

# The CS 5 Post

## ALIEN INVASION!!!

Claremont (AP): A party at a private college here was disrupted when uninvited aliens burst through the gates.

“Every year, we celebrate *Long Tall Penguins*,” explained an angry student. “We get together, dress like the stuffiest professors, and chip bits off an iceberg to cool our drinks. This year, just as we were about to chill the mackerel, two strange alien creatures ran into the courtyard, picked everyone up, and took turns stacking us in piles.”

But another student claimed that the aliens were just misunderstood. “They love to play Connect 4, and since we were wearing black and white clothes, they thought we were playing pieces. They stacked us up in a 5-ply lookahead formation. It was fun!”

According to police, no charges will be filed because the aliens are not subject to Solar jurisdiction.



CS 5 today:

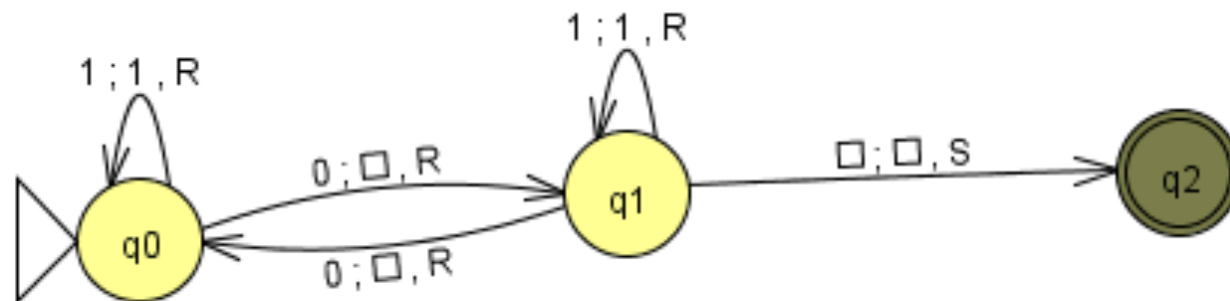
more machines!

Final ideas...

Turing Machines and the **MANY** things computers can't compute...  
!



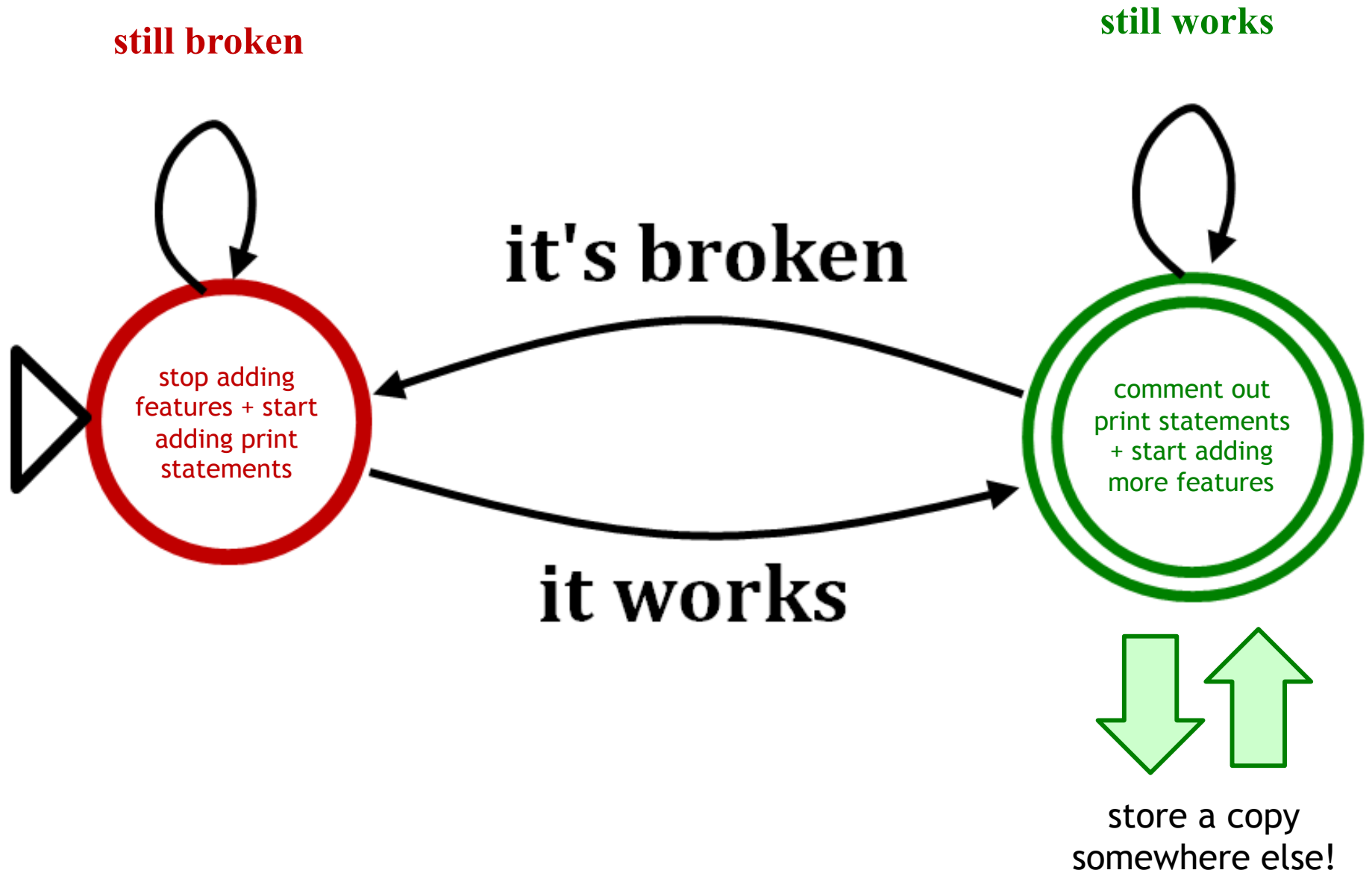
This machine doesn't look all-powerful to me!



