

# CS 133: Databases

Fall 2019  
Lec 22 – 11/26  
Database Design  
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## Warm-up Exercise

(See exercise sheet. You can start before class.)

Given:  $X \rightarrow Y$  and  $YW \rightarrow Z$

$XW \rightarrow YW$  (augmentation)  
 $XW \rightarrow Z$  (transitivity)

## Rules of Inference

- **Armstrong's Axioms** ( $X, Y, Z$  are sets of attributes):
  - Reflexivity: If  $Y \subseteq X$ , then  $X \rightarrow Y$
  - Augmentation: If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$  for any  $Z$
  - Transitivity: If  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$
- Some additional rules (that follow from **AA**):
  - Union: If  $X \rightarrow Y$  and  $X \rightarrow Z$ , then  $X \rightarrow YZ$
  - Decomposition: If  $X \rightarrow YZ$ , then  $X \rightarrow Y$  and  $X \rightarrow Z$
  - Pseudo-transitivity: If  $X \rightarrow Y$  and  $YW \rightarrow Z$ , then  $XW \rightarrow Z$

## Goals for Today

- Learn how to decompose a relation to adhere to Boyce-Codd Normal Form (BCNF)
- Understand lossy vs. loss-less decompositions
- Reason about issues that can result even if a decomposition is loss-less

## The Issue with Non-Key FDs

- Why does the FD  $rating \rightarrow hourly\_wages$  yield redundancy issues?

S	N	L	R	W	H
123-22-3666	Attishoo	48	8	10	40
231-31-5368	Smiley	22	8	10	30
131-24-3650	Smethurst	35	5	7	30
434-26-3751	Guldu	35	5	7	32
612-67-4134	Madayan	35	8	10	40

Hourly\_Emps

- $Rating$  is a **non-key field**, so there could be **duplicate pairs** of particular  $\{rating, hourly\_wages\}$  in this relation
- By separating  $\{rating, hourly\_wages\}$  into its own relation, we resolve redundancy!
  - Can regain the original data via **natural join**

## “Normal” Forms for a Schema

- Idea*: decompose relation into two or more relations to remove redundancy. Decomposition **guided by FDs!**
- Boyce-Codd Normal Form (BCNF)**
  - Adhere to simple conditions and anomalies caused by data redundancy cannot occur
- BCNF definition: A Relation  $R$  with FDs  $F$  is in BCNF if, **for all  $X \rightarrow A$  in  $F^+$** 
  - $A \in X$  (a trivial FD), or
  - $X$  is a **superkey for  $R$**
- I.e.:  $R$  is in BCNF if the **only non-trivial FDs over  $R$  are key constraints**

Each tuple in  $R$  is an entity or relationship **identified by a key and described by other attributes**

## Problems with Decompositions

- There are three potential problems to consider:
  - May be **impossible to reconstruct the original relation!** (**Lossiness**)
  - Checking functional dependencies may require joins
  - Some queries become more expensive due to joins
    - e.g., *How much does Smiley earn?*

S	N	L	R	H	R	W
123-22-3666	Attishoo	48	8	40	8	10
231-31-5368	Smiley	22	8	30	5	7
131-24-3650	Smethurst	35	5	30		
434-26-3751	Guldu	35	5	32		
612-67-4134	Madayan	35	8	40		

Hourly\_Emps2

Wages

**Lossiness (#1) cannot be allowed**  
 #2 and #3 are design tradeoffs  
 Must consider these issues vs. redundancy

## Lossy vs. Lossless Decomposition

- Example schema: Oversees(**ProjectId**, **EmployeeId**, **DepartmentId**)
- FDs:
  - $E \rightarrow P$  (an employee oversees only one project)
  - $D \rightarrow P$  (a dept works on only one project)
  - $E \rightarrow D$  (an employee only works with one dept for these projects)
- Example instance of Oversees:

Project	Employee	Department
Comet	Alice	Physics
Comet	Bob	Astronomy
Genomics	Carl	Biology
Genomics	Denise	Biology

**Redundancy?**

## Lossy vs. Lossless Decomp (cntd)

- Redundancy with the FD  $D \rightarrow P$

Project	Employee	Department
Comet	Alice	Physics
Comet	Bob	Astronomy
Genomics	Carl	Biology
Genomics	Denise	Biology

