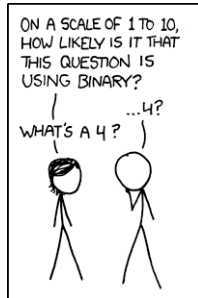


CS 101 Today



My top-10 list of binary jokes...

Read Sections 4.1 to 4.2.2

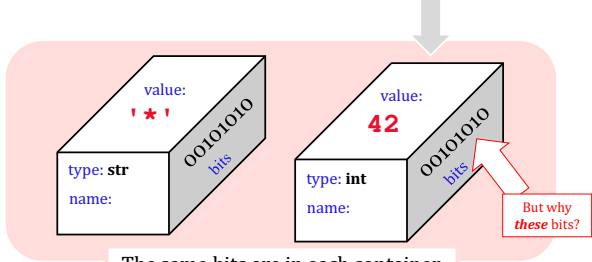
Looking Back
Computing as composition
clay == functions

Looking Forward
Computing as representation
clay == data & bits

Binary Storage & Representation

Binary	Dec	Hex	Glyph
0010 0000	32	20	(blank) (sp)
0010 0001	33	21	!
0010 0010	34	22	"
0010 0011	35	23	#
0010 0100	36	24	\$
0010 0101	37	25	%
0010 0110	38	26	&
0010 0111	39	27	'
0010 1000	40	28	(
0010 1001	41	29)
0010 1010	42	2A	*
0010 1011	43	2B	+

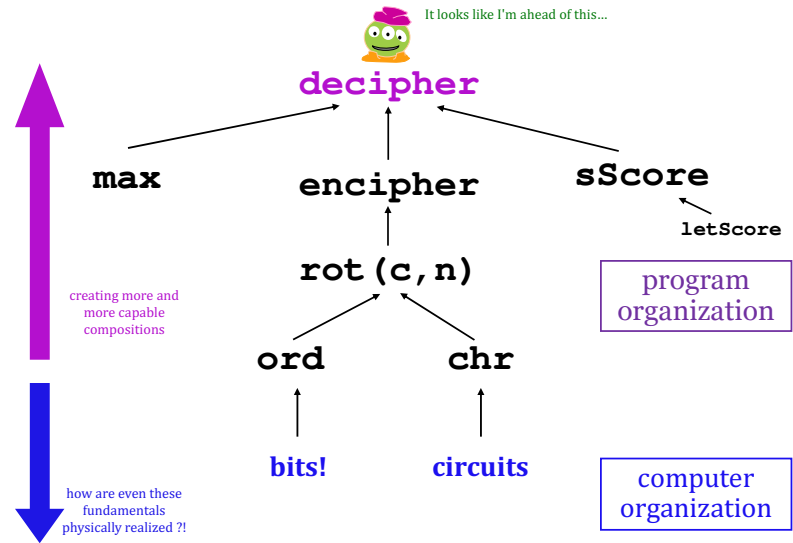
8 bits = 1 byte = 1 box



The same bits are in each container.

The SAME bits can represent different pieces of data, depending on **type**

Some legs to stand on!



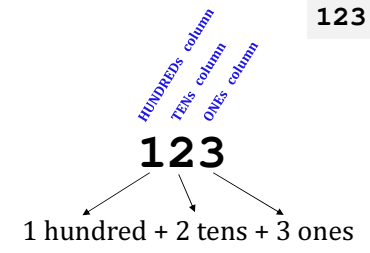
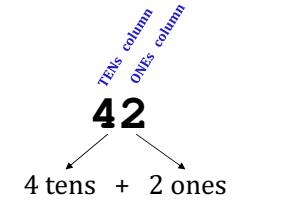
Base 2

each column represents the base's next power



Write 123 in binary...

Base 10



base 1 digits: 1

Beyond Binary

base 2 — 101010 digits: 0, 1

base 3 — 1120 digits: 0, 1, 2

- base 4
- base 5
- base 6
- base 7
- base 8
- base 9
- base 10
- base 11
- base 12
- ...
- base 16

Which of these *isn't* 42...?
222 **60** **54** **46** **39**
 and what are the *bases* of the rest?

42 digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9

base 1 digits: 1

base 2 — 101010 digits: 0, 1

base 3 — 1120 digits: 0, 1, 2

base 4 — 222 digits: 0, 1, 2, 3

base 5 — 132 digits: 0, 1, 2, 3, 4

base 6 — 110 digits: 0, 1, 2, 3, 4, 5

base 7 — 60 digits: 0, 1, 2, 3, 4, 5, 6

base 8 — 52 digits: 0, 1, 2, 3, 4, 5, 6, 7

base 9 — 46 digits: 0, 1, 2, 3, 4, 5, 6, 7, 8

base 10 — 42 digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9

base 11 — 39 digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A

base 16 — 2A Hexadecimal digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F

All 42s!