- hw12 + milestone due on Monday, 12/4
- 5 finite-state machines due as part of hw12

Turing machines extra!

# *Final project* state machine



# State-machine *limits*?

Are there limits to what FSMs can do?



they can't  
necessarily  
drive  
safely...



MIT's car,  
Talos

# An autonomous vehicle's FSM

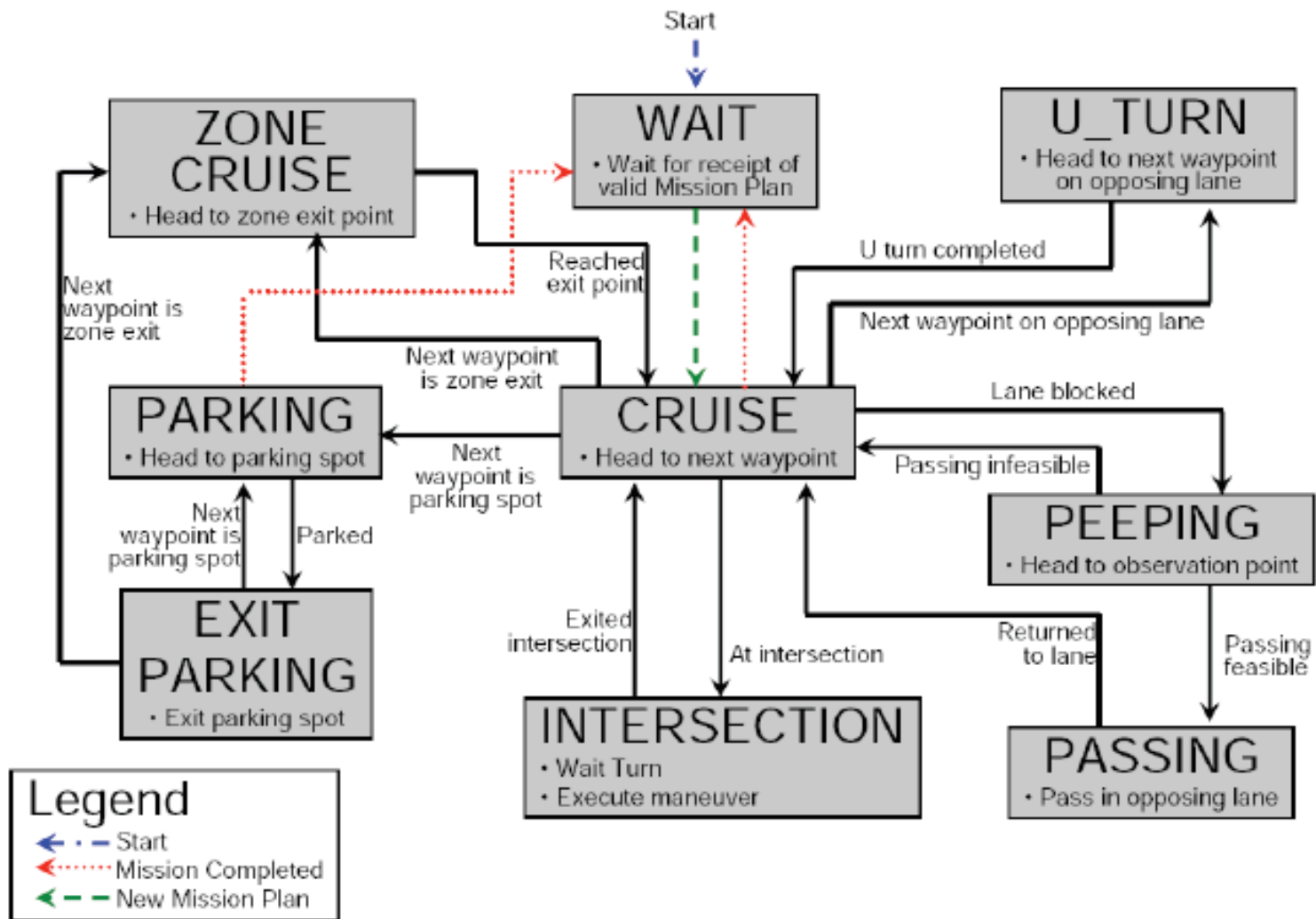
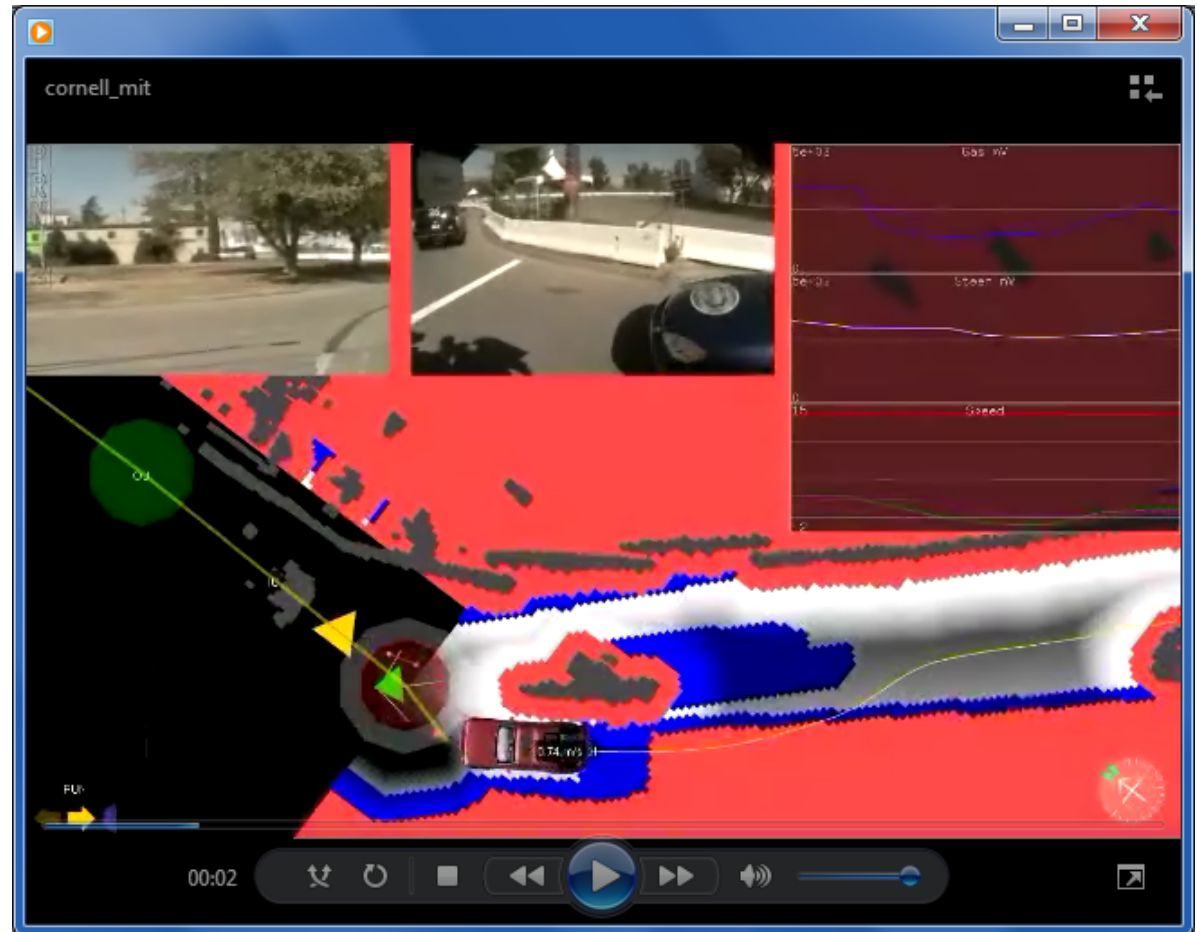


Fig. 9. Situational Interpreter State Transition Diagram. All modes are sub-modes of the system RUN mode (Fig 4(b)).

