

Today in CS 42

yes

Hw #10: Prolog

Coming up...

Monday 11/14: HW10 due (Prolog intro)

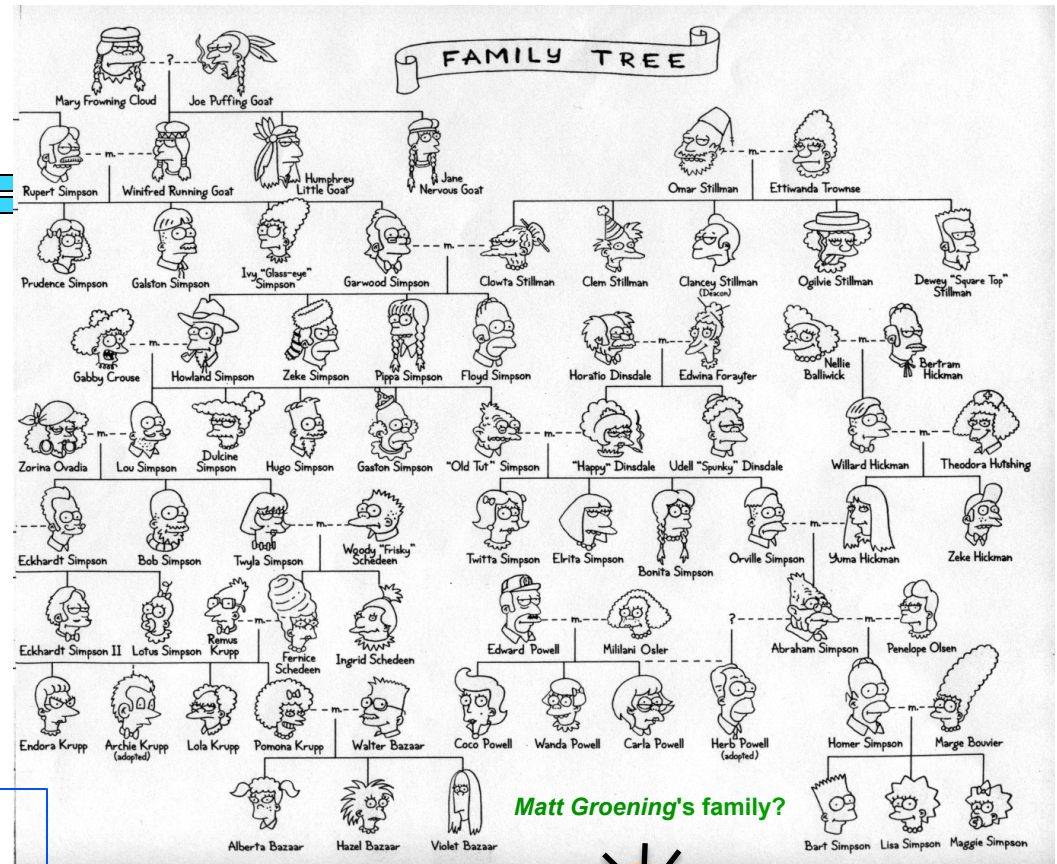
Thursday 11/18: **Midterm distributed**

Monday 11/21: **NO HW DUE**

Tuesday 11/22: **Midterm due**

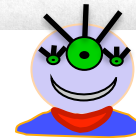
Thursday 11/24: Thanksgiving (no class)

Tuesday 11/29: HW11 due (Prolog games)



The Simpsons character names

Groening famously named the main Simpson characters after members of his own family: his parents, Homer and Margaret (Marge or Marjorie in full), and his younger sisters, Lisa and Margaret (Maggie).



[edit]

Review: Tail Recursion and Hmmm

```
(define (tower N)
  (tower-tr N 2))
```

Is tower-tr tail recursive?

