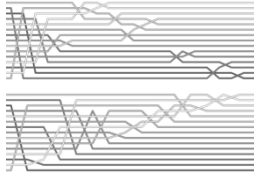


# CS 42 Today

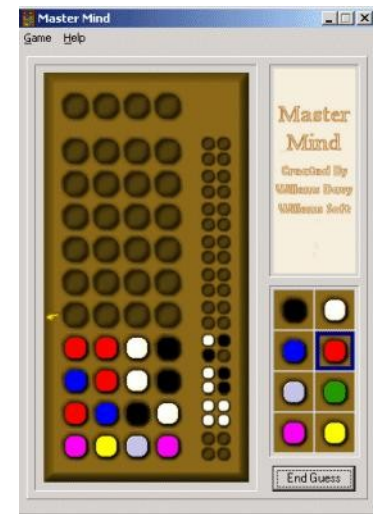
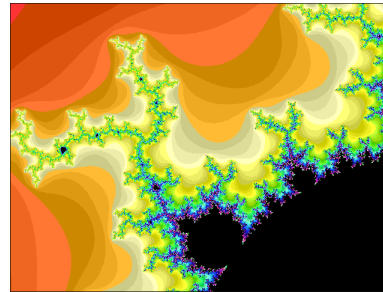
Today:

More sorting



files

## HW7 PREVIEW



'Cause somethin' like he left knee and a harp," said he had to the whole school? The shouting and then some strange and Mrs. "Well, I know Hagrid; they spotted handkerchief and get him get rid of course, had a gigantic beet with her," he knew what to all he's

All the sky with the sun in the sun in the church where you're gone Lucy in my eyes. There beneath the girl with an hourglass And then the banker never wears a lot to hold your hand. Can't buy me tight, tight Owww! Love is love I can't hide,

Who is the author?    What is the work?    What is going on?

This is but ourselves. No, faith, My uncle! O royal bed of confession Of your rue for leave to nature; to this time I should weep for thy life is rotten before he is. have sworn 't. Or my blood. I have closely sent for nine; and unprofitable,

The Senators and the date of a written declaration that Purpose, they shall consist of nine States, shall not, when he shall have such Vacancies. The President pro tempore, in the Desire of a Qualification to the Speaker of the Senate. Article 6. When vacancies by the office upon probable

# Sorting Algorithms

Slow:

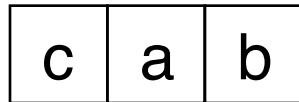
1 1 1  
1 1 2  
1 1 3  
1 2 1  
1 2 2  
1 2 3  
1 3 1  
1 3 2  
1 3 3  
2 1 1  
2 1 2  
2 1 3  
2 2 1  
2 2 2  
2 2 3  
2 3 1  
2 3 2  
2 3 3  
3 1 1  
3 1 2  
3 1 3  
3 2 1

the *fruit flies* of complexity theory...

## Checksort

check permutations until sorted

List of length n



Check:

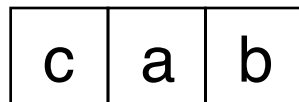
3 1 2  
3 2 1  
1 2 3  
1 3 2  
2 1 3  
2 3 1

"bogosort"

## SlowSort !

pull # s from a hat  
**with** replacement...

List of length n



[article](#) [discussion](#) [edit this page](#) [history](#)

## Bogosort

From Wikipedia, the free encyclopedia

**Bogosort** is a particularly ineffective [sorting algorithm](#).

# Sorting Algorithms: Can we do better?

---

---

Yes!



Fun for all ages

# Sorting Algorithms

---

---

The fruit flies of complexity theory...

**Minsort**  
choose the min each iteration

7	4	3	2	1	5	0	6
---	---	---	---	---	---	---	---

# An algorithm of a similar sort...

---

---

**Insertion Sort**  
insert elements in order to the left

7	4	3	2	1	5	0	6
---	---	---	---	---	---	---	---

vs. minsort ?  
better than  $O(N^2)$ ?

# < $N^2$ run times... ?

1959

**Shell Sort**  
sort column-sublists of increasing size

7	4	3	2	1	5	0	6	1
---	---	---	---	---	---	---	---	---

# $<O(N^2)$ via 2d sorting!

Shell Sort  
sort column-sublists of increasing size

7	4	3	2	1	5	0	6	1
---	---	---	---	---	---	---	---	---

7	4	3	2	1
5	0	6	1	



5	0	3	1	1
7	4	6	2	

2 elements per column

# $<O(N^2)$ via 2d sorting!

Shell Sort  
sort column-sublists of increasing size

7	4	3	2	1	5	0	6	1
---	---	---	---	---	---	---	---	---

7	4	3	2	1
5	0	6	1	



5	0	3	1	1
7	4	6	2	

2 elements per column

5	0	3
1	1	7
4	6	2



1	0	2
4	1	3
5	6	7

3 elements per column



# $<O(N^2)$ via 2d sorting!

Shell Sort  
sort column-sublists of increasing size

7	4	3	2	1	5	0	6	1
---	---	---	---	---	---	---	---	---

7	4	3	2	1
5	0	6	1	



5	0	3	1	1
7	4	6	2	

2 elements per column

5	0	3
1	1	7
4	6	2



1	0	2
4	1	3
5	6	7

3 elements per column

1	0
2	4
1	3
5	6
7	



1	0
1	3
2	4
5	6
7	

4 el. per col.

# $O(N^{3/2})$ or better

depending on the skip sequence

## Shell Sort

sort column-sublists of increasing size

7	4	3	2	1	5	0	6	1
---	---	---	---	---	---	---	---	---

7	4	3	2	1
5	0	6	1	



5	0	3	1	1
7	4	6	2	

2 elements per column

5	0	3
1	1	7
4	6	2



1	0	2
4	1	3
5	6	7

3 elements per column

1	0
2	4
1	3
5	6
7	



1	0
1	3
2	4
5	6
7	

4 el. per col.