- Proposed decomposition:

Project	Employee
Comet	Alice
Comet	Bob
Genomics	Carl
Genomics	Denise

Department	Project
Physics	Comet
Astronomy	Comet
Biology	Genomics

## Lossy vs. Lossless Decomp (cntd)

- Redundancy with the FD  $D \rightarrow P$

Project	Employee
Comet	Alice
Comet	Bob
Genomics	Carl
Genomics	Denise



Department	Project
Physics	Comet
Astronomy	Comet
Biology	Genomics

Project	Employee	Department
Comet	Alice	Physics
Comet	Alice	Astronomy
Comet	Bob	Physics
Comet	Bob	Astronomy
...	...	...

← Tuples not in original!

## Lossy vs. Lossless Decomp (cntd)

- Decomposition attempt #2, for FD  $D \rightarrow P$ :

Department	Employee
Physics	Alice
Astronomy	Bob
Biology	Carl
Biology	Denise



Department	Project
Physics	Comet
Astronomy	Comet
Biology	Genomics

Project	Employee	Department
Comet	Alice	Physics
Comet	Bob	Astronomy
Genomics	Carl	Biology
Genomics	Denise	Biology

## Loss-less Decomposition

- Decomposition of R into X and Y is *lossless-join* w.r.t. a set of FDs F if, for every instance r that satisfies F:

$$\pi_X(r) \bowtie \pi_Y(r) = r$$

- Decomposition of R into X and Y is *lossless with respect to F* if and only if  $F^+$  contains:

$$X \cap Y \rightarrow X, \text{ or } X \cap Y \rightarrow Y$$

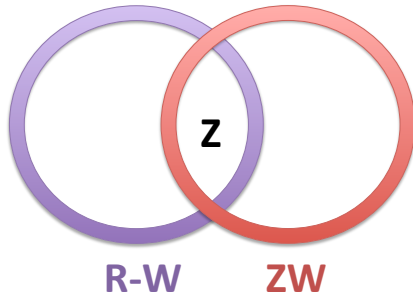
In other words, the common attributes form a key for X or Y

**Corollary:** If  $Z \rightarrow W$  holds over R and  $Z \cap W$  is empty, then decomposition of R into  $ZW$  and  $R - W$  is loss-less.

- In "Oversees" example, decomposing into {E,P} and {D,P} is *lossy* because the intersection (i.e., **Project**) is not a key of either resulting relation

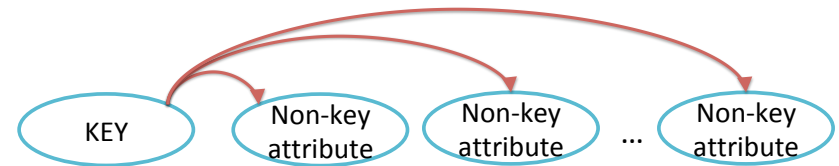
## Loss-less Decomposition into BCNF

- Relation R has FDs F. If  $Z \rightarrow W$  in F violates BCNF:
  - decompose R into **R - W** and **ZW** (guaranteed to be loss-less)



## Reasoning about BCNF

- Relation R with FDs F is in BCNF if, **for all  $X \rightarrow A$  in  $F^+$** 
  - $A \in X$  (a trivial FD), or
  - X is a superkey for R**



Also recall that relations are sets of tuples

## Reasoning about BCNF

- If relation R is in BCNF, then each field of a tuple provides a fact **that cannot be inferred using FDs alone**

- Suppose we are told that the FD  $X \rightarrow A$  holds for this relation:

X	Y	A
x	y1	a
x	y2	?

Possible to guess the value of the missing attribute!

We can infer missing value using the FD... this relation is *not* in BCNF.

## Example 1: Is Hourly\_Emps in BCNF?

### Hourly\_Emps

S	N	L	R	W	H
123-22-3666	Attishoo	48	8	10	40
231-31-5368	Smiley	22	8	10	30
131-24-3650	Smethurst	35	5	7	30
434-26-3751	Guldu	35	5	7	32
612-67-4134	Madayan	35	8	10	40

- SNLRWH has FDs

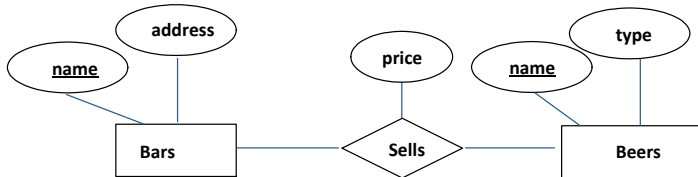
$S \rightarrow SNLRWH$

$R \rightarrow W$

In BCNF??