A. Yes

```
(define (tower-tr N A)
  (if (= N 0)
```

B. No

A

C. Not sure

```
(power A (tower-tr (- N 1) A))))
```

Review: Tail Recursion and Hmmm

```
(define (power-tr b n A)
  (if (= n 0)
      A
      (power-tr b (- n 1) (* A b))))
```

Which is a "faithful" implementation of the Racket code above in HMMM?

- A. left side only
- B. right side only
- C. both
- D. neither

```
42 jeqz r2 46      42 jeqz r2 51
43 addn r2 -1     43 addn r2 -1
44 mul r3 r3 r1  44 mul r3 r3 r1
45 jump 42        45 storei r14 r15
46 mov r13 r3    46 addn r15 1
47 jumpi r14     47 call r14 42
                  48 addn r15 -1
                  49 loadi r14 r15
                  50 jumpi r14
                  51 mov r13 r3
                  52 jumpi r14
```

Big O comparison

Please do not try these at home!

Problem

Find the maximum element in a list

8	42	9	0
---	----	---	---

paranoid
algorithm

First, verify the $<$ operator with 2,000 known comparisons ($1 < 2$)

Second, look at each list element, compare it with the current max

-- Replace the current max if necessary.

As you do this, make each comparison 1,000 times just to “be sure”

You have a minimum-element finder already.

All elements start unmarked.

Find the smallest unmarked element and mark it.

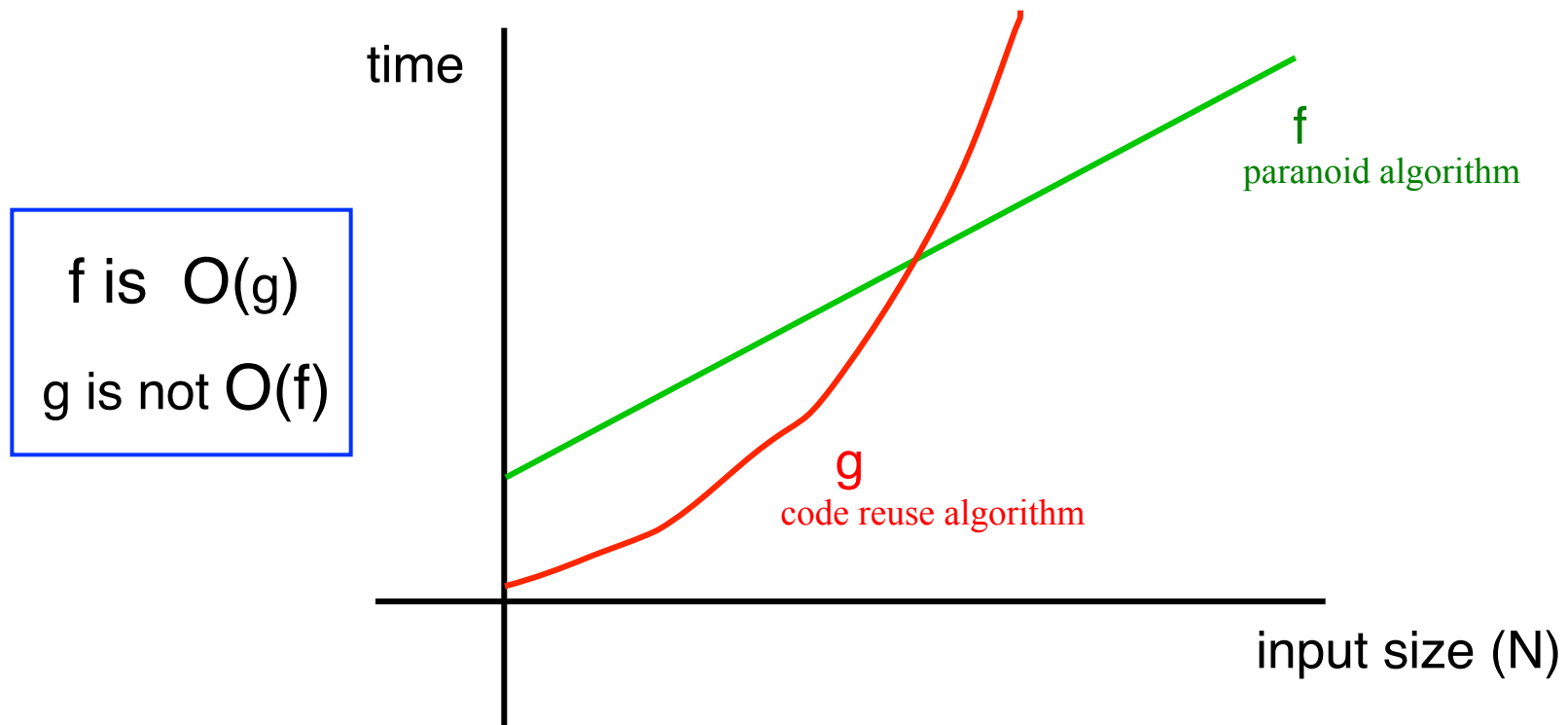
Repeat, keeping track of the last element marked each time.