1
0
1
3
2
4
5
6
7

N el. per col.

# Divide and Conquer

---

---

**Mergesort**  
merge sorted lists together

7	4	3	2	1	5	0	6
---	---	---	---	---	---	---	---

# Running Time: **Loop counting**

---

---

**How many steps are needed? (usually in the worst case...)**

$T(N)$  = running time as a function of problem size,  $N$

**MM algorithm:**

The problem size is the list length,  $N$ .  
Each comparison ( $<$  or  $>$ ) will count as 1 step

```
for ( i=1 ; i < N ; ++i )
{
    if (L[i] > E) E = L[i];
    if (L[i] < e) e = L[i];
}
```

**Running Times:**

$T(N) =$

nested loops?  
big-O?

# Running Time: Loop counting

---

---

Nested loops will produce a series ...

```
for ( int i=0 ; i<N ; ++i )
{
    for ( int j=0 ; j<(i*i) ; ++j )
    {
        1 time step of work here...
    }
}
```

i see you're up  
to something...



but not always  $O(N^2)$ !

# Algorithms and Impatience

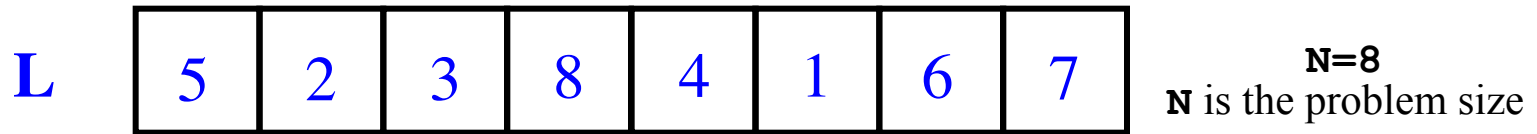
hubris  
laziness

---

---

Problem: Search through an array to find  $\max$  *and*  $\min$

Divide-and-conquer!



better or worse than looping?  
in absolute terms? / big-O terms?

# Running Time: Recurrences

---

---

$T(N)$  = running time as a function of problem size,  $N$

Recursive algorithms lead to *recurrence relationships*:

base case: **MMRec(L) :**      `if L == [x,y] and x > y then  
return [x,y] else return [y,x];`

recursion: **MMRec(L) :**      `[E1,e1] = MMRec( half1(L) ),      first half of L  
[E2,e2] = MMRec( half2(L) ),      second half of L  
if E1 > E2 then E=E1 else E=E2,  
if e1 < e2 then e=e1 else e=e2,  
return [E,e];`

Running Time:

as a Recurrence Relation

$$T(2) = 1$$

$$T(N) =$$

# Recurrences

---

---

Recurrence relation from the recursive max/min finding program...

$$T(2) = 1$$

$$T(N) = 2 T\left(\frac{N}{2}\right) + 2$$

what is  $T(N/2)$  ?

recursive vs. looping?  
big-O?

# Mergesort

---

---

Mergesort  
merges sorted lists together

7	4	3	2	1	5	0	6
---	---	---	---	---	---	---	---

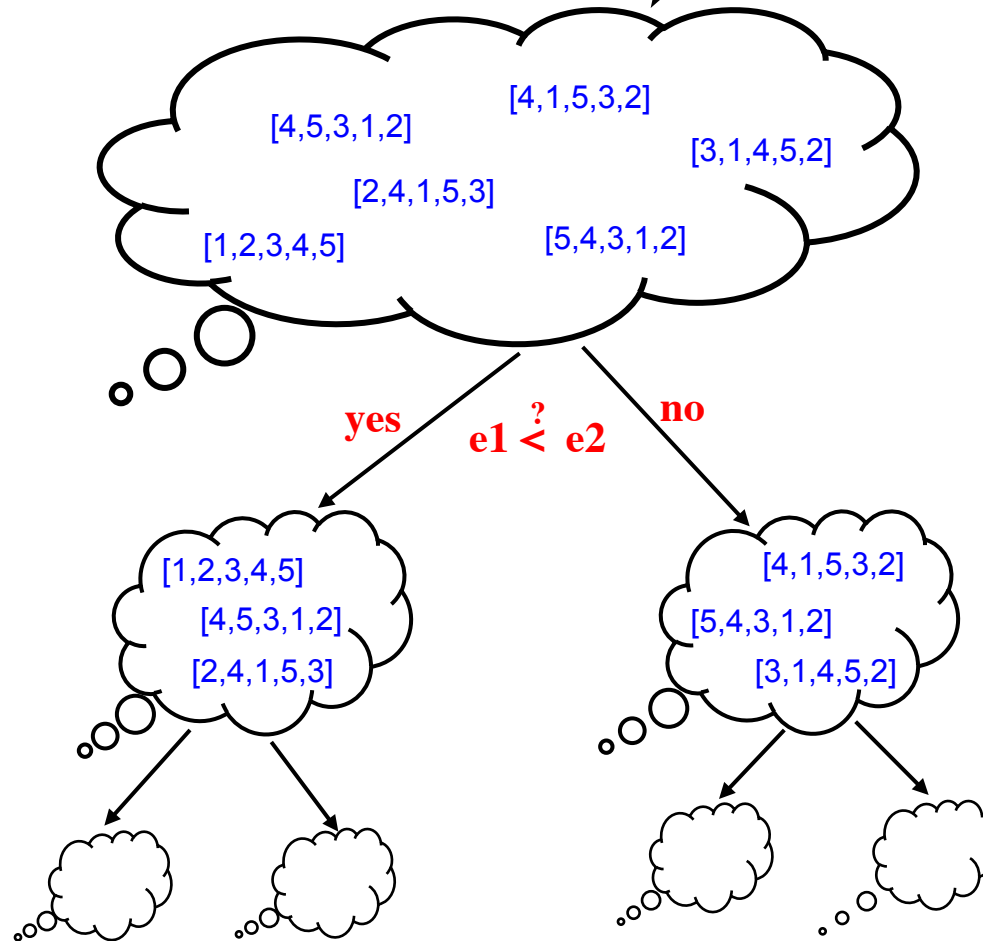
Recurrence relation for mergesort:

Big-O running time:

# Any Comparison Sort is at best $O(n \cdot \log(n))$

Start with all of the permutations of an n-element list.  
[ $e_1, e_2, e_3, \dots, e_n$ ]

Sorting is equivalent to determining *which* of the permutations we started with...