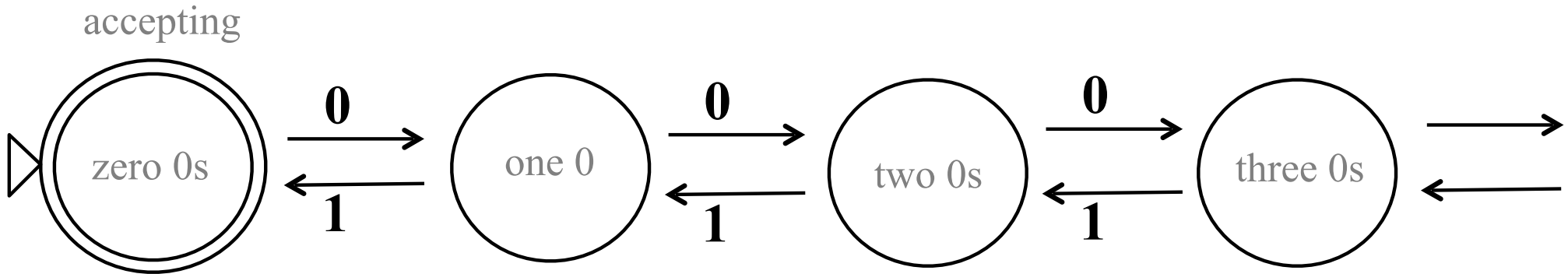
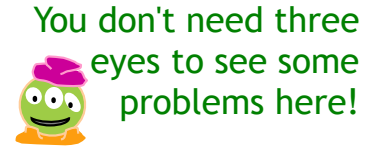
# The data driving the state machine...

MIT's car,  
Talos - *and  
its sensor  
suite*



But are there any **binary-string** problems that FSMs can't solve?

# State-machine *limits*?



Let's build a FSM that accepts strings with any # of 0s followed by the same #of 1s

*rejected*

011

001

11100

00110

*accepted*

000111

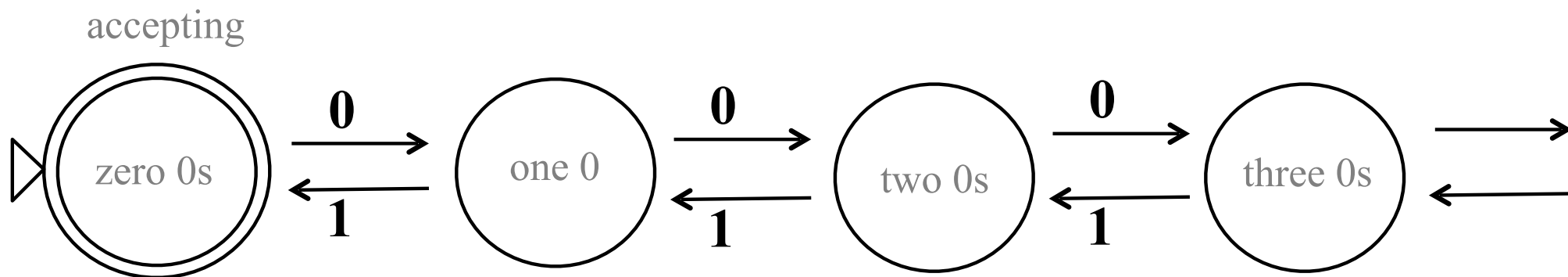

0011

01

$\lambda$

# State-machine *limits*?

You don't need three eyes to see some problems here!



Let's build a FSM that accepts strings with any # of 0s followed by the same # of 1s