When they're all marked, return the last element marked.

code reuse
algorithm

The Big Picture on “Big Oh”

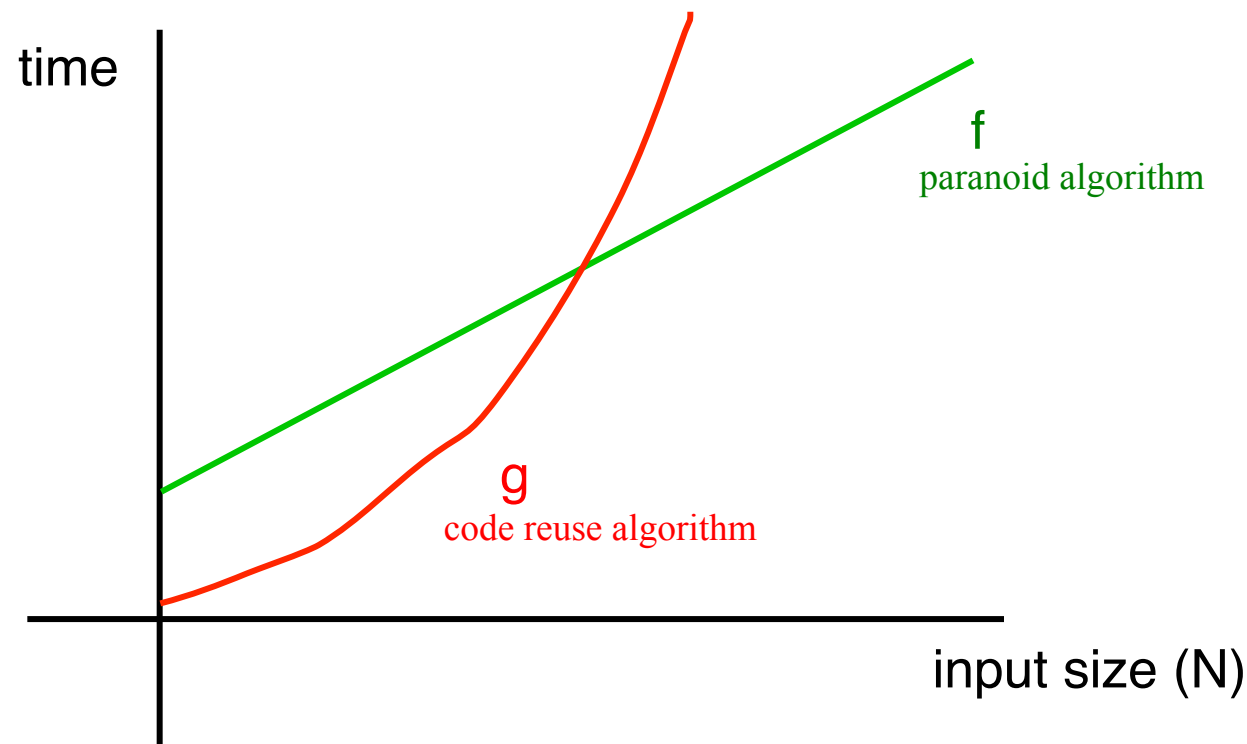
O (“Big Oh”) compares running times for algorithms



The Formal Definition of Big-O

$f(n)$ is $O(g(n))$ if there exists constants c and n_0 s.t.

$$f(n) \leq c * g(n) \text{ for all } n \geq n_0$$



Big O in practice

big-O = hand-waving math!