The Adversary

“Adversary Argument”

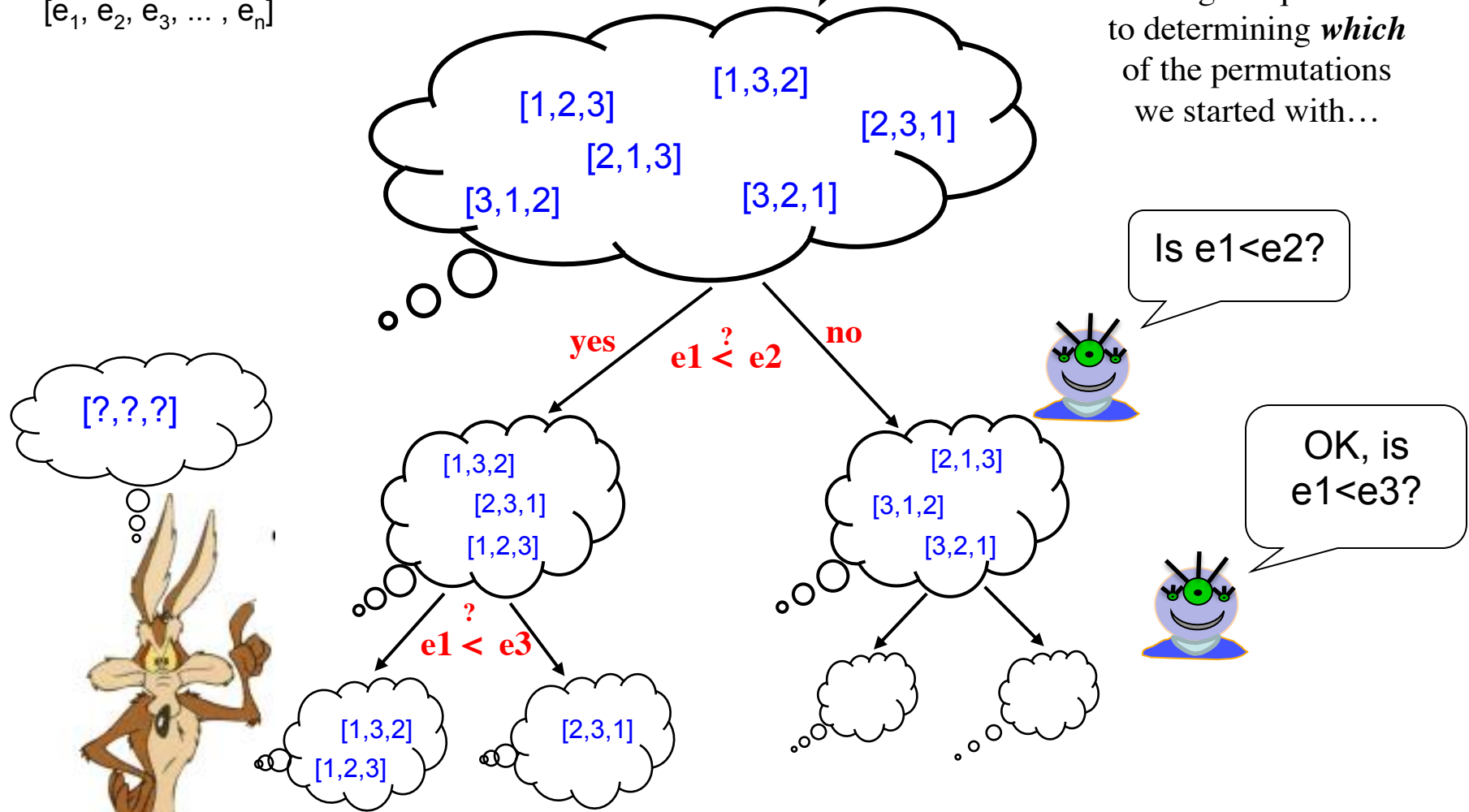


The “adversary” doesn't seem to do all that much...

# Any Comparison Sort is at best $O(n \cdot \log(n))$

Start with all of the permutations of an n-element list.  
 $[e_1, e_2, e_3, \dots, e_n]$

Sorting is equivalent to determining *which* of the permutations we started with...