rejected

011

001

11100

00110

**FSMs "can't count"**

at least, not arbitrarily high

accepted

000111

0011

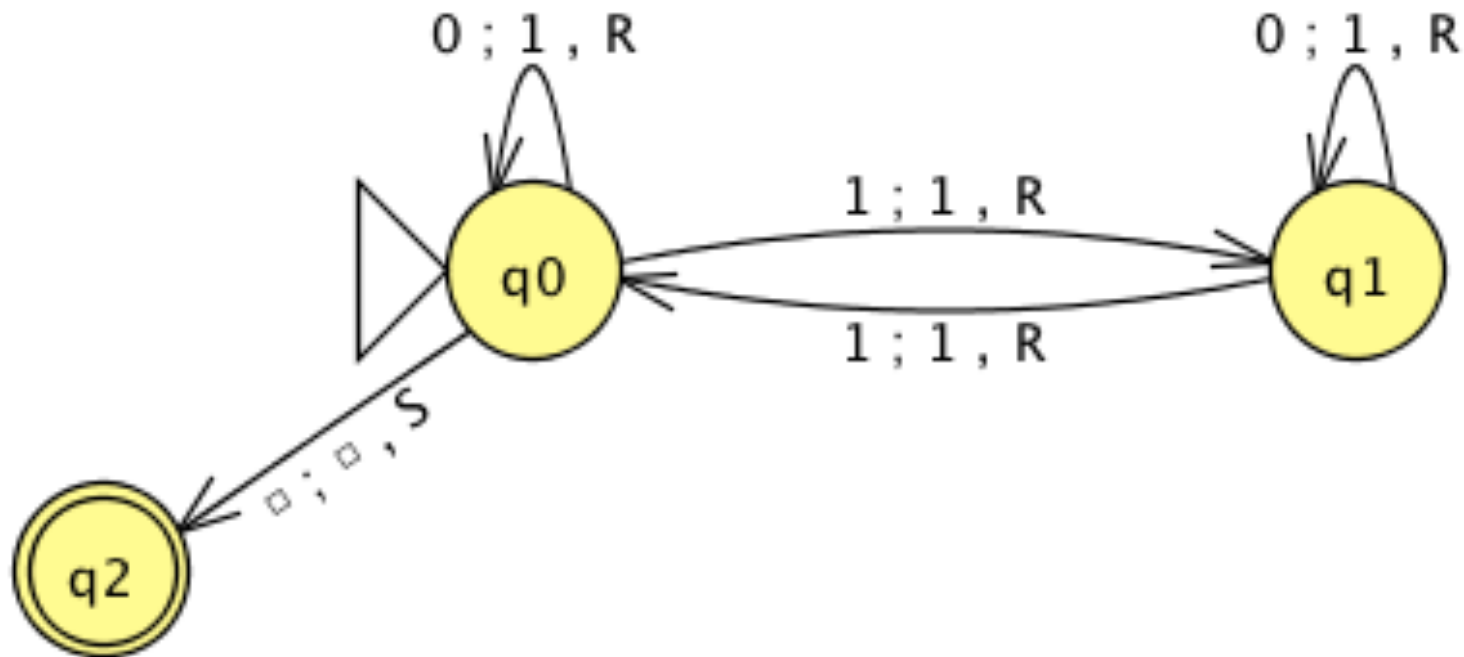
01

$\lambda$



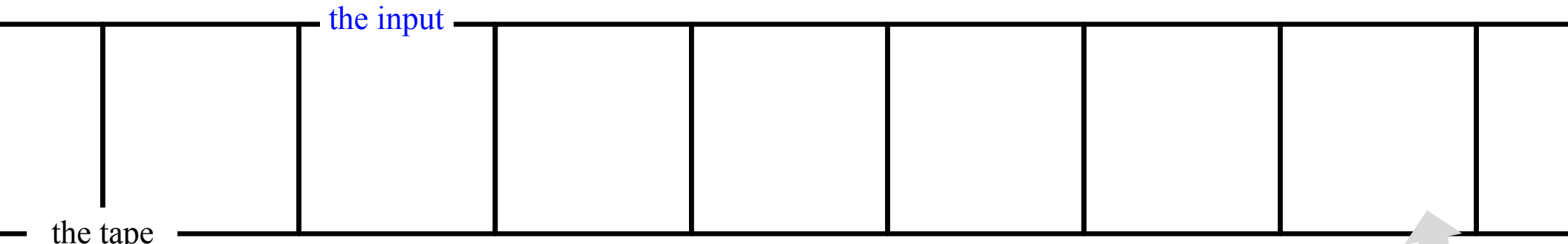
FSMs can't *count*...

