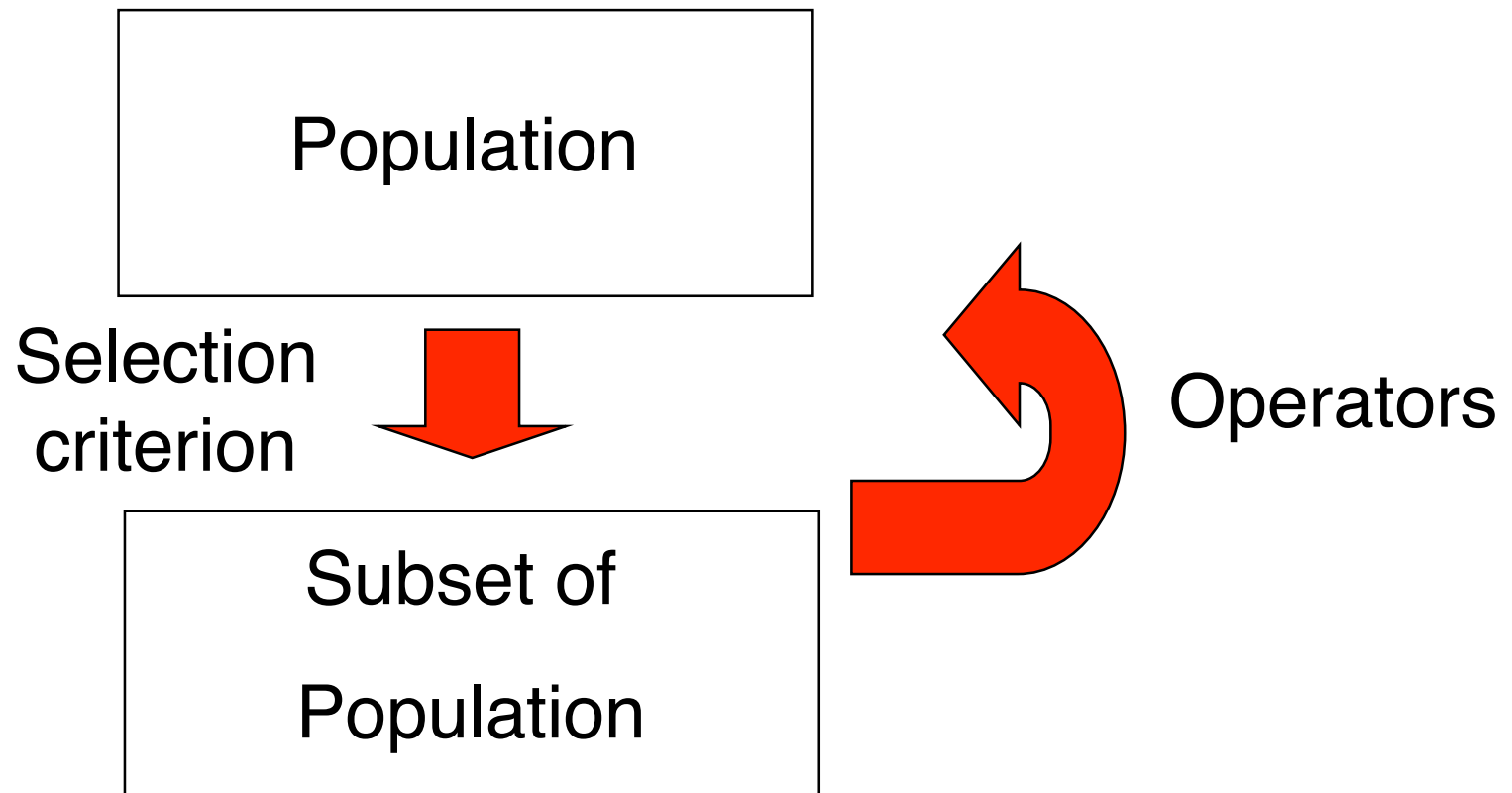
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- Concentrate on **population** rather than a *single* individual
- Individuals that are fit enough to survive will reproduce
- Create new individuals from existing ones
  - Crossover
  - Mutation

# Genetic Flow Diagram

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until an individual exists satisfying performance criterion or resources are exhausted

# Common Operators

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- **Copy** (aka Reproduce): An individual from the current generation is copied into the next generation.
- **Crossover**: Two (or more) individuals from the current generation are used to form an individual in the next generation.
- **Mutate**: A single individual from the current generation is mutated to form an individual in the next generation.

# Individuals

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- Individuals are represented by their genome, or **genotype**.
- The genotype may be the “program” for the actual individual, or **phenotype**.

# Genetic Algorithm Example

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- Consider the “subset sum” problem:
  - Given a set of integers  $S$  and a target value  $T$ , find a subset of  $S$  that the maximum sum **without exceeding**  $T$ .

# Genetic Algorithm Example

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- “subset sum” problem:
  - Given a set of integers  $S$  and a target value  $T$ , find a subset of  $S$  that the maximum sum without exceeding  $T$ .
- This is an *optimization* problem. The related *decision* problem, find whether there is a subset summing to *exactly*  $T$ , is known to be NP-complete.
- A related problem arises in cryptography.

# Genetic Approach

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- As the genome, use a bit-vector.
- There is one bit for each element in the set  $S$ .
- The bit is 1 iff the element is in the subset.

# Example

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- $S = \{19, 23, 35, 52, 61, 68, 76, 84, 92\}$
- $T = 200$
- Genome is an element of  $\{0, 1\}^9$
- Possible individuals:
  - 010001001,  $\text{sum}\{23, 68, 92\} = 183$
  - 101000010,  $\text{sum}\{19, 35, 84\} = 138$

# What can we try to produce more fit individuals?

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- **Mutation:** change a random bit:

101000010,  $\text{sum}\{19, 35, 84\} = 138$



111100010,  $\text{sum}\{19, 23, 35, 84\} = 161$

# Fatal Mutations

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- Note that a mutation could be “fatal”, resulting in a totally unfit individual. The “carcass” of this individual could still be in the next generation, however.

# What can we try to produce more fit individuals?

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- **Crossover:** Combine two individuals

001|110000,  $\text{sum}\{35, 52, 61\} = 148$   
100|000110,  $\text{sum}\{19, 76, 84\} = 179$

crossover point selected at random

- New genomes:

001000110,  $\text{sum}\{35, 76, 84\} = 195$   
100110000,  $\text{sum}\{19, 52, 61\} = 132$

← better

# Crossover Variations

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- Sometimes two crossover points are chosen, rather than one, and the subsequences between them are swapped.
- Just as with mutation, crossover could produce one or more individuals that are totally unfit.