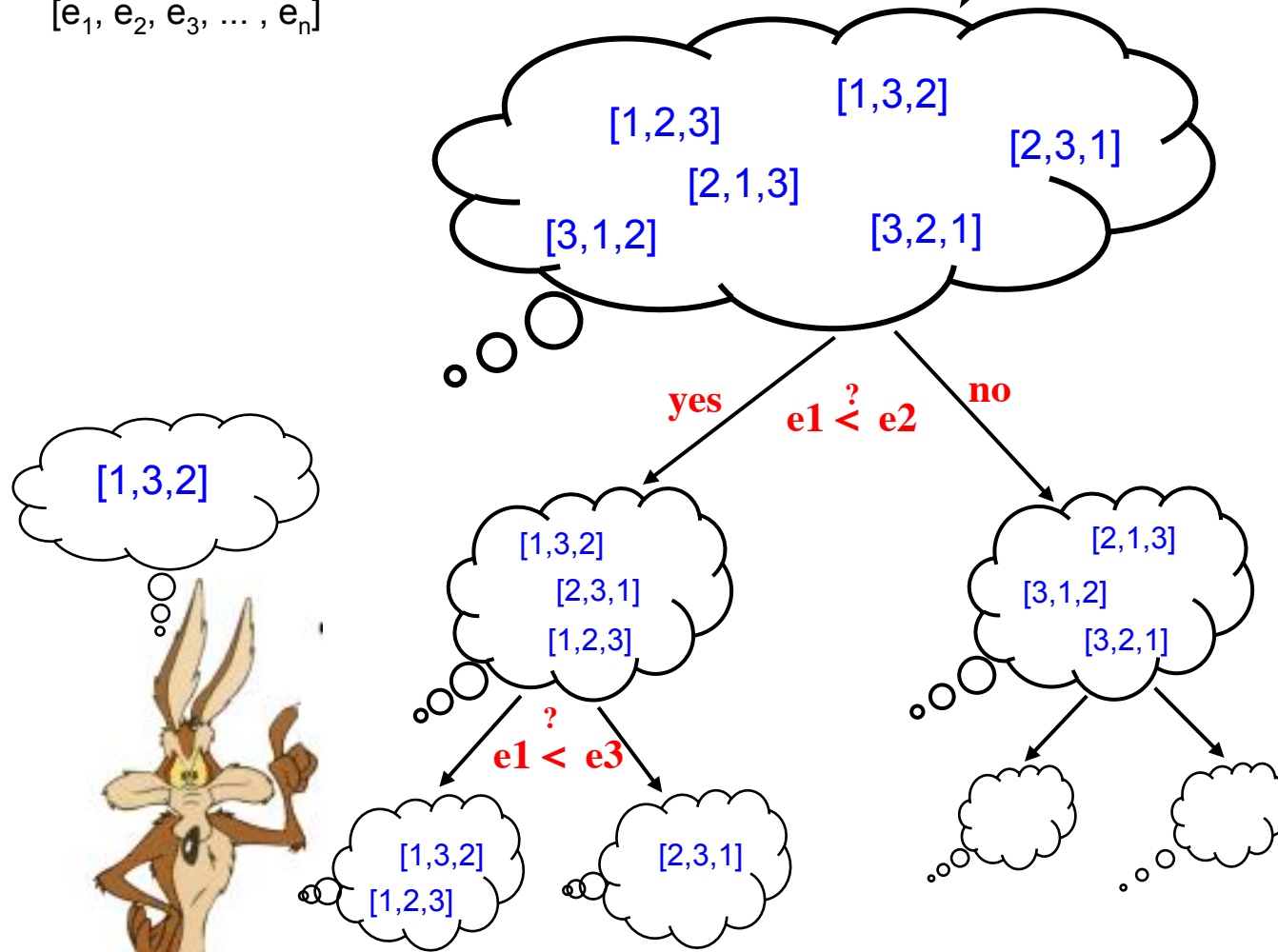
The Adversary

“Adversary Argument”

# Any Comparison Sort is at best $O(n \cdot \log(n))$

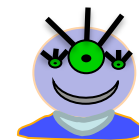
Start with all of the permutations of an n-element list.  
 $[e_1, e_2, e_3, \dots, e_n]$

Sorting is equivalent to determining *which* of the permutations we started with...



The Adversary

“Adversary Argument”