Ignore everything but the dominant term

← even there, ignore the constant

$$420n^2 + 3n^3 - 201$$

$$17 + 300\sqrt{n} + 0.5\log(n)$$

$$\frac{117}{n} + \frac{2^n}{3^n} + 1700$$

Big-O is simply an upper bound, but normally we want the **BEST** upper bound...

Review: Big-O

What is Big-O running time of the following mystery function? (and what does it do?)

```
(define (mystery N)
  (reverse (mystery-help N)))
```

```
(define (mystery-help N)
  (cond
    ((= N 0) '())
    ((= 1 (modulo N 2)) (cons 1 (mystery-help (/ (- N 1) 2))))
    (else (cons 0 (mystery-help (/ N 2))))))
```

A. $O(\log N)$ B. $O(N)$ C. $O(N \log N)$ D. All of these E. None of these

Midterm #2

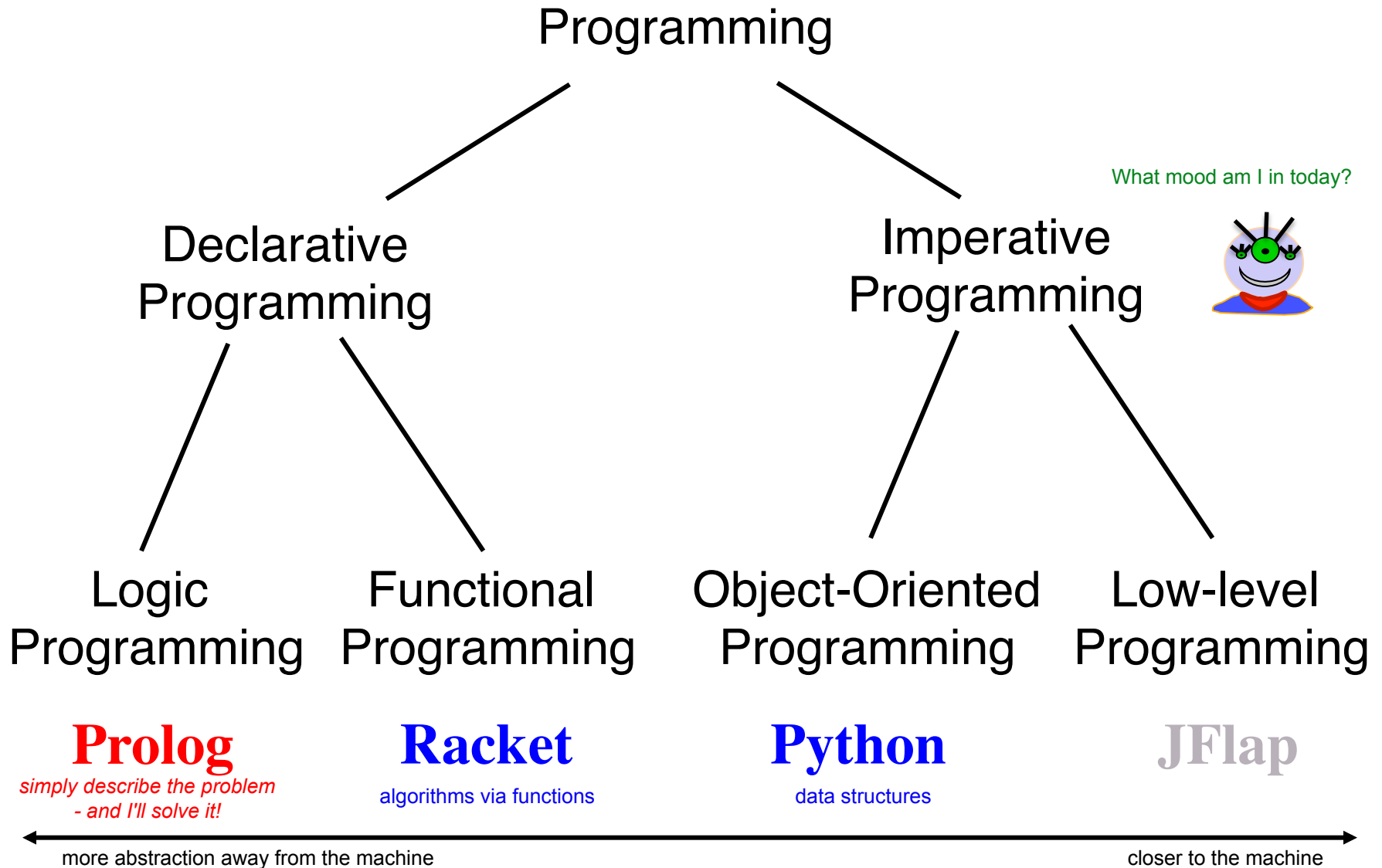
- Take home, distributed Thursday Nov 17
- Same ground rules as first midterm.
- Everything up through Prolog (this week) even if we only saw it in class.
including topics from before midterm 1
- Short reviews over the next two lectures
More review problems posted online soon