# Sample GA Program

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- The program  
`/cs/cs152/ga/subsum/subsum.java`  
carries out the genetic algorithm on this  
problem.
- Examples:
  - `go ss1.in`
  - `go ss2.in`

# Main Loop of the Subset Sum GA Program (1)

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---

```
public void evolve(int generations)
{
  for( generation = 0; generation < generations; generation++ )
  {
    retain();           // retain the more fit individuals
    crossover();       // perform crossover on those retained
    mutate();          // mutate the resulting population
    sort();             // sort by fitness
  }
}
```

# Sample Run of subsum (1)

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Subset sum problem

generations = 100

population size = 10

retain size = 5

immutable = 5

mutation rate = 0.1

target = 200.0

values = (19 23 35 52 61 68 76 84 92)

# Sample Run of subsum (1)

---

---

generation 0, average fitness = 33.7:

181/200	(r 19)	000111000	52	61	68	} only two fit individuals		
164/200	(r 36)	100010010	19	61	84			
-1/200	(r 201)	000011110	61	68	76	84		
-1/200	(r 201)	010111000	23	52	61	68		
-1/200	(r 201)	000010110	61	76	84			
-1/200	(r 201)	000111100	52	61	68	76		
-1/200	(r 201)	101101101	19	35	52	68	76	92
-1/200	(r 201)	000011110	61	68	76	84		
-1/200	(r 201)	101101101	19	35	52	68	76	92
-1/200	(r 201)	001100101	35	52	76	92		

# Sample Run of subsum (2)

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generation 1, average fitness = 64.4:

181/200	(r 19)	000111000	52	61	68		
164/200	(r 36)	100010010	19	61	84		
160/200	(r 40)	000000110	76	84			
145/200	(r 55)	000010010	61	84			
-1/200	(r 201)	001100101	35	52	76	92	
-1/200	(r 201)	000011110	61	68	76	84	
-1/200	(r 201)	010111000	23	52	61	68	
-1/200	(r 201)	000011110	61	68	76	84	
-1/200	(r 201)	100011110	19	61	68	76	84
-1/200	(r 201)	000010110	61	76	84		

four fit  
individuals

# Sample Run of subsum (3)

generation 2, average fitness = 114.3:

197/200	(r 3)	000110010	52	61	84	
181/200	(r 19)	000111000	52	61	68	
164/200	(r 36)	100010010	19	61	84	
160/200	(r 40)	000000110	76	84		
148/200	(r 52)	100011000	19	61	68	
145/200	(r 55)	000010010	61	84		
96/200	(r 104)	001010000	35	61		
54/200	(r 146)	101000000	19	35		
-1/200	(r 201)	000110011	52	61	84	92
-1/200	(r 201)	001100101	35	52	76	92

eight fit  
individuals

# Sample Run of subsum (4)

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generation 5, average fitness = 157.7:

200/200 (r 0) 100111000 19 52 61 68

197/200 (r 3) 000110010 52 61 84

197/200 (r 3) 000110010 52 61 84

181/200 (r 19) 000111000 52 61 68

181/200 (r 19) 000111000 52 61 68

179/200 (r 21) 001100001 35 52 92

164/200 (r 36) 100010010 19 61 84

164/200 (r 36) 100010010 19 61 84

115/200 (r 85) 101010000 19 35 61

-1/200 (r 201) 000111010 52 61 68 84

best possible fit reached in generation 5



perfect individual

# Complexity Considerations

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- All possible subsets of  $n$  values can be **enumerated** in  $2^n$  steps.
- For low  $n$  (say in the 20's or less), this might be feasible.
- For larger  $n$ , it is not ( $2^{32} =$  about 5 billion).
- For large  $n$ , the genetic algorithm can produce good, if not optimal, answers in much less time than enumeration.

# Other Genomes

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- A bit vectors is not the only way, or necessarily the best way, to represent a genome.
- Other possibilities:
  - A list or matrix of integers or floats

# Challenges in representing Genomes: Traveling Salesperson Problem

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- Not every optimization problem has a genome encoding that will allow naïve mutations and crossovers.
- Consider the TSP:
  - An instinctive way to represent a genome is as a **permutation** of the cities on a tour.

# Crossing two Permutations

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- $[1, 3, 2, 6, 5, 4]$   
 $[2, 3, 4, 1, 6, 5]$

crossover points selected at random

- Result of naïve crossing:  
 $[1, 3, 4, 1, 6, 5]$   
 $[2, 3, 2, 6, 5, 4]$
- Unfortunately, these sequences are **not** permutations.

# Reinterpreting permutation crossings

- $[1, 3, | 2, 6, 5, | 4]$   
 $[2, 3, | 4, 1, 6, | 5]$

**crossover points selected at random**

- Interpret as:
  - Insert 2,6,5 in the second genome at the first crossover point and remove those elements from wherever they occurred in the second genome.