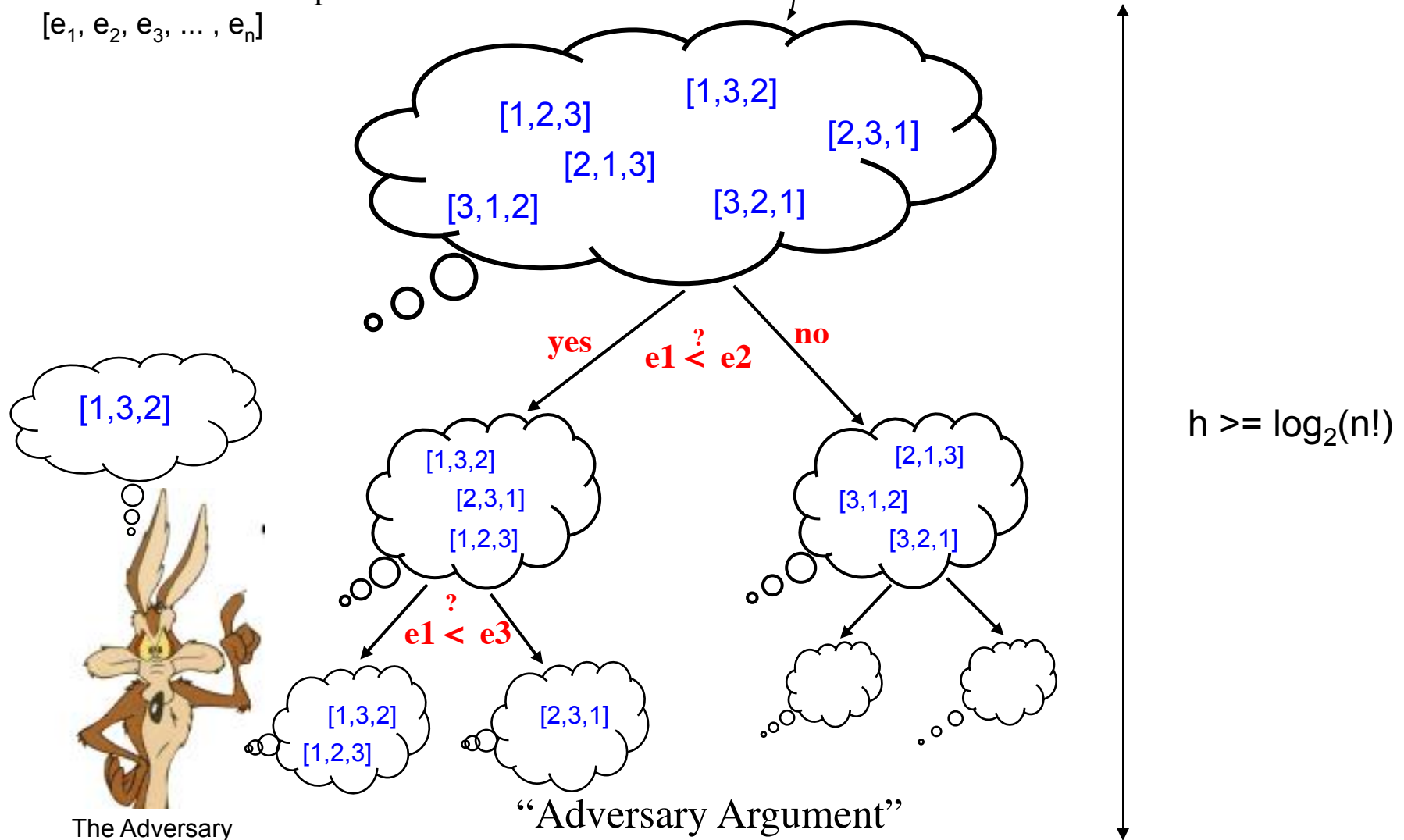


Ah, this adversary is tricky after all!

# Any Comparison Sort is at best $O(n \cdot \log(n))$

Start with all of the permutations of an n-element list.

$[e_1, e_2, e_3, \dots, e_n]$



# Fun with Logs and Big-Omega

---

---

$$\left(\frac{n}{2}\right)^{\frac{n}{2}} < n!$$

$$\log\left(\frac{n}{2}\right)^{\frac{n}{2}} < \log n! \leq h$$

$$\frac{1}{2} n \log\left(\frac{n}{2}\right) < \log n! \leq h$$

$$\frac{1}{2} n (\log n - \log 2) < \log n! \leq h$$

$$\frac{1}{2} (n \log n - n \log 2) < \log n! \leq h$$

$$h > \frac{1}{2} (n \log n - n \log 2)$$

$h$  is  $\Omega(n \log n)$

So I guess omega is sort of like  
an upside-down O.



# HW7: Loops, loops and more loops!

---

---

**for**

*definite iteration*

For a **known** number of iterations

**while**

*indefinite iteration*

For an **unknown** number of iterations

# Problem 1: the Mandelbrot Set

Consider the following update rule for all complex numbers  $c$ :

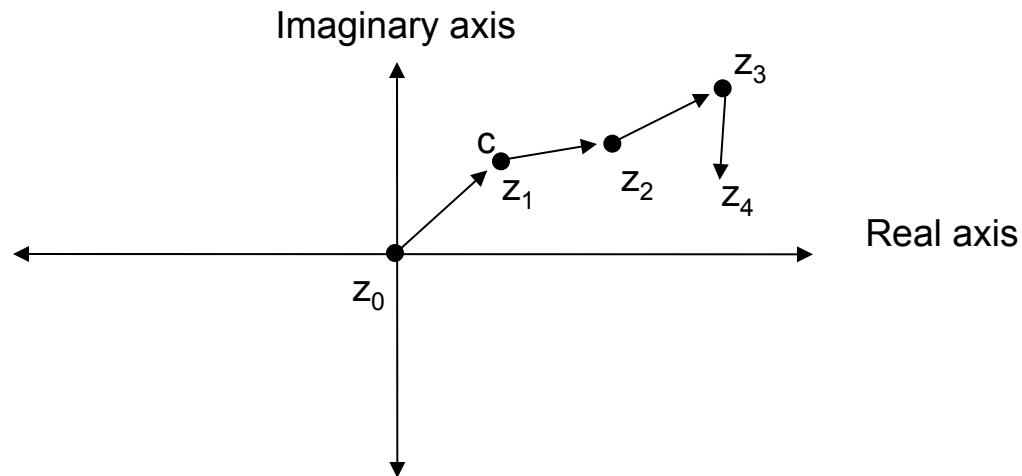
$$z_0 = 0$$

$$z_{n+1} = z_n^2 + c$$



Benoit M.

If  $z$  does *not* diverge, then  $c$  is in the M. Set.



# Problem 1: the Mandelbrot Set

Consider the following update rule for all complex numbers  $c$ :

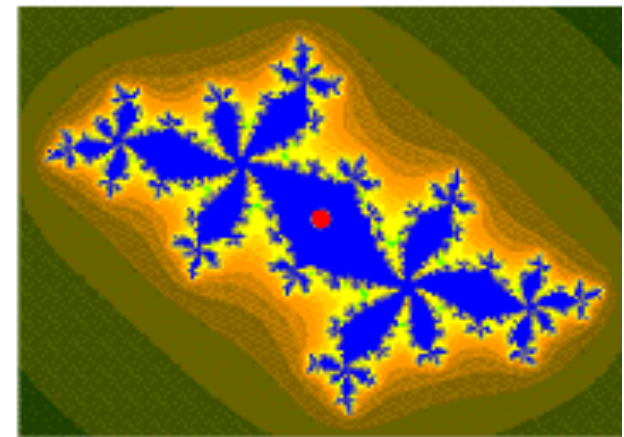
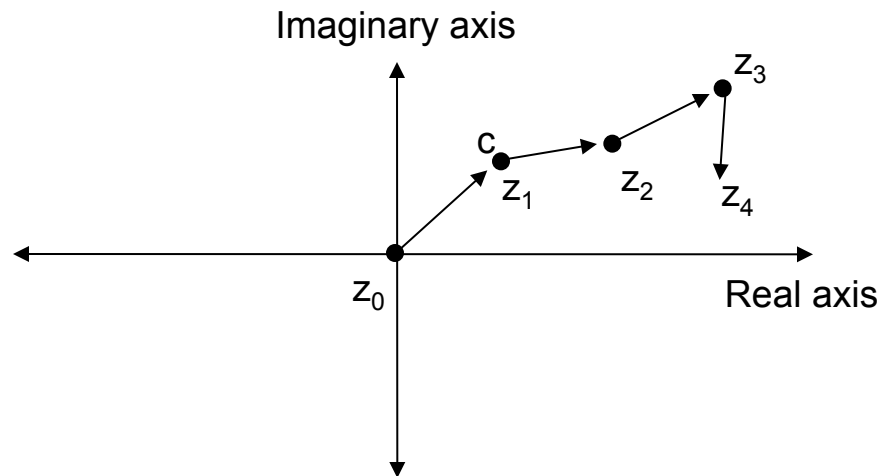
$$z_0 = 0$$

$$z_{n+1} = z_n^2 + c$$



Benoit M.