**Logic: another thing that
penguins aren't very good at.**

And now, for something
completely different...

Taxonomy of Programming Models



Prolog: The Dream

We feed Prolog a bunch of facts relevant to our problem

```
pairs(apple, walnut).      pairs(strawberry, honey).
pairs(apple, honey).      pairs(strawberry, ginger).
pairs(walnut, avocado).   pairs(strawberry, tea).
pairs(walnut, banana).    pairs(tea, walnut).
pairs(apple, banana).     pairs(tea, tomato).
pairs(banana, ginger).    pairs(tea, milk).
pairs(banana, cloves).
pairs(banana, strawberry). pairs(X,X).
pairs(banana, coriander). pairs(X, coconut).
```

We describe how to *recognize* a solution

```
yummy_triple(X,Y,Z) :- pairs(X,Y), X \= Y,
                        pairs(Y,Z), Y \= Z,
                        pairs(X,Z), X \= Z.
```

Prolog then finds solution(s) for us.

So buy now! <http://www.swi-prolog.org/>

Demo...

Prolog: Just the Facts!

```
%% Here is a comment in Prolog
/* this is also a comment */

chocolate_is_good.    %% A fact, but not in a very useful form

good(spam).    %% a debatable fact, but now prolog thinks so
good(42).    %% no one can deny this..

weird_list([3.14,42,spam,'+', "hi"]).    %% Well, I think so.

better(tofu, spam).    %% "tofu" is better than spam
better(chocolate, tofu).    %% "chocolate" is better than "tofu"
better(money, chocolate).    %% "money" is better than "chocolate"

%% Does prolog know that money is better than spam? Does prolog even
%% know what spam is??? NO!
```

Prolog can be alien...

prolog seems
reasonable to me!



- To run: `/opt/local/bin/swipl` (macs)
`swipl` (ssh to knuth.cs.hmc.edu server)
- To exit: `halt.`
- To (re)load a file: `[file].` or `reconsult('file.pl').` [user]. lets you type facts
- The Prolog environment is for queries only!
Use your favorite editor to change files... Windows's `swipl` has an editor built-in.

```
parent(homer,bart).  
parent(homer,lisa).  
parent(marge,bart).  
parent(marge,lisa).  
child(A,B) :- parent(B,A).
```

FACTS

RULES

some facts and rules from the file `simpsons.pl`

```
?: parent(homer,lisa).  
yes TEST  
  
?: parent(X,bart).  
X = homer ; GENERATE  
X = marge ;  
no
```

queries within the Prolog environment

Prolog syntax is the stranger



you mean L'Étranger...