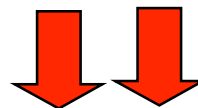
# Reinterpreting permutation crossings

- $[1, 3, 2, 6, 5, 4]$   
 $[2, 3, 4, 1, 6, 5]$

crossover points selected at random

- $[1, 3, 2, 6, 5, 4]$

$[2, 3, 4, 1, 6, 5]$



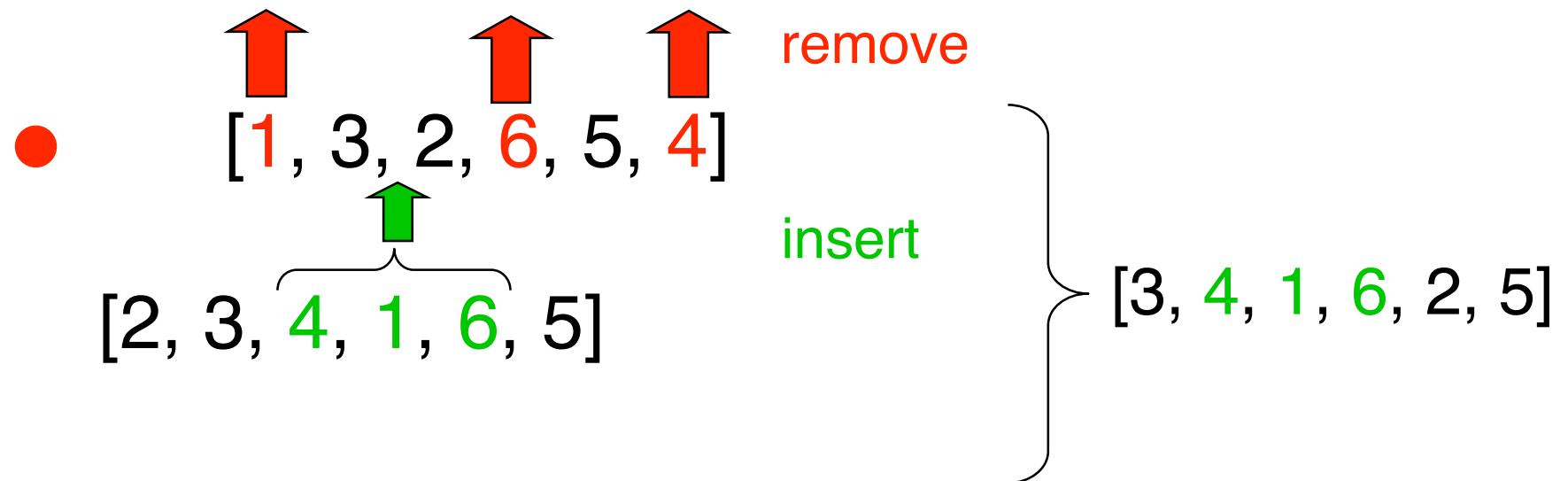
insert

remove

$[3, 2, 6, 5, 4, 1]$

# Similarly, to produce the second new genome

- $[1, 3, 2, 6, 5, 4]$   
 $[2, 3, 4, 1, 6, 5]$

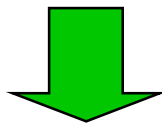


# Net effect of Crossover

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- $[1, 3, 2, 6, 5, 4]$   
 $[2, 3, 4, 1, 6, 5]$



- $[3, 4, 1, 6, 2, 5]$   
 $[3, 2, 6, 5, 4, 1]$

- The results share some of the structure of both parents, which is desirable.

# Keller's TSP GA

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- `/cs/cs152/ga/tsp`
- Uses same overall loop as the subset sum algorithm.
- The genome is now a permutation vector.
- Crossover is as described.
- Mutation consists of swapping two random elements of the permutation.

# TSP GA in operation (1)

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Traveling Salesperson Problem

generations = 1000

population size = 50

retain size = 25

immutable = 15

mutation rate = 0.1

# TSP GA in operation (2)

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Costs:

0.0	1.0	2.0	4.0	9.0	8.0	3.0	2.0	1.0	5.0	7.0	1.0	2.0	9.0	3.0
1.0	0.0	5.0	3.0	7.0	2.0	5.0	1.0	3.0	4.0	6.0	6.0	6.0	1.0	9.0
2.0	5.0	0.0	6.0	1.0	4.0	7.0	7.0	1.0	6.0	5.0	9.0	1.0	3.0	4.0
4.0	3.0	6.0	0.0	5.0	2.0	1.0	6.0	5.0	4.0	2.0	1.0	2.0	1.0	3.0
9.0	7.0	1.0	5.0	0.0	9.0	1.0	1.0	2.0	1.0	3.0	6.0	8.0	2.0	5.0
8.0	2.0	4.0	2.0	9.0	0.0	3.0	5.0	4.0	7.0	8.0	3.0	1.0	2.0	5.0
3.0	5.0	7.0	1.0	1.0	3.0	0.0	2.0	6.0	1.0	7.0	9.0	5.0	1.0	4.0
2.0	1.0	7.0	6.0	1.0	5.0	2.0	0.0	9.0	4.0	2.0	1.0	1.0	7.0	8.0
1.0	3.0	1.0	5.0	2.0	4.0	6.0	9.0	0.0	3.0	3.0	5.0	1.0	6.0	4.0
5.0	4.0	6.0	4.0	1.0	7.0	1.0	4.0	3.0	0.0	9.0	1.0	8.0	5.0	2.0
7.0	6.0	5.0	2.0	3.0	8.0	7.0	2.0	3.0	9.0	0.0	2.0	1.0	8.0	1.0
1.0	6.0	9.0	1.0	6.0	3.0	9.0	1.0	5.0	1.0	2.0	0.0	5.0	4.0	3.0
2.0	6.0	1.0	2.0	8.0	1.0	5.0	1.0	1.0	8.0	1.0	5.0	0.0	9.0	6.0
9.0	1.0	3.0	1.0	2.0	2.0	1.0	7.0	6.0	5.0	8.0	4.0	9.0	0.0	7.0
3.0	9.0	4.0	3.0	5.0	5.0	4.0	8.0	4.0	2.0	1.0	3.0	6.0	7.0	0.0

# TSP GA in operation (3)

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Improvement in generation 1: 25: 4 6 10 14 9 11 7 12 3 5 13 1 0 8 2

Improvement in generation 9: 22: 4 6 14 9 11 7 12 10 3 5 13 1 0 8 2

Improvement in generation 10: 20: 4 6 9 14 10 11 7 12 3 5 13 1 0 8 2

Improvement in generation 30: 18: 4 6 9 14 10 12 7 11 3 5 13 1 0 8 2

Improvement in generation 317: 17: 4 6 9 14 10 12 5 13 3 11 7 1 0 8 2

best after 1000 generations, 17: 4 6 9 14 10 12 5 13 3 11 7 1 0 8 2

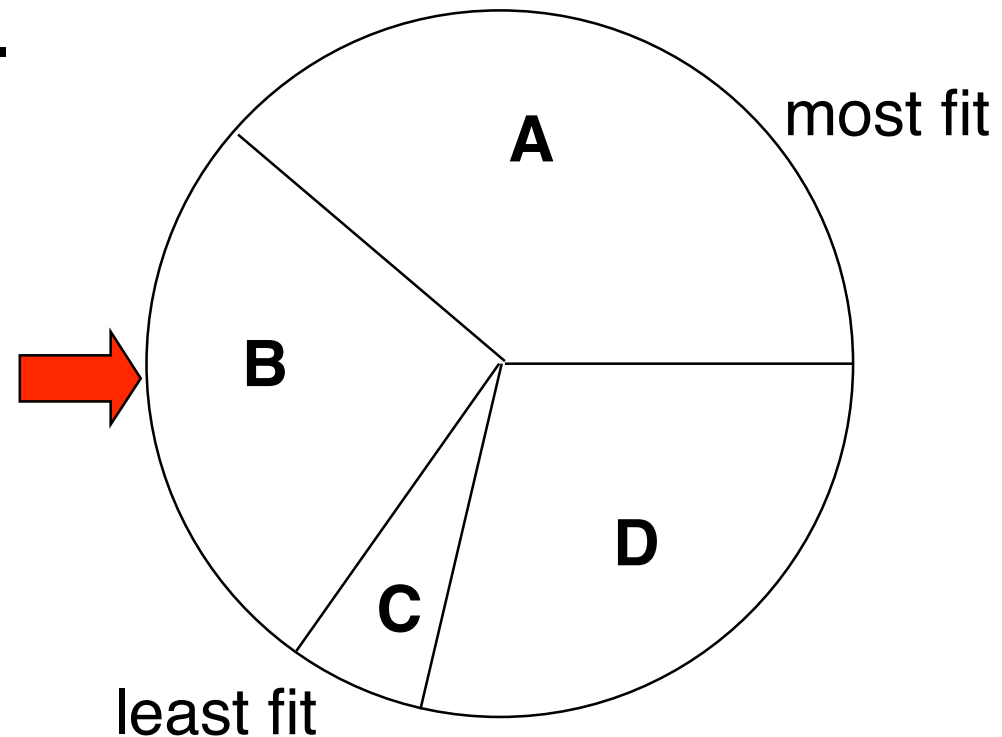
verification: 4 (1.0) 6 (1.0) 9 (2.0) 14 (1.0) 10 (1.0) 12 (1.0) 5 (2.0) 13  
(1.0) 3 (1.0) 11 (1.0) 7 (1.0) 1 (1.0) 0 (1.0) 8 (1.0) 2 (1.0) 4