If  $z$  does *not* diverge, then  $c$  is in the M. Set.



example of a non-diverging cycle

# Problem 1: the Mandelbrot Set

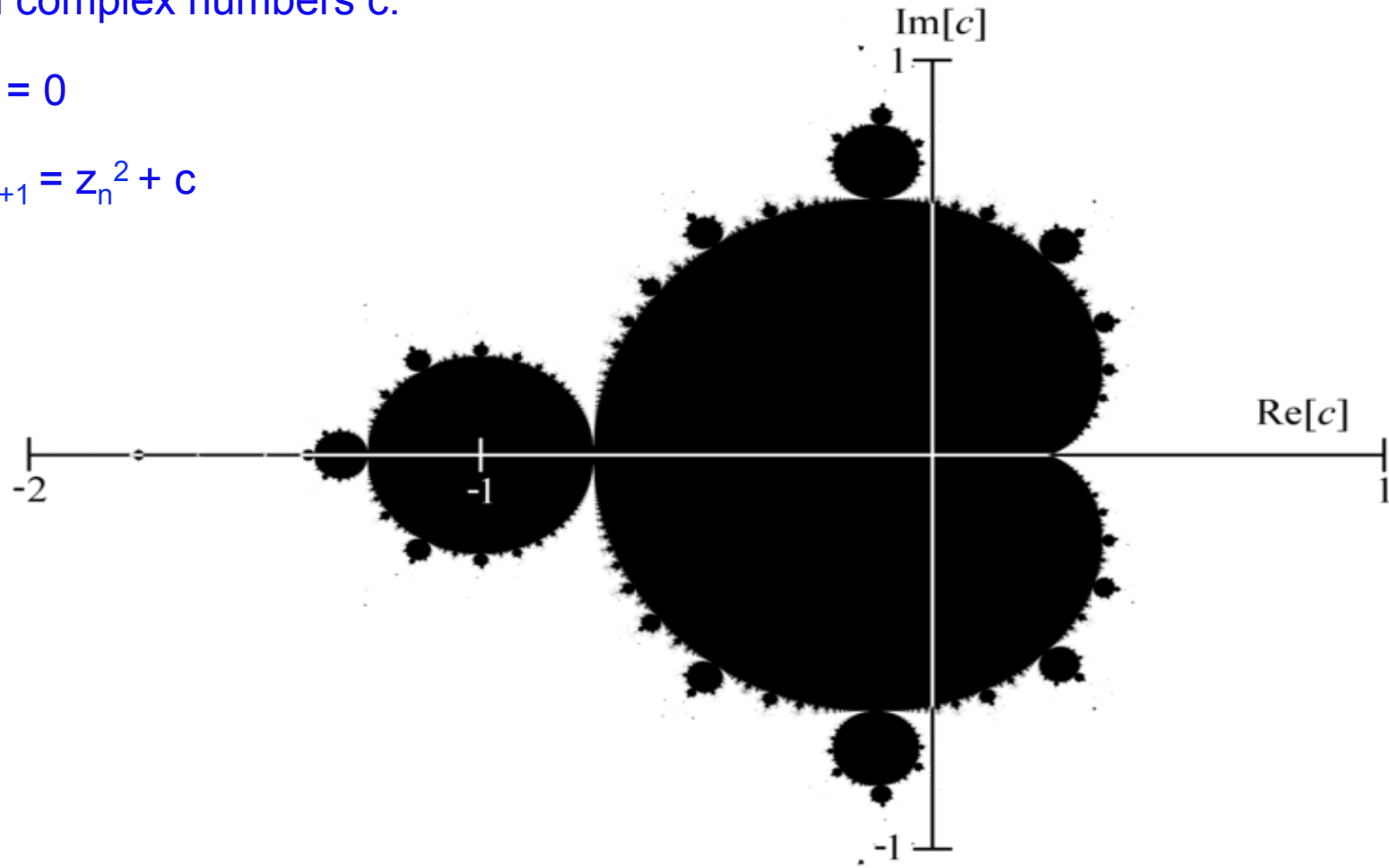
---

---

Consider the following update rule for all complex numbers  $c$ :

$$z_0 = 0$$

$$z_{n+1} = z_n^2 + c$$



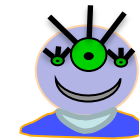
The shaded area are points that do not diverge.

# Python and images

---

---

`from bmp import *` ← *for creating and saving images*



Eco-friendly  
bitmps!

`image = BitMap( 300, 200, Color.GREEN )`

←  
←  
*creates a bitmap object  
and names it **image***

# Python and images and *objects*

---

---

```
from bmp import *
```

```
image = BitMap( 300, 200, Color.GREEN )
```

*here, a bitmap **object** named **image**  
is calling an internal method named **saveFile***



```
image.saveFile( "test.bmp" )
```

# Python and images and *objects*

---

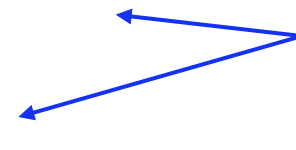
---

```
from bmp import *
```

```
image = BitMap( 300, 200, Color.GREEN )
```

```
image.setPenColor( Color.Red )
```

```
image.plotPixel( 150, 100 )
```



*two more  
internal  
methods*

```
image.saveFile( "test.bmp" )
```

**objects** are variables that can contain their own functions, often called *methods*

# Imagining Images

```
from bmp import *

def test():
    """ image demonstration """
    width = 200
    height = 200
    image = BitMap( width, height )

    # a 2d loop over each pixel
    for col in range(width):

        for row in range(height):

            if col == row:

                image.plotPoint( col, row )

    image.saveFile( "test.bmp" )
```

upper triangle?

thicker diagonal?

reverse?

both?