The idea:

Provide data/relationships that describe the world. Then ask questions.

Relationships:

mother(X, Y) :- parent(X, Y), female(X).

colon-hyphen means "IF"

variables always start with a capital letter

commas mean "AND"

child(X, Y) :- parent(Y, X).

predicates and constants start with a lowercase letter

ancestor(X, Y) :- parent(X, Y).

ancestor(X, Y) :- parent(X, Z), ancestor(Z, Y).

these relationships are **predicates** not functions. They *have* a value, but **they do not return a value!**

multiple rules express "OR" ; also means "OR"

recursion welcome!

File simpsons.pl

```
/*
 * the parent predicate
 */

parent(olf, skug).
parent(helga, skug).
parent(skug, esmerelda).
parent(skugerina, esmerelda).
parent(esmerelda, klotho).
parent(gemini, klotho).
parent(esmerelda, atropos).
parent(gemini, atropos).
parent(esmerelda, lachesis).
parent(gemini, lachesis).
parent(olf, homericus).
parent(helga, homericus).
parent(ug, matilda).
parent(uggette, matilda).
parent(homericus, homer).
parent(matilda, homer).
parent(homericus, gomer).
parent(matilda, gomer).
parent(homer, bart).
parent(marge, bart).
parent(homer, lisa).
parent(marge, lisa).
parent(homer, maggie).
parent(marge, maggie).
parent(john, marge).
parent(jackie, marge).
parent(john, selma).
parent(jackie, selma).
parent(john, patty).
parent(jackie, patty).
parent(john, glum).
parent(jackie, glum).
parent(glum, millhouse).
parent(cher, millhouse).
parent(glum, wentworth).
parent(cher, wentworth).
```

```
/*
 * the age predicate
 */

age(helga, 97).
age(olf, 99).
age(uggette, 93).
age(ug, 92).
age(matilda, 65).
age(homericus, 76).
age(skugerina, 101).
age(skug, 78).
age(esmerelda, 55).
age(gemini, 54).
age(klotho, 20).
age(atropos, 19).
age(lachesis, 18).
age(marge, 35).
age(homer, 38).
age(lisa, 8).
age(maggie, 1).
age(bart, 10).
age(gomer, 41).
age(john, 62).
age(jackie, 59).
age(patty, 38).
age(selma, 38).
age(glum, 27).
age(cher, 44).
age(millhouse, 8).
age(wentworth, 8).
```

```
/*
 * the female predicate
 */
```

```
female(helga).
female(esmerelda).
female(skugerina).
female(uggette).
female(matilda).
female(marge).
female(jackie).
female(selma).
female(patty).
female(cher).
female(lisa).
female(maggie).
female(klotho).
female(atropos).
female(lachesis).
```

```
/*
 * the male predicate
 */
```

```
male(olf).
male(skug).
male(homericus).
male(ug).
male(homer).
male(gomer).
male(gemini).
male(john).
male(glum).
male(bart).
male(millhouse).
male(wentworth).
```

```
/*
 * Here are three rules about families
 */
```