# Roulette-Wheel Optimization

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- Give individuals in the population a probability of being picked in proportion to their fitness.



# GA Perspective

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- Like gradient descent, GA's can also get stuck in local fitness extrema.
- The space is different; for GA's, a stuck point corresponds to a population from which crossover does not yield any better individuals.
- Mutation is one hope for leaving such an extremum. Other possibilities are simulated annealing, random restarts.

# Evolution Options

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- Since we are simulating using a computer, not actually evolving species, there is no reason why **Lamarckian**, rather than **Darwinian**, evolution could not be used.
- Most results to date are Darwinian.
- Lamarckian could integrate other learning models to breed new species from individuals that have learned.

# Lamarckian Leads

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- Grefenstette, J. 1991. *Lamarckian learning in multi-agent environments*. In Proceedings of the Fourth International Conference of Genetic Algorithms, 303-310. Morgan Kaufmann.
- Houck, C., Joines, J., and Kay, M., Utilizing Lamarckian Evolution and the Baldwin Effect in Hybrid Genetic Algorithms, NCSU-IE TR 96-01, 1996.

# Genetic Programming

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- Genetic programming is the GA idea applied to evolving *programs* (as opposed to just numbers).
- The prime mover of this field is John R. Koza.

# Reference

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John R. Koza

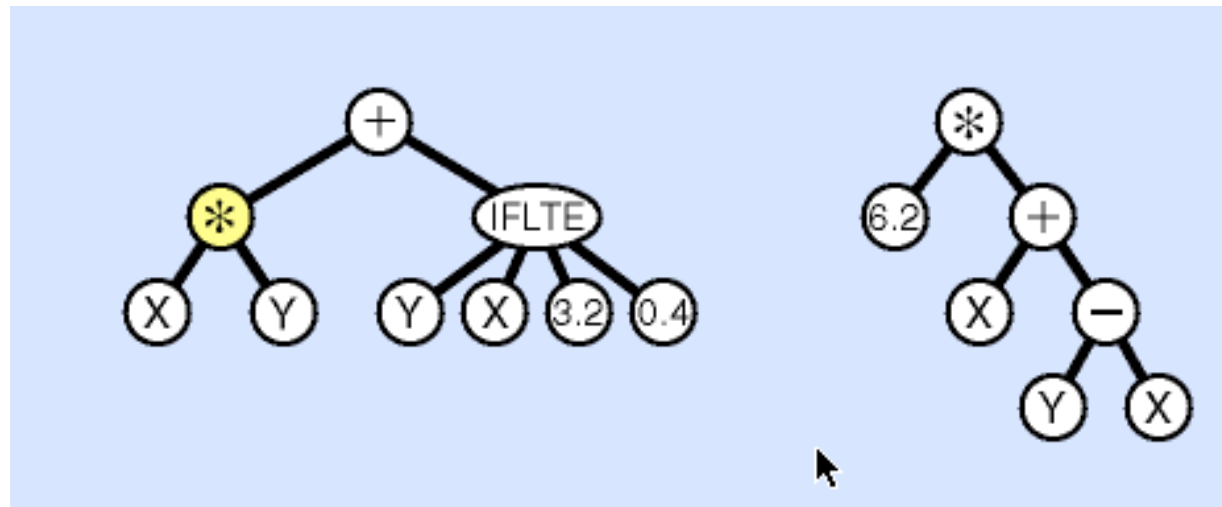
Genetic Programming :  
On the Programming of Computers  
by Means of Natural Selection