# Seeing into the future...

---

---

```
def menu():
    choice = 1    # Anything except 9
    while choice != 9:
        print "I see danger in your future..."
        printMenu()
        choice = input("Make your choice ")

    print "The inner eye can see no more"

def printMenu():
    print "What would you like to do?"
    print "\t 0: See another prediction"
    print "\t 9: Quit"
```

"\t" represents a tab



# Gimme a **break**

```
def menu():  
    while True:  
        print "I see danger in your future..."  
        printMenu()  
        choice = input("Make your choice ")  
        if choice == 9:  
            break  
  
    print "The inner eye can see no more"
```

I'll figure out later how  
to get out of this loop!

OK - I'll stop the loop  
now and continue with  
the code *after* the loop

```
def printMenu():  
    print "What would you like to do?"  
    print "\t 0: See another prediction"  
    print "\t 9: Quit"
```

**break** stops the execution of the current loop

# Name that author... ?

---

---

'Cause some like he left knee and a harp," said he had to the whole school? The shouting and then some strange and Mrs. "Well, I know Hagrid; they spotted handkerchief and get him get rid of course, had a gigantic beet with her," he knew what to all he's

All the sky with the sun in the sun in the church where you're gone Lucy in my eyes. There beneath the girl with an hourglass And then the banker never wears a lot to hold your hand. Can't buy me tight, tight Owww! Love is love I can't hide,

Who is the author?

What is the work?

What is going on?

This is but ourselves. No, faith, My uncle!  
O royal bed of confession Of your rue  
for leave to nature; to this time I should  
weep for thy life is rotten before he is.  
have sworn 't. Or my blood. I have  
closely sent for nine; and unprofitable,

The Senators and the date of a written  
declaration that Purpose, they shall consist  
of nine States, shall not, when he shall have  
such Vacancies. The President pro tempore,  
in the Desire of a Qualification to the  
Speaker of the Senate. Article 6. When  
vacancies by the office upon probable

# HW7 Pr 2: Read some text and automatically generate new (reasonable?) text

---

---

'Cause somethin' like he left knee and a harp," said he had to the whole school? The shouting and then some strange and Mrs. "Well, I know Hagrid; they spotted handkerchief and get him get rid of course, had a gigantic beet with her," he knew what to all he's

All the sky with the sun in the sun in the church where you're gone Lucy in my eyes. There beneath the girl with an hourglass And then the banker never wears a lot to hold your hand. Can't buy me tight, tight Owww! Love is love I can't hide,

Who is the author?

What is the work?

What is going on?

This is but ourselves. No, faith, My uncle! O royal bed of confession Of your rue for leave to nature; to this time I should weep for thy life is rotten before he is. have sworn 't. Or my blood. I have closely sent for nine; and unprofitable,

The Senators and the date of a written declaration that Purpose, they shall consist of nine States, shall not, when he shall have such Vacancies. The President pro tempore, in the Desire of a Qualification to the Speaker of the Senate. Article 6. When vacancies by the office upon probable

# Markov Model

Technique for modeling any sequence of natural data

Each item depends *on only the item immediately before it* .

1st-order  
Markov  
Model

**The text file:** I like spam. I like toast and spam.  
I eat ben and jerry's ice cream too.

For each word, keep track of the words that can follow it (and how often)

**The Model:**

I: like, like, eat	ben: and
like: spam., toast	jerry's: ice
spam.: I, I	ice: cream
toast: and	cream: too.
eat: ben	too.:
and: spam., jerry's	

- We can repeat words to indicate frequency
- Where to begin??

# 1<sup>st</sup> order Generative Markov Model

---

---

Technique for modeling any sequence of natural data

Each item depends ***on only the item immediately before it .***

A key benefit is that the model can ***generate*** feasible data!

**I like spam. I like spam. I like toast and jerry's ice cream too.**

## Generating text (1<sup>st</sup> order):

- 1) start with the first word in the file. Call it **w**
- 2) choose a word following **w**, at random. Call it **w**
- 3) choose a word following **w**, at random. And so on...

# HW7 Pr 2: Need to be able to...

---

---

Read text from a file

Compute and store the model

Generate the new text

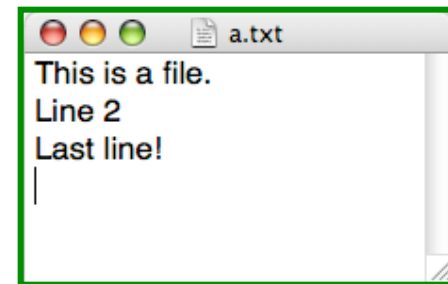
# Reading Files

---

---

In Python reading files is no problem...

```
>>> f = file( 'a.txt' )
```



```
>>> text = f.read()
```

```
>>> text
```

```
'This is a file.\nLine 2\nLast line!\n'
```

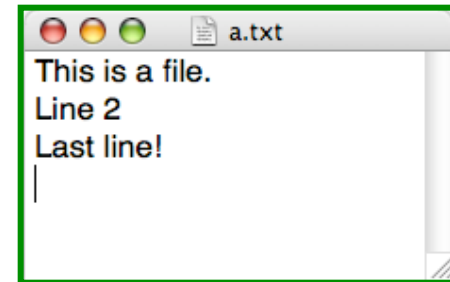
```
>>> f.close()
```

# Files

In Python reading files is no problem...

```
>>> f = file( 'a.txt' )
```

opens the file and calls it `f`



```
>>> text = f.read()
```

reads the whole file and calls it `text`

```
>>> text
```

```
'This is a file.\nLine 2\nLast line!\n'
```

```
>>> f.close()
```

`text` is a single string containing all the text in the file

But how to process the text from here...?