## Example 2: Is Bar\_Sells in BCNF?

- Combing Bars and Sells  
**Bar\_Sells** (bar\_name, beer\_name, address, price)



- FDs (for just Bar\_Sells):  
 bar\_name → address  
 bar\_name, beer\_name → price

In BCNF??  
(Exercise 2)

## Examples: BCNF Decomposition

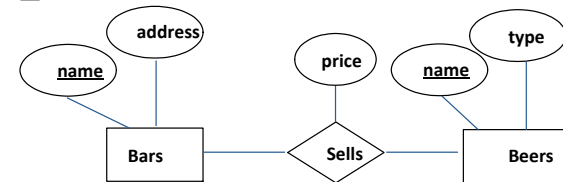
- Hourly\_Emps

S	N	L	R	H
123-22-3666	Attishoo	48	8	40
231-31-5368	Smiley	22	8	30
131-24-3650	Smethurst	35	5	30
434-26-3751	Guldu	35	5	32
612-67-4134	Madayan	35	8	40

R	W
8	10
5	7

Wages

- Bar\_sells



Hourly\_Emps2

Bars(bar\_name, address)      Sells(bar\_name, beer\_name, price)

## Transitive Dependencies

- Violating FD involves *attribute(s) depending on non-key attribute(s)*

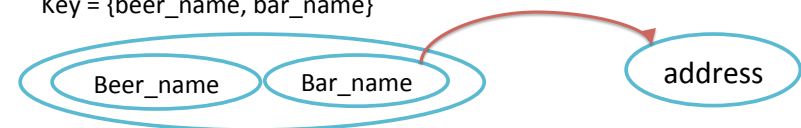


Hourly\_Emps violating FD: R → W

## Partial Dependencies

- Violating FD involves *attribute(s) depending on attribute(s) that are proper subset of a key*

Key = {beer\_name, bar\_name}



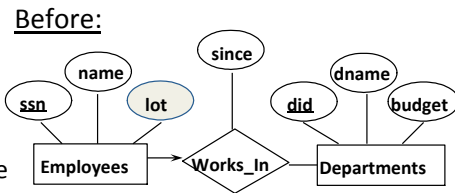
Bar\_sells violating FD: bar\_name → address

## Refining an ER Diagram

- 1st diagram becomes:

**Workers(S,N,L,D,Si)**  
**Departments(D,M,B)**

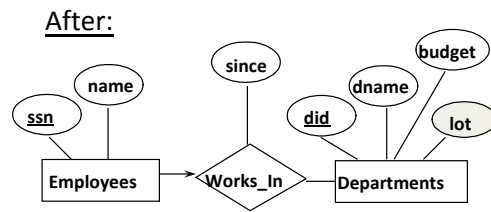
- Lots associated w/ workers



- Suppose all workers in a dept are assigned the same lot:  $D \rightarrow L$

- Redundancy; fixed by:

**Workers2(S,N,D,Si)**  
**Dept\_Lots(D,L)**  
**Departments(D,M,B)**



- Can fine-tune this:  
**Workers2(S,N,D,Si)**  
**Departments(D,M,B,L)**

## Repeated Decomposition

- Repeated decomposition**

- May be needed to get set of relations that are in **BCNF**
- Can confirm BCNF for original relation  $R$  using only FDs  $F$ , but *each decomposed relation*  $R_i$  must be checked for violating each [relevant] FD in  $F^+$

- Using *attribute closure* to check decomposed  $R_i$

- To confirm  $R_i$  is in BCNF: for each subset of attributes  $\alpha$  in  $R_i$ , check that  $\alpha^+$  (under  $F$ ):
  - Contains no attributes of  $R_i - \alpha$ , *or*
  - Contains all attributes of  $R_i$

## Exercise 3: BCNF Decomposition

- Candidate key={id, advisorId}
- FD violation? Both!
- Decomposed into three relations:
  - $R_1 = \{id, name, dorm\}$
  - $R_2 = \{advisorId, advisorName\}$
  - $R_3 = \{id, advisorId\}$

## An Aside: *Multiple Candidate Keys*

- For relation **Bars(bar\_name, address)**, suppose we knew:
  - $bar\_name \rightarrow address$
  - $address \rightarrow bar\_name$

Either attribute could serve as primary key!