MIT Press, 1996

# Genetic Programming Genomes = Syntax Trees

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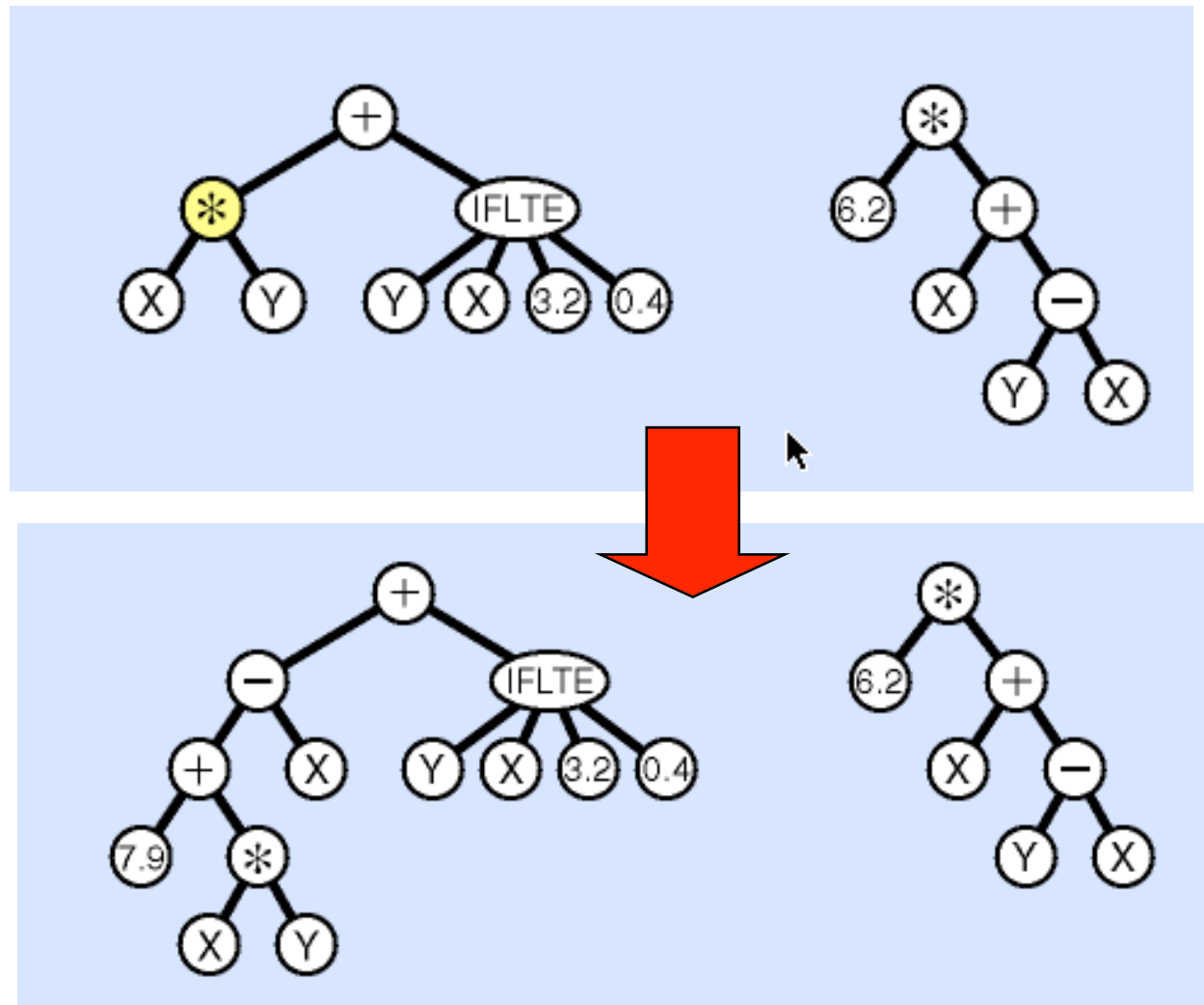
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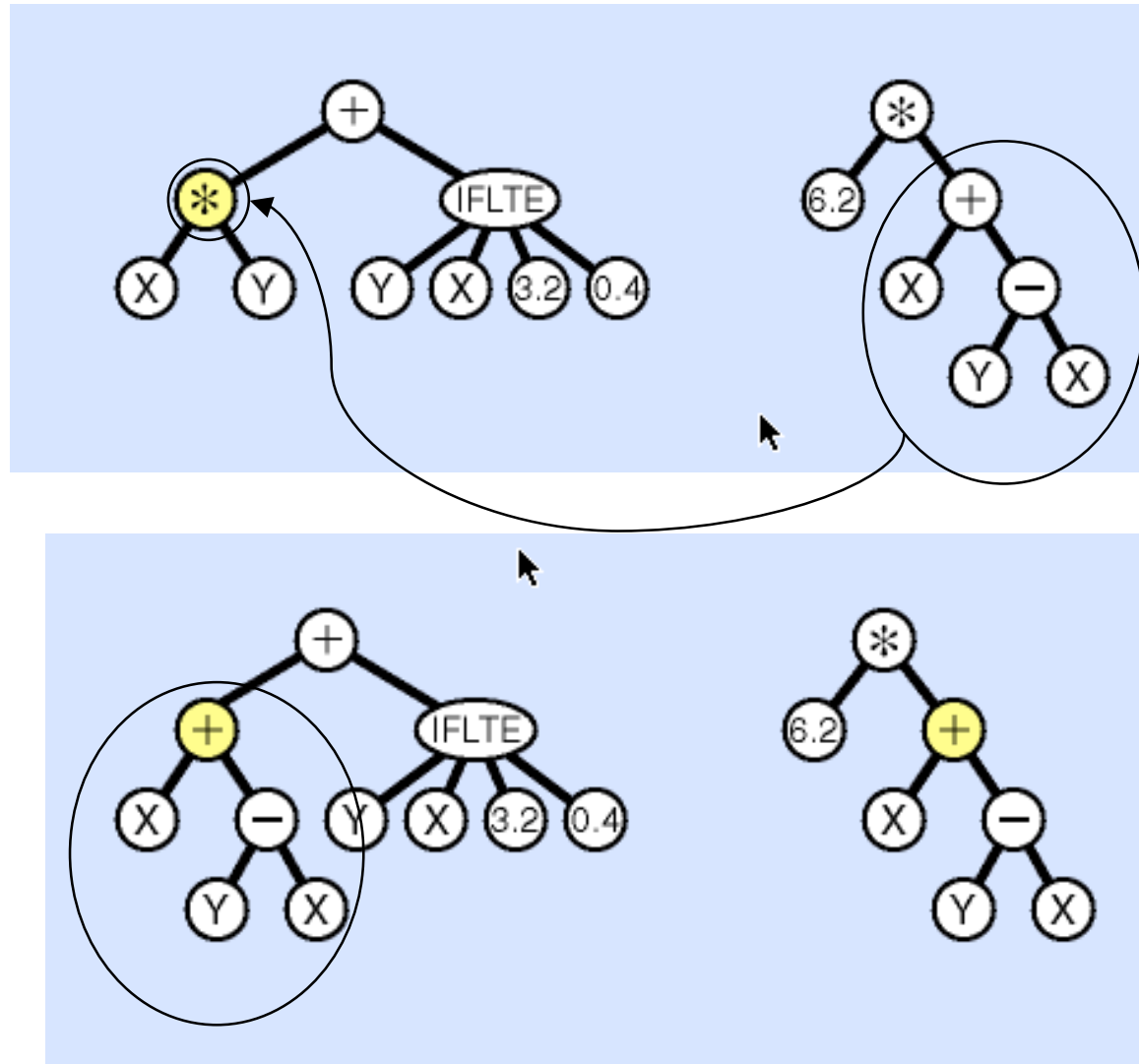
For animated tutorial, please see:

<http://www.genetic-programming.com/ganimatedtutorial.html>

# Mutation of a Program

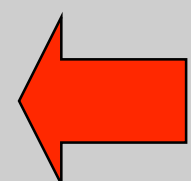
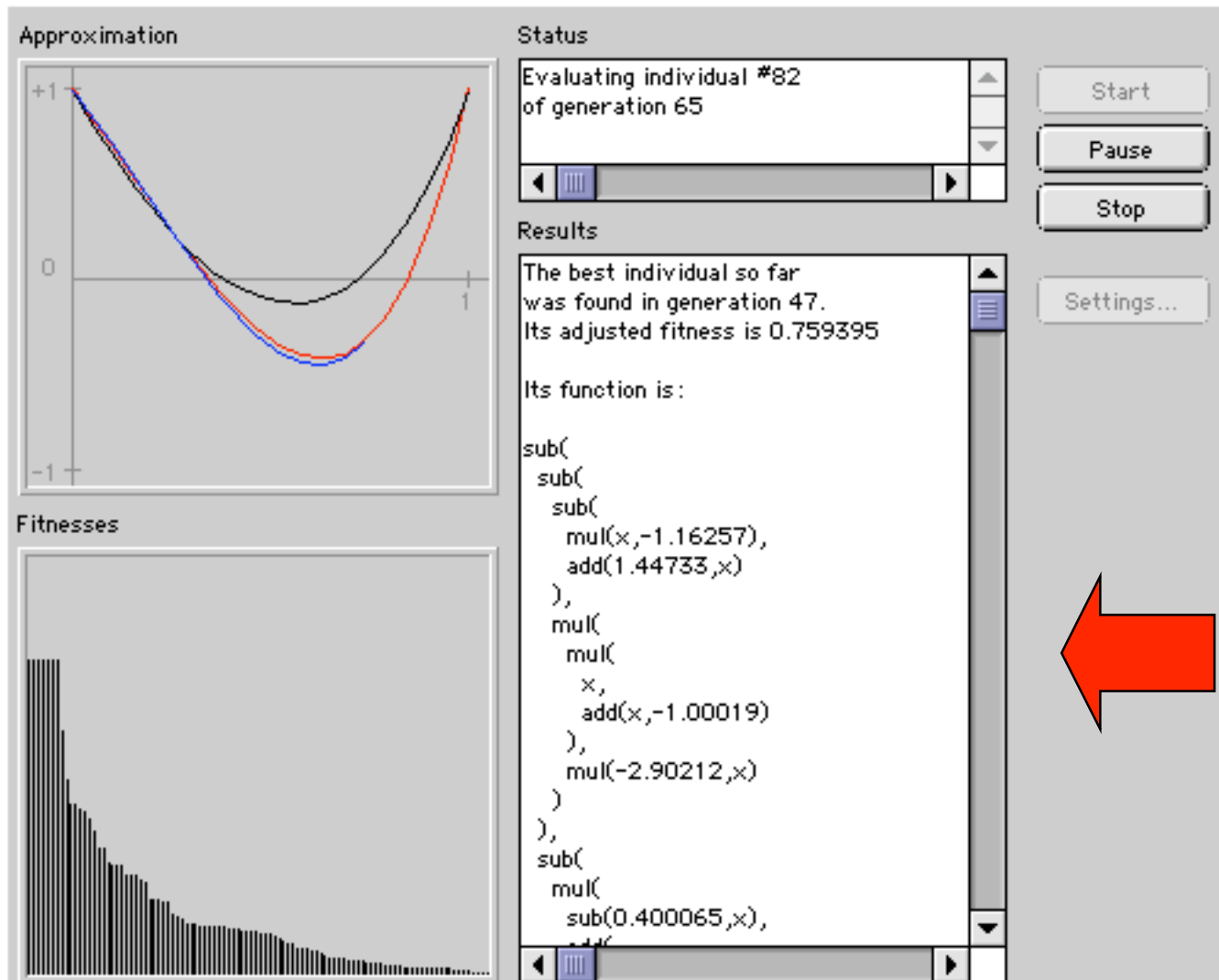


# Crossover of Two Programs



# Genetic Programming Demo: Symbolic Regression

(<http://www.ifh.ee.ethz.ch/~gerber/approx/default.html>)



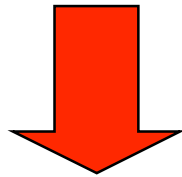
The evolved program

```
sub(  
  sub(  
    sub(  
      mul(x,-1.16257),  
      add(1.44733,x)  
    ),  
    mul(  
      x,  
      add(x,-1.00019)  
    ),  
    mul(-2.90212,x)  
  )  
,  
  sub(  
    mul(  
      sub(0.400065,x),  
      ...  
    )  
  )  
)
```

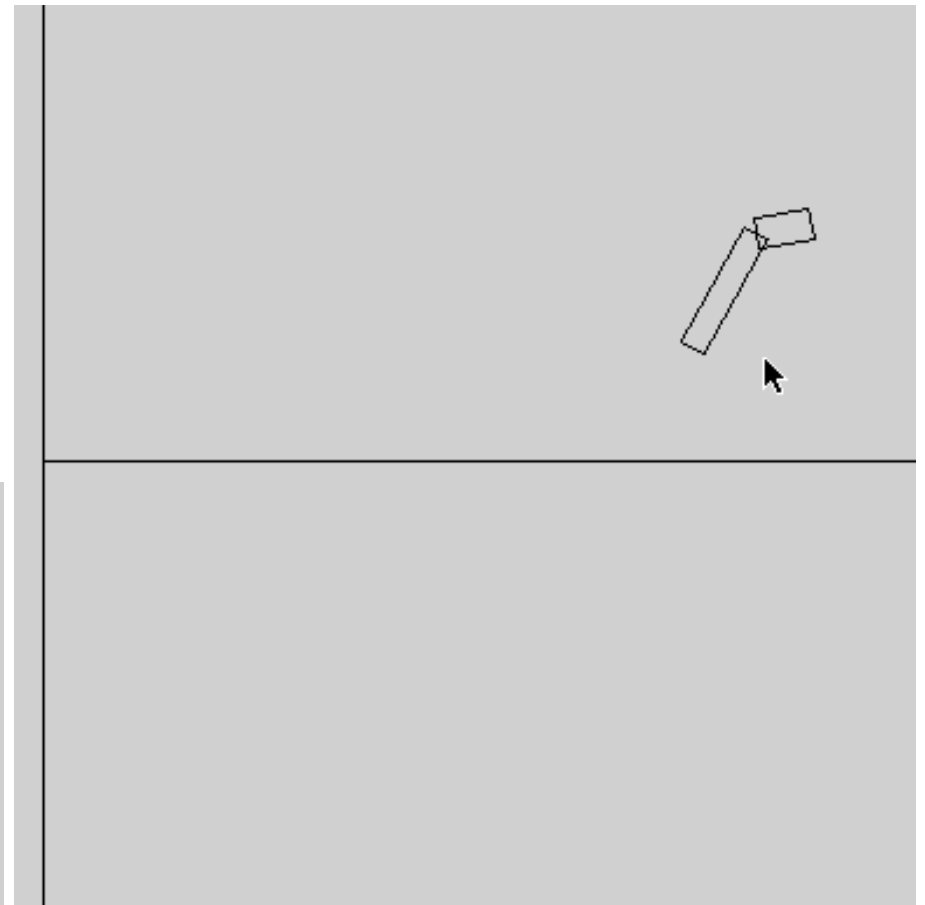
# Truck-Backer using GP

<http://www.handshake.de/user/blickle/Truck/index.html>

The  
evolved  
program



```
PLUS[MINUS[y,MUL[x,trailert]],IFLTZ[PLUS[MINUS[y  
MUL[x,trailert]],x],PLUS[PLUS[0.124600,cabt],  
ATG[-0.798000,0.220800]],  
PLUS[PLUS[cabt,cabt],PLUS[MINUS[y,MUL[MINUS[y,  
MUL[MINUS[y,MUL[MINUS[y,MUL[x,trailert]],  
trailert]] trailert]] trailert]] PLUS[PLUS[cabt
```



# GP Caution

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- Typically fitness of genetically-evolved programs is established by working on a large number of test cases.
- We know this is not completely sound.
- A possible fruitful area is to evolve a proof of correctness along with the program itself. I know of no work in this area.