Two symbols is easiest!

A computer has to differentiate *physically* among all its possibilities.



ten symbols ~ ten different voltages



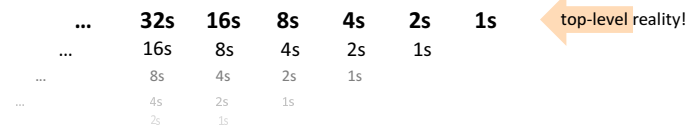
two symbols ~ two different voltages



What digits are these?

Easy!

Extra! Can you figure out the **last binary digit** (bit) of **53** without determining any other bits? The last **two**? **3**? All?



53

in the end, we need "53"-worth of value

Lab 4: Computing in binary



```
def numToBinary(N):
    if N == 0:
        return ''
    elif N%2 == 0:
        return numToBinary(N//2) + '0'
    else:
        return numToBinary(N//2) + '1'
```

Annotations for the code:

- empty string means 0 (pointing to the return '' line)
- If N is even, what is the final bit? (pointing to the '0' in the elif branch)
- If N is odd, what is the final bit? (pointing to the '1' in the else branch)
- How much VALUE is left to convert!? (pointing to the N//2 in the recursive calls)

Reasoning, bit by bit



left-shift by 1

```
11 3 << 1
110 6
```

What does *left-shifting* do to the **value** of a #?

left-shift by 2

```
11 3 << 2
1100 12
```

right-shift by 2

```
101010 42 >> 2
1010 10
```

What does *right-shifting* do to the **value** of a #?

Reasoning, bit by bit



and (both) **&** | or (either)

bitwise and

```
5: 101
6: 110
& 100
4
```

bitwise and

```
11: 1011
5: 0101
&

```

bitwise or

```
5: 101
6: 110
| 111
7
```

bitwise or

```
11: 1011
5: 0101
|

```

Being bit-wise

Try these for a bit...

```
7 << 1
5 << 4
170 >> 2
```

Annotations: "You don't need to convert to binary for these three..." (pointing to the first three lines), "left-shift" (pointing to the first two lines), "right-shift" (pointing to the third line).

```
14: 1110
9: 1001
14 | 9
14 & 9
```

Annotations: "You do need to use binary for these two!" (pointing to the first two lines), "or" (pointing to the third line), "and" (pointing to the fourth line).

In processors **shifts, ands, ors, adds, and subtractions** are *very fast*, whereas **multiplying, dividing, and mod** are relatively *slow*.

Given this, what is a way to compute these expressions using *only fast* operations, maybe in combination?

- N//4
- N*7
- N*17
- N%16 (extra sneaky!)

Intel x86 processor instructions
and their speeds (2014)

Table C-16. General Purpose Instruction:

Instruction	Latency ¹		Throughput
	OF_3H	OF_3H	
CPUID			
ADC/SBB reg, reg	8		3
ADC/SBB reg, imm	8		2
ADD/SUB	1		0.5
AND/OR/XOR	1		0.5
BSF/BSR	16		2
BSWAP	1		0.5
BTC/BTR/BTS	8-9		1
CLI			
CMP/TEST	1		0.5
DEC/INC	1		0.5
IMUL r32	10		1
IDIV MOD is the same	66-80		30

In processors **shift, and, or, add, and subtract** are ***much faster*** than **multiply, divide, and mod**, which are ***relatively slow***.

Given this, what is a way to compute these statements using combinations from only the ***fast*** operations above?

- $N/4 \Rightarrow N \gg 2$
- $N*7 \Rightarrow$
- $N*17 \Rightarrow$
- $N\%16 \Rightarrow$

Name(s): _____

Quiz

In binary, I'm an 11-eyed alien!



Convert these two binary numbers *to decimal*:

32 16 8 4 2 1
110011

10001000

Convert these two decimal numbers *to binary*:

32 16 8 4 2 1

28₁₀

101₁₀

Add these two binary numbers:

$$\begin{array}{r} 101101 \\ + 1110 \\ \hline \end{array}$$

Multiply these binary numbers:

$$\begin{array}{r} 101101 \\ * 1110 \\ \hline \\ + \\ \hline \end{array}$$

WITHOUT
converting
to decimal !

$$\begin{array}{r} 1 \\ 529 \\ + 742 \\ \hline 1271 \end{array}$$

Hint: Remember these algorithms? They're the same in binary!

$$\begin{array}{r} 529 \\ * 42 \\ \hline 1058 \\ + 2116 \\ \hline 22218 \end{array}$$



Extra! Can you figure out the last binary digit (bit) of 53 *without determining any other bits*? The last two? 3?