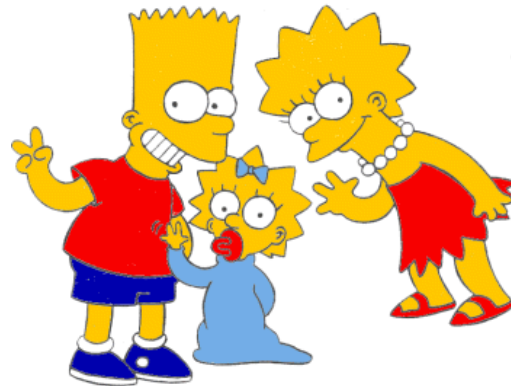
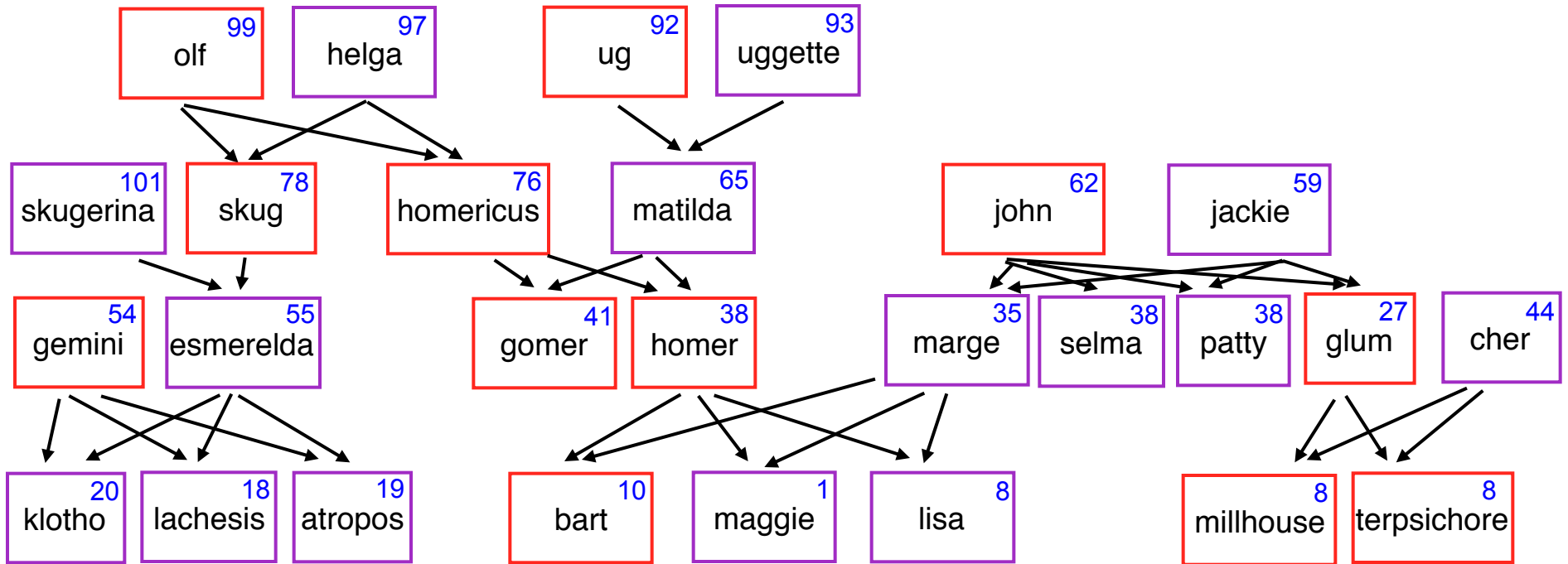
```
child(X, Y) :- parent(Y, X).
```

```
mother(X, Y) :- female(X), parent(X, Y).
```

```
anc(X, Y) :- parent(X, Y).
```

```
anc(X, Y) :- parent(Z, Y), anc(X, Z).
```

A more complete picture ...



The idea:

Provide data/relationships that describe the world. Then ask questions.

Questions:

`child(lisa,marge).`

Is Lisa a child of Marge?

`parent(marge,X).`

Who has Marge as a parent?

Is Ug a parent of Bart?

Who are the ancestors of Lisa?

Who are uggette's descendants?

Who is who's parent?

Who are John's grandchildren?

Name:

“Quiz”

Write these three family-relationship predicates in prolog:

sibs (X, Y)

true if X and Y are siblings

aunt (A, N)

true if A is N's aunt

rel (X, Y)

true if X and Y are related (by blood)

Name:

“Quiz”

Are these definitions correct? A. Yes B. No

sibs (X, Y) true if X and Y are siblings

`sibs (X, Y) :- parent (A,X) , parent (A,Y) .`

aunt (A, N) true if A is N's aunt

`aunt (X, Y) :- parent (Q, N) , sibs (Q, A) , female (A) .`

rel (X, Y)
true if X and Y are related (by blood)

`rel (X, Y) :- anc (Z, X) , anc (Z, Y) .`

What's wrong here?

```
sibs (X, Y) :- parent (A, X),  
                parent (A, Y),  
                X \== Y.
```

Nothing is wrong...