# Engineering Applications: Evolving Hardware (Analog & Digital)

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- The evolved program is a *list of instructions* for constructing the circuit, rather than the graph of the circuit itself.
- This approach has also been used to construct neural networks.
- The results for circuit design are competitive with, or superior to, human engineering.
- Numerous patents have been reinvented using GP.

# Generating Analog Circuits

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## EETIMES

June 03, 1996, Issue: 904

Section: Technology

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### Genetic program auto-designs analog circuits

R. Colin Johnson

Palo Alto, Calif. - Genetic algorithms (GA) can sometimes rescue software engineers stymied by problems that don't lend themselves to conventional programming techniques. But hardware engineers should be using GAs for designing analog circuits too, claims Stanford professor John Koza.

"Genetic programming can design what-you-want-is-what-you-get electronic circuitry without any prior knowledge about electrical engineering," said Koza. He went on to contrast his approach with that of conventional artificial intelligence: "AI says that the power is in the knowledge, but I say that knowledge is the enemy.

"What we want to use is nature's method to evolve optimal solutions without the hindrance of preconceived knowledge."

<http://www.genetic-programming.com/published/eetimes060396.html>

# An analog filter generated by genetic programming

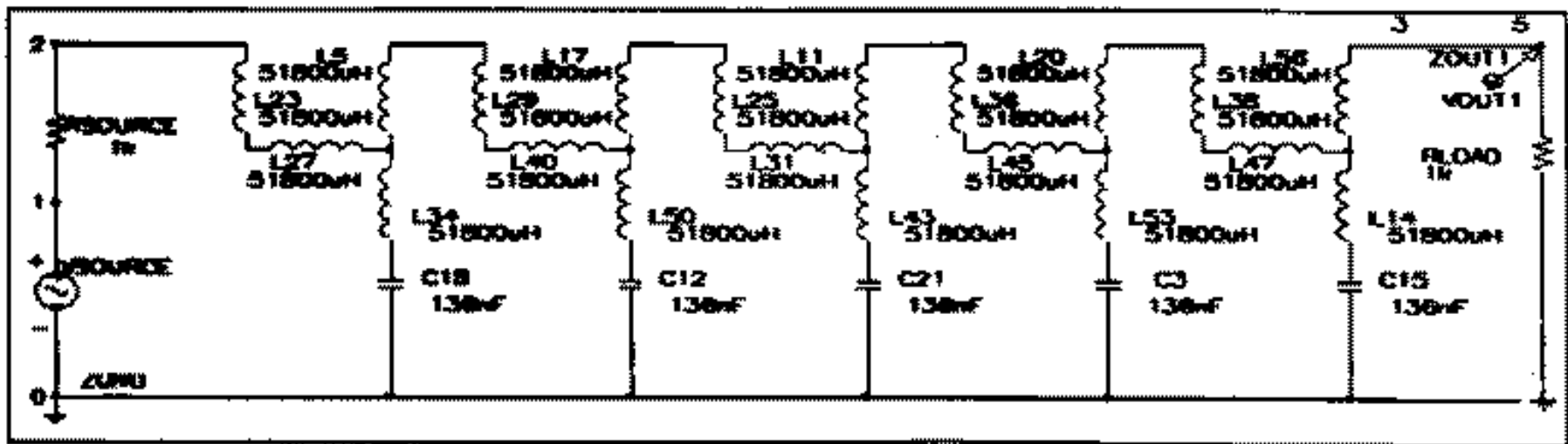


Figure 7 The 100% compliant best circuit of generation 31 has the Cauer (elliptic) topology.

