Petri Nets with Time
Adding *Time* to Petri Nets

- **Variation 1:** *Transitions* have a delay time; firing takes a non-zero time from enabling. Time may be bounded from above or below.

- **Variation 2:** *Places* have a delay time: A token must dwell on a place a certain amount of time (determined by the place) before becoming usable in firing.

- **Variation 3:** Like 2, but *Tokens* have a delay time.
Variation 1 is Prevalent

A **Time Petri Net** is like a Petri Net with a time interval on each transition:

\[ [t_1, t_2] \quad \text{or} \quad [t_1, \infty) \]

From the time the transition is enabled, it cannot fire before \( t_1 \) and *must* fire by \( t_2 \) (unless disabled by firing another transition).
Example: Representing Time-out

If the normal transition has not fired by time \( \delta \) after being enabled, then the time-out transition will fire and the normal transition will be disabled.
Give sufficient conditions for boundedness for Time Petri Nets with rational time bounds.
Example: Sending messages between two sites.
Problem

- A message sent by a sender could get lost or be garbled.

- Thus the receiver must ack each message.

- If the ack is not received in a specified time, the transmission is regarded as having timed out and the sender must resend.

- The ack could also get lost or be garbled.
Problem, continued

- The sender might decide to resend although the original message has only been delayed, not lost.

- How can the receiver tell whether an incoming message is new or just a retransmission of an earlier message?
A Solution

- Each message is uniquely **timestamped** by a sequence number.

- The receiver only accepts and acknowledges the next number in sequence, not the replay of an earlier number.

- The acknowledgment indicates the number of the message being acknowledged.
Problem & Fix

- The set of timestamps is not bounded.

- Alternating bit protocol (ABP):
  - Use only 0 and 1 as numbers.
  - Sender sends 1 only when 0 has been successfully acknowledged.
  - Sender sends 0 only when 1 has been successfully acknowledged.
Only one message can be in transit at a time.
More general possibilities (not ABP)
A message can be sent at an arbitrary time.

Once sent, the message can be received or lost, within a bounded time.

If the message is received, an ack is sent.

The ack can be received or lost.

If an ack is not received in a bounded time, the message is resent.

If a resent message is received, it is ack’ed.
Pseudo-Code
(from http://www.fmi.uni-stuttgart.de/szs/teaching/ws0405/nets/nets.pdf)

Assume that `send` and `recv` are primitives for sending and receiving a single piece of data over a channel.

```c
void abp.send () {
    i = 0; s = 0;
    while (true) {
        i = i+1; s = !s;
        while (true) {
            send (data[i],s);
            wait (timeout);
            if (recv(ack) == s) break;
        }
    }
}

void abp.recv () {
    i = 0; r = 0;
    while (true) {
        i = i+1; r = !r;
        while (true) {
            recv (c,b);
            send (b);
            if (b == r) { data[i] = c; break; }
        }
    }
}
```
State Chart Version of ABP
(from:http://ls4-www.cs.uni-dortmund.de/home/thummler/papers/WOSP00.pdf)
ABP in Uppaal

1 of 16 possible messages
Example from Berthomieu & Diaz: Representing ABP in TPN

Basic

If the message is sent at time $t$, it will be received by time $t+1$. 
We will focus on the 0 half of the protocol. The 1 half is a mirror image.
ABP:
Add possible loss

If the message is sent at time $t$, it will be received or lost by time $t+1$. 
ABP:
Add Acknowledgement

If a message sent at time $t$ is received by $t+1$, it will be ack’ed by $t+3$ and the ack received by $t+4$.

This is the ack time assumed by B&D. Would 1 work just as well?
ABP:
Add Resend Capability

If a message sent at time $t$ is not ack’ed by $t+4$, it will be resent by $t+6$. A different transition is used for resend.
ABP:
Add receipt of resent messages

send msg [0, ∞)

receive ack [0, 1]

lose msg [0, 1]

resend msg [5, 6]

receive and accept msg [0, 1]

send ack [0, 2]

lose ack [0, 1]

receive resent msg [0, 1]

A duplicate of an earlier message is still ack’ed.
The original ack may have been lost.
By showing that the system is bounded, in even the original cyclic context, it is established that finite queuing capacity suffices.

B&D give a sufficient condition for boundedness and show that it is satisfied for the version of the ABP presented here.

B&D develop a “Class Diagram” (not UML) representation for TPN and show that it is finite for this particular example. (In general, it won’t be.)
B&D Class Diagram

- Each node of the class diagram includes:
  - State (or “marking”), giving the distribution of tokens on places.
  - For each enabled transition, upper and lower bounds on when the transition can fire, relative to the time at which the class is entered.
ABP:
Full System

Coding
- send/recv
- ack/recv
- lose
- resend/recv
- recv duplicate

- $t_1 [0, \infty)$
- $t_2 [5, 6]$
- $t_3 [0, 1]$
- $t_4 [0, \infty)$
- $t_5 [5, 6]$
- $t_6 [0, 1]$
- $t_7 [0, 1]$
- $t_8 [0, 2]$
- $t_9 [0, 1]$
- $t_{10} [0, 1]$
- $t_{11} [0, 2]$
- $t_{12} [0, 1]$
- $t_{13} [0, 1]$
- $t_{14} [0, 1]$
- $t_{15} [0, 1]$
- $t_{16} [0, 1]$
The state class diagram has one node per combination of marking and transition time-bounds. In general, the diagram can be finite or infinite.
Other Uses of the State Class Diagram

- Determine various properties of the system, much as could be done by inspecting a finite-state-machine state diagram.