closes the file (closing Python does the same)

# String Manipulation

---

---

```
>>> text
'This is a file.\nLine 2\nLast line!\n'
>>> print text
This is a file.
Line 2
Last line!
```

*Returns a list of the words in the string  
(splitting at spaces, tabs and newlines)*

```
>>> text.split()
['This', 'is', 'a', 'file.', 'Line', '2', 'Last', 'line!']
>>> text
'This is a file.\nLine 2\nLast line!\n'
>>> lines = text.split('\n')
>>> lines
['This is a file.', 'Line 2', 'Last line!', '']
```

*Returns a list of the lines in the string  
(splitting at newlines)*

# Objects, objects, everywhere!

---

---

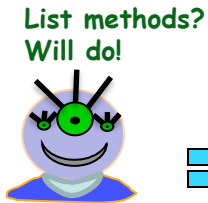
```
>>> L = []      # create a list, L
```

```
>>> dir(L)      # see all of L's methods
```

all list methods appear -- lots of them including **append**, **index**,  
**remove**, and **sort**

```
>>> help(L.sort)  # I wonder...
```

```
>>> help(L.index) # What does this do?
```



# List methods

---

---

not including list *operators*

```
>>> dir([])
```

```
append  
count  
extend  
index  
insert  
pop  
remove  
reverse  
sort
```

# String methods

---

---

not including string *operators*

```
>>> dir('')
```

```
capitalize  
center  
count  
find  
index  
isalpha  
lower  
replace  
split  
strip  
title  
upper  
and ~10 more...
```

**help** can help

but there's a fundamental difference... what and why?

# Mutable vs. immutable objects

---

---

Lists are *mutable* objects.

```
>>> L = [2,1,3]
>>> L.sort()
>>> L
[1,2,3]
```

no return value

L has changed.

Strings are *immutable* objects.

(So are numbers.)

```
>>> s = 'string'
>>> s.replace('st','')
'ring'
>>> s
'string'
```

returns a NEW string

s has NOT changed

# WMSCI 2005

## Router: A Methodology for the Typical Unification of Access Points and Redundancy

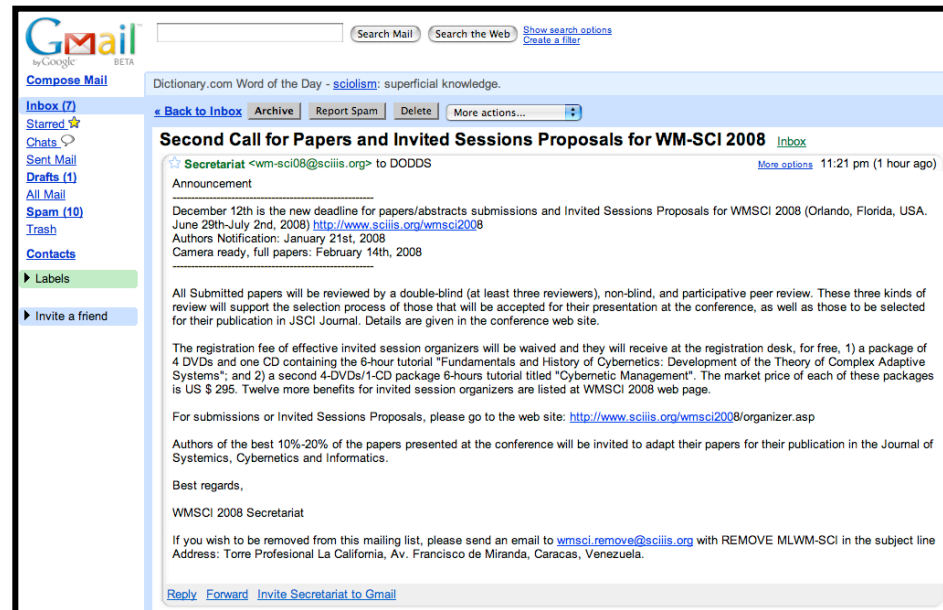
Jeremy Stribling, Daniel Aguayo and Maxwell Krohn



Randomly-generated submission  
accepted to WMSCI 2005

<http://pdos.csail.mit.edu/scigen/>

No end to the WMSCI emails...





# The Price Is Right!



Goal: Buy from a set of 5 items (as many of each as you want) while spending between \$9.25 and \$10.00.

# Demo



# Step 1: Identify Information To Store

---

---

- What information does this program need to keep track of?

# Step 1: Identify Information To Store

---

---

- How much has the user spent?  
`float: money`
- Which items are available?  
`list of strings: items`
- How much does each available item cost?  
`list of floats: prices`
- Which item did the user currently choose?  
`int: choice`
- How many of the currently chosen item does the user want?  
`int: number`

## Step 2: Break Down Functionality

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- What are the things that this program needs to do?

## Step 2: Break Down Functionality

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- Control the overall game play
- Prompt the user to enter a choice and number of items
- Calculate the total spent
- Figure out when the game is over
- Figure out win or lose
- Print a welcome message
- Remove the purchased item from the lists

## Attempt 1

```
def playTry1():
    print "Welcome to the price is right!"
    print "Your goal is to buy 5 or fewer items (any number of each)"
    print "and spend between $9.25 and $10"

    items = ["bleach", "coke", "ramen", "ice cream", "super ball"]
    prices = [1.35, .75, .25, 3.00, 1.75]
    money = 0.0

    while money < 9.25 and len(items) > 0:
        print "You have spent $", money
        printItems( items )
        choice = input( "Which item would you like to buy? " )
        number = input( "How many "+items[choice]+" would you like?" )
        print items[choice], "is $", prices[choice]
        money += prices[choice]*number

        prices = prices[0:choice] + prices[choice+1:]
        items = items[0:choice] + items[choice+1:]

    print "You have spent $", money
    if money >= 9.25 and money <= 10.0:
        print "You win!"
    else:
        print "You lose!"
```