# A Genetically-Evolved Amplifier

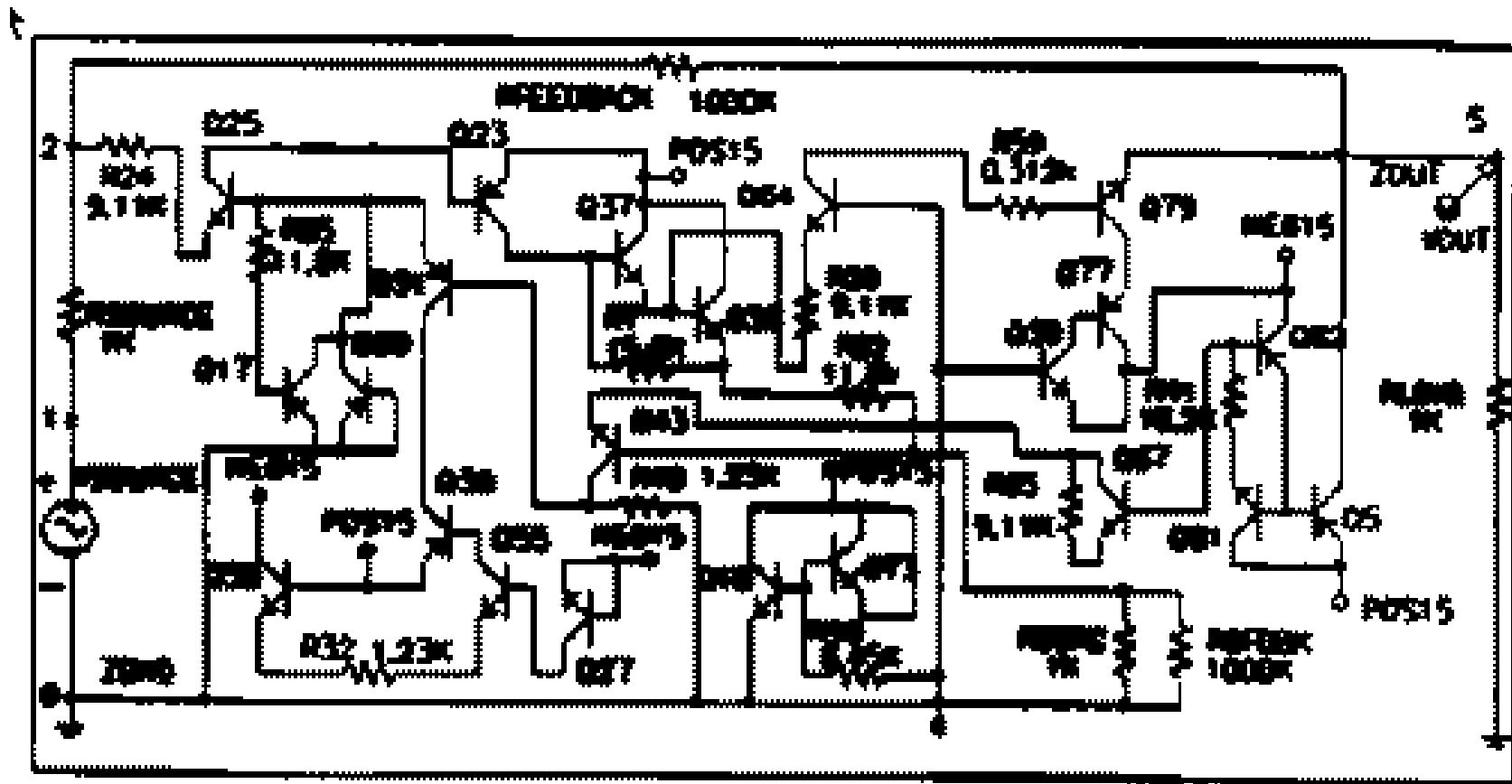


Figure 13 Best circuit from generation 109.

# Koza (striped shirt) with 70-node Beowulf cluster

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# Koza's 1000 node Beowulf used for genetic programming

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# Commercial Applications: Marketing Projections



**POPULATION AND BREEDING CONTROLS**

**POPULATION**

Population size: 1000  
Max prog length: 24

**Stop when**

Decile 1 Cum Lift is greater 300  
OR generations = 100

**Breeding Parameters**

PROBABILITIES	%
Crossover	80
Terminal Selection	16
Mutation (I/R/P)	50
Editing	2

Set standard breeding values

**FITNESS CONTROL**

**FITNESS BASED ON**

OLS only  
 G-1  
 G-max  
 entropy  
 take logs of dependent

Using  
Squares   
Absolutes

**SELECTION METHOD**

Fitness only  
 Fitness + beauty  
 Tournament

Pressure: 1.2  
Elitism %: 66

**DATA SAMPLING METHODS**

**SAMPLING OPTIONS**

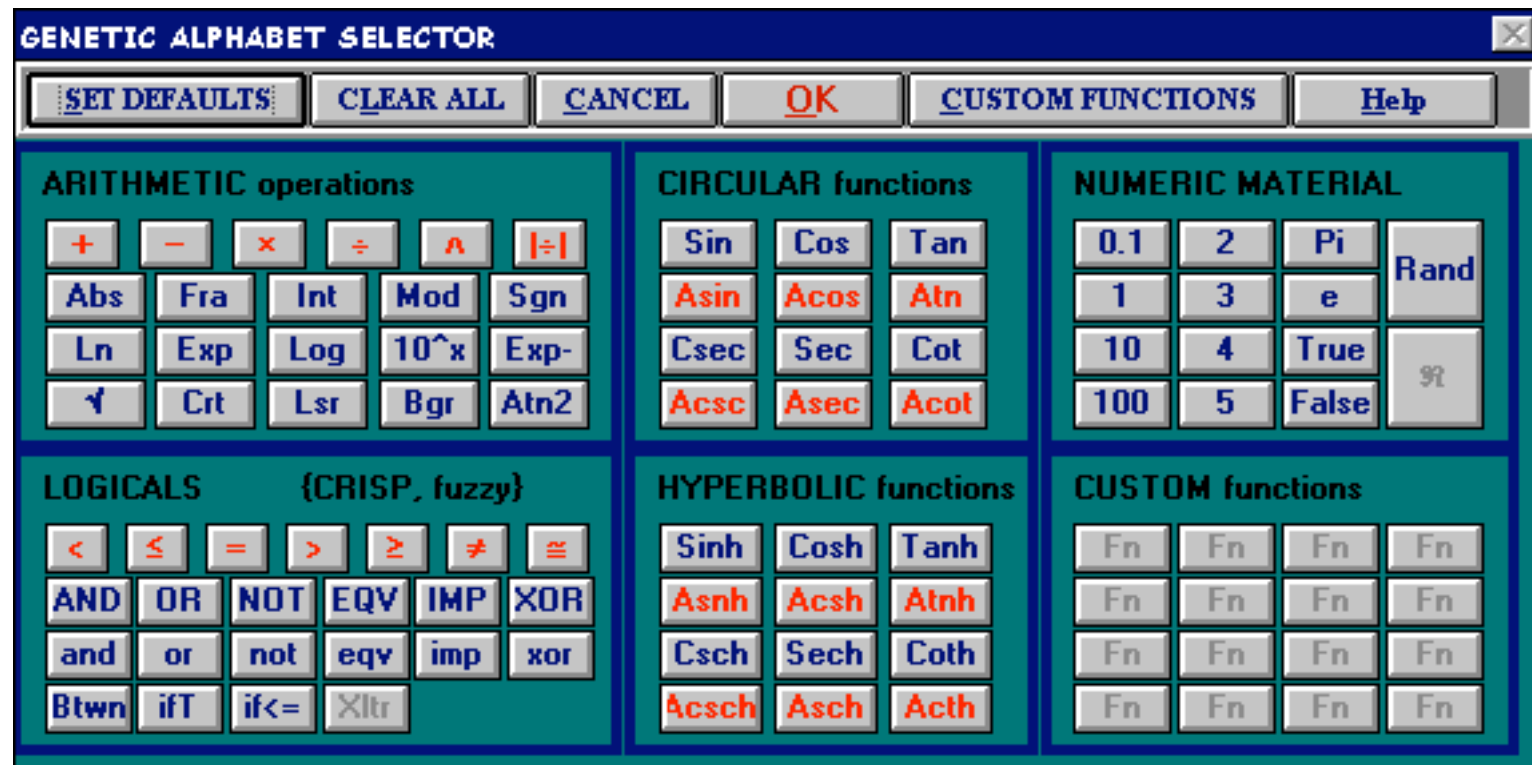
All data  
 Sliding window  
 Every Nth  
 x% evenly spread  
 x% randomly spread

OK Cancel

<http://www.statsoft.com/textbook/stcluan.html#h>

# Gmax-dm

## Function Repertoire Menu



# Other Opportunities

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- Parallelism in Computation (local work of Beda & Margileth, and Tom Johnson, CS 152 steu)
- Parallelism optimizing transformations
- Music
- Robotics

# Koza GP Video Clips

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