- For example,
  - Are two specific transitions ever enabled simultaneously?
  - Is mutual exclusion ever violated?
  - Is a buffer bound ever exceeded?
  - Can there be deadlock?
We see that there is never more than one message outstanding on a channel.

If the retransmission time-out were set too low, this would not be the case.

There is no deadlock.
Exercise: Develop a specification, such as a Time Petri Net specification, for the following real-time problem:

- A home alarm system has the following objects:
  - Siren
  - Entry switch (indicates when door is open)
  - Keypad (for arming/disarming)

- The keypad is located inside the home and one must use the door to get to it.
If the system is not armed, the siren will not sound.

When the system is set to be armed via the keypad, the user has 30 seconds in which to use the door before the system actually becomes armed.

If the door is opened while the system is armed, the siren will sound, *unless* the combination is entered on the keypad within 15 seconds.

Once the siren begins sounding, it will continue until disarmed at the keypad or until for 15 minutes have elapsed, at which time it will enter an advisory state that indicates an alarm occurred.

The system will stay in the advisory state until disarmed at the keypad.
The TAPAAL tool offers a graphical editor for drawing TAPN models, simulator for experimenting with the designed nets and a verification environment that automatically answers logical queries formulated in a subset of CTL logic (essentially EF, EG, AF, AG formulae without nesting). It also allows the user to check whether a given net is k-bounded for a given number k. The verification algorithm translates the TAPAAL queries into UPPAAL ones and relies on the UPPAAL verification engine, but the user does not have to leave the TAPAAL GUI during any phase of the model verification and error traces are displayed directly in TAPAAL.

Source: http://www.tapaal.net/
Definition of Timed-Arc Petri Nets

- Tokens are annotated with an age (an integer value indicating the elapsed time from its creation).

- Arcs connecting places with transitions have an associated time interval, which limits the age of the tokens consumed to fire the adjacent transition.
TAPAAL
Origin of TAPN
(Timed-Arc Petri Nets)


Timed-Arc Petri Nets vs.
Networks of Timed Automata

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Abstract. We establish mutual translations between the classes of 1-safe timed-arc Petri nets (and its extension with testing arcs) and networks of timed automata (and its subclass where every clock used in the guard has to be reset). The presented translations are very tight (up to isomorphism of labelled transition systems with time). This provides a convenient characterization from the theoretical point of view but is not always satisfactory from the practical point of view because of the possible non-polynomial blow up in the size (in the direction from automata to nets). Hence we relax the isomorphism requirement and provide efficient (polynomial time) reductions between networks of timed automata and 1-safe timed-arc Petri nets preserving the answer to the reachability question. This makes our techniques suitable for automatic translation into a format required by tools like UPPAAL and KRONOS. A direct corollary of the presented reductions is a new PSPACE-completeness result for reachability in 1-safe timed-arc Petri nets, reusing the region/zone techniques already developed for timed automata.
Other Variations on Petri Nets

- Add inhibiting arcs
- Add logic
- Add priorities to transitions
- Add stochastic behavior
- Coloured Petri Nets (Jensen)
  - Add types to tokens
  - Add complex operations to transitions
  - Add hierarchy
- HL (High-Level) Nets
For XML fans: PNML

http://www2.informatik.hu-berlin.de/top/pnml/about.html

- Petri Net mathematical description

```xml
<pn>
  <place id="input">
    <name>Input</name>
    <type>InItem</type>
  </place>

  <arc id="a1">
    <placeend idref="input">
      <transend idref="get-next-item">
        <expr>iitem</expr>
      </transend>
    </placeend>
  </arc>

  <transition id="get-next-item">
    <name>Get Next Item</name>
  </transition>

  <place id="idle">
    <name>Idle</name>
    <type>M</type>
    <initmark>M</initmark>
  </place>

  <arc id="a2">
    <placeend idref="idle">
      <transend idref="get-next-item">
        <expr>m</expr>
      </transend>
    </placeend>
  </arc>

  ...

</pn>
```
For XML fans: PNML

Petri Net layout description

```xml
<layout>
  <node ref="machine.pn#input">
    <coord>
      <x>10.0</x>
      <y>0.0</y>
    </coord>
  </node>

  <conn ref="machine.pn#a1">
    <!-- no bend points -->
  </conn>

  <node ref="machine.pn#get-next-item">
    <coord>
      <x>10.0</x>
      <y>10.0</y>
    </coord>
  </node>

  <conn ref="machine.pn#a2">
    <coord>
      <x>20.0</x>
      <y>20.0</y>
    </coord>
  </conn>

  <node ref="machine.pn#idle">
    <coord>
      <x>20.0</x>
      <y>10.0</y>
    </coord>
  </node>

  <conn ref="machine.pn#a2">
    <coord>
      <x>20.0</x>
      <y>10.0</y>
    </coord>
  </conn>

  ...

</layout>
```