- When creating a relation in SQL, use *one* candidate key as the primary key
  - Enforce others using UNIQUE key word
  - Commonly used when use *surrogate key* as a primary key

## Dependency Preservation

- Decomposed example from “Oversees”:
  - $E \rightarrow P$  (an employee oversees only one project)
  - $D \rightarrow P$  (a dept works on only one project)
  - $E \rightarrow D$  (an employee only works with one dept for these projects)

Project	Department
Comet	Physics
Comet	Astronomy
Genomics	Biology

Department	Employee
Physics	Alice
Astronomy	Bob
Biology	Carl
Biology	Denise

- How can we check  $E \rightarrow P$  ??  
(an employee oversees only one project)

## Dependency Preserving Decomposition

- Dependency preserving decomposition** (Intuition):
  - If  $R$  is decomposed into  $X$ ,  $Y$  and  $Z$ , and we enforce the FDs that hold individually on  $X$ ,  $Y$ , and  $Z$
  - then all FDs that were given to hold on  $R$  must also hold
- The **projection of  $F$  on attribute set  $X$**  (denoted  $F_X$ ):
  - The set of FDs  $U \rightarrow V$  in  $F^+$  (closure of  $F$ , not just  $F!$ ) such that all of the attributes on both sides of the FD **are in  $X$**
  - That is:  $U$  and  $V$  are subsets of  $X$

## Dependency Preserving Decompositions (Contd.)

- Decomposition of  $R$  into  $X$  and  $Y$  is **dependency preserving** if  $(F_X \cup F_Y)^+ = F^+$ 
  - i.e., we can check FDs on  $X$  and  $Y$  independently
- “Oversees” example, continued:
  - $X = \{\text{Employee, Department}\}$ ,  $F_X = \{E \rightarrow D\}$
  - $Y = \{\text{Project, Department}\}$ ,  $F_Y = \{D \rightarrow P\}$
  - Does  $(F_X \cup F_Y)^+$  include  $E \rightarrow P$ ?

**YES!** (transitive property)

## Exercise 4: Movie showings

- {movie, city} and {movie, theater}
- After decomposing on Theater  $\rightarrow$  city, can't preserve the FD movie, city  $\rightarrow$  theater

## Movie showings: decomposition issue

- Showings (movie, theater, city)
- FDs:
  - movie, city  $\rightarrow$  theater
  - theater  $\rightarrow$  city
- Decompose on theater  $\rightarrow$  city:

Theater	City
ArcLight	Pasadena
iPic	Pasadena



Theater	Movie
ArcLight	The Martian
iPic	The Martian

Theater	City	Movie
ArcLight	Pasadena	The Martian
iPic	Pasadena	The Martian

Above decomposition could allow this to happen!

Violates FD  
movie, city  $\rightarrow$  theater

## Third Normal Form (3NF)

- Definition: for all  $X \rightarrow A$  in  $F^+$ 
  - $A \in X$  (called a trivial FD), or
  - $X$  is a superkey for  $R$ , **OR**
  - $A$  is a *part of some candidate key* for  $R$
- Allows FDs like non-key  $\rightarrow$  partial key
- 3NF but not BCNF?
  - have overlapping composite candidate keys

A is called a  
prime attribute

Always possible to get a loss-less, dependency-preserving decomposition into 3NF!

(may contain redundancy)

## Alternate Formulation of 3NF & BCNF

BCNF change

Every ~~non-key~~ attribute must describe *a fact* about "the key, the whole key, and *nothing but the key*, so help me Codd"

(1<sup>st</sup> Normal Form)  
(2<sup>nd</sup> Normal Form)  
(3<sup>rd</sup> Normal Form)

- Normal forms increasingly restrictive
  - 1<sup>st</sup> NF  $\supset$  2<sup>nd</sup> NF  $\supset$  3<sup>rd</sup> NF  $\supset$  Boyce-Codd NF