What's wrong here?

```
sibs (X, Y) :- parent (A, X),  
                parent (A, Y),  
                X \== Y.
```

Nothing **IS** wrong...

setof

?- setof(A,aunt(A,bart),S).

?- setof(N,aunt(marge,N),S).

$\text{setof}(R, p(R), S)$

is true when S is the set (list) of R s that satisfy predicate p .

trace. / notrace. / debug. / nodebug.

spy(female).

nospall.

Prolog is DFS

Maybe this should be Prolog == DFS?



Who are Bart's aunts?

`aunt(A, bart)`

`aunt(A,N) :- parent(P,N), sibling(A,P), female(A).`

`N = bart`

`parent(P,N)`

is there a parent?
`parent(homer, bart)`
YES `N = bart`
`P = homer`

other parents?
`parent(marge, bart)`
YES `N = bart`
`P = marge`

backtrack!

`sibling(A,P)`

is there a sibling?
`sibling(gomer, homer)`
YES `N = bart`
`P = homer`
`A = gomer`

other siblings?
NO

is there a sibling?
`sibling(glum, marge)`
YES `N = bart`
`P = marge`
`A = glum`

other siblings?
`sibling(selma, marge)`
YES `N = bart`
`P = marge`
`A = selma`

backtrack!

backtrack!

`female(A)`
`female(gomer) ?`
NO (fails)

`female(glum) ?`
NO

`female(selma)`
SUCCESS
YES!

Prolog: The Dream

We feed Prolog a bunch of facts relevant to our problem

```
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pairs(apple, honey).      pairs(strawberry, ginger).
pairs(walnut, avacado).   pairs(strawberry, tea).
pairs(walnut, banana).   pairs(tea, walnut).
pairs(apple, banana).    pairs(tea, tomato).
pairs(banana, ginger).   pairs(tea, milk).
pairs(banana, cloves).
pairs(banana, strawberry). pairs(X,X).
pairs(banana, coriander). pairs(X, coconut).
```

We describe how to *recognize* a solution

```
yummy_triple(X,Y,Z) :- pairs(X,Y), X \= Y,
                        pairs(Y,Z), Y \= Z,
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```

Prolog then finds solution(s) for us.

So buy now! <http://www.swi-prolog.org/>

Demo...

Prolog: The Reality

We feed Prolog a bunch of facts relevant to our problem

```
pairs(apple, walnut).           pairs(X,X).
pairs(apple, honey).           pairs(X, coconut).
pairs(walnut, avocado).
pairs(walnut, banana).         pairs(X,Y) :- pairs(Y,X).
%% etc.
```

We describe how to *recognize* a solution

```
yummy_triple(X,Y,Z) :- pairs(X,Y), X \= Y,
                        pairs(Y,Z), Y \= Z,
                        pairs(X,Z), X \= Z.
```

Prolog then finds solution(s) for us?

In practice, you have to think hard about DFS...

Infinite loop Demo...

Prolog: The Reality (2)

We feed Prolog a bunch of facts relevant to our problem

```
pairs(X,Y) :- pairs(Y,X).      pairs(apple, walnut).
                                pairs(apple, honey).
pairs(X,X).                    pairs(walnut, avocado).
pairs(X, coconut).            pairs(walnut, banana).
                                %% etc.
```

We describe how to *recognize* a solution

```
yummy_triple(X,Y,Z) :- pairs(X,Y), X \= Y,
                        pairs(Y,Z), Y \= Z,
                        pairs(X,Z), X \= Z.
```

Prolog then finds solution(s) for us?

In practice, you often have to think hard about DFS...

Infinite Loop Demo...