*So, let's build a better machine!*



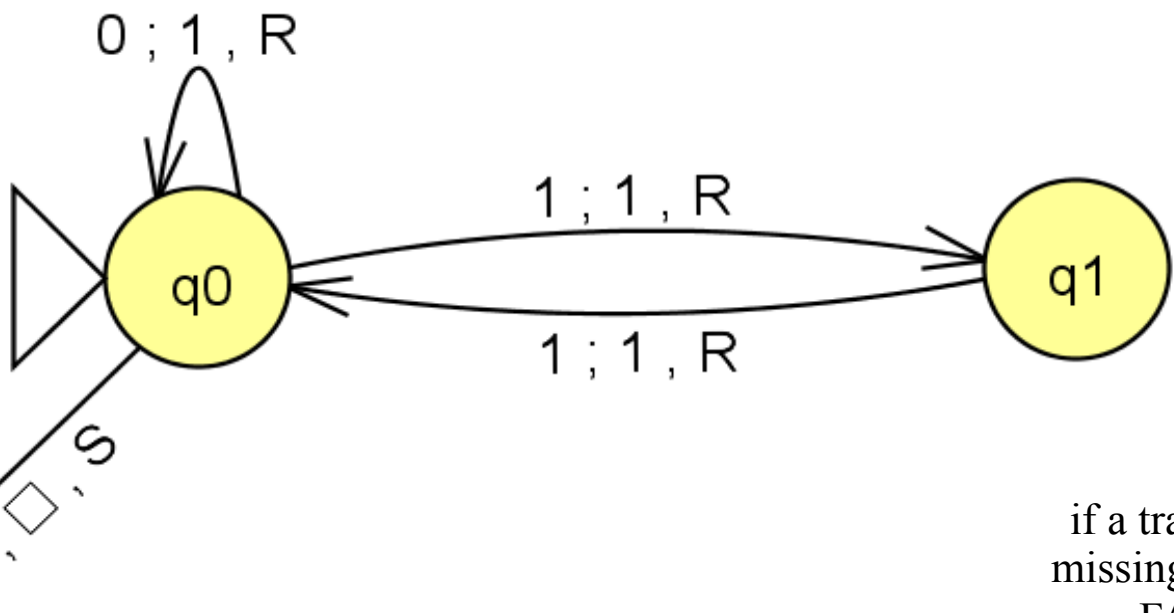
Shiny!

*Turing Machine*



"blanks" are the default

an accepting state **always halts** -- then basks in its success!



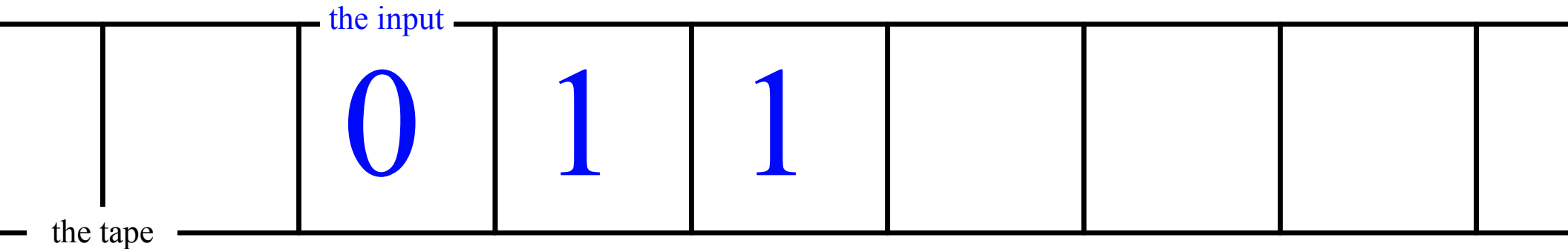
if a transition is missing, the input FAILS!

a Turing Machine rule:

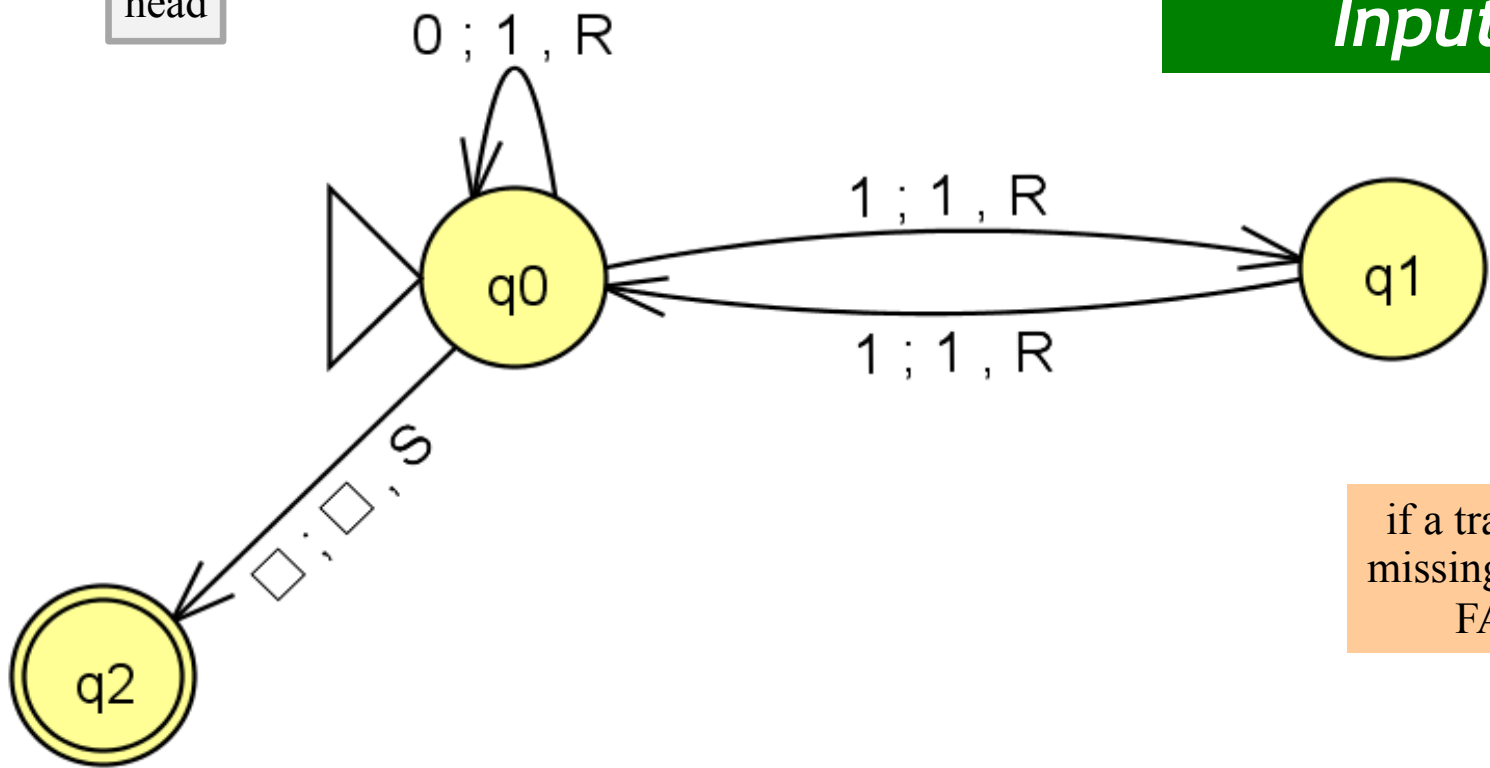
**0 ; 1 , R**

READ                  WRITE                  MOTION

try it in JFLAP...



**Accepted Input!**

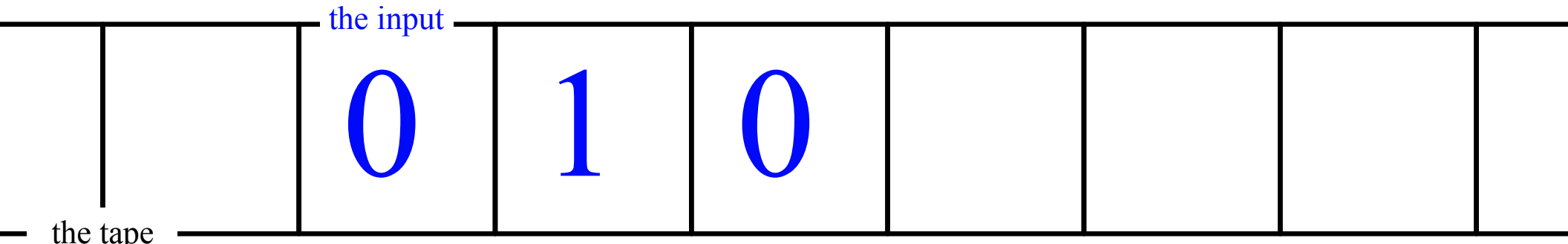


if a transition is missing, the input FAILS!

a Turing Machine rule:

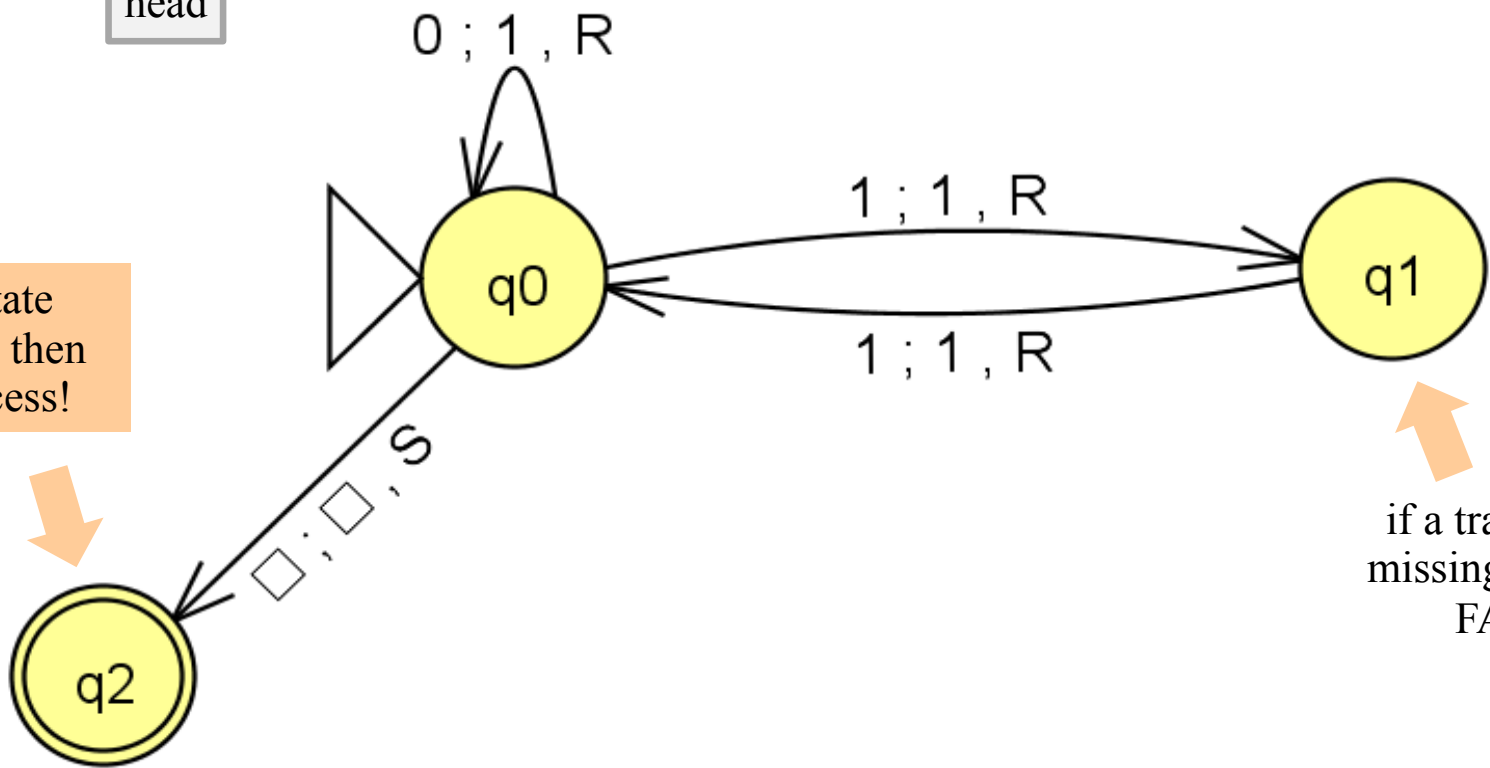
**0 ; 1 , R**

READ                  WRITE                  MOTION



**Rejected Input.**

an accepting state **always halts** -- then basks in its success!

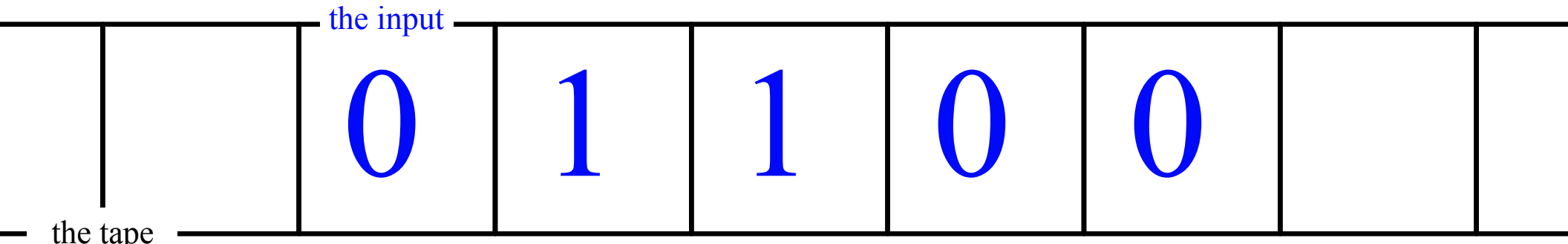


if a transition is missing, the input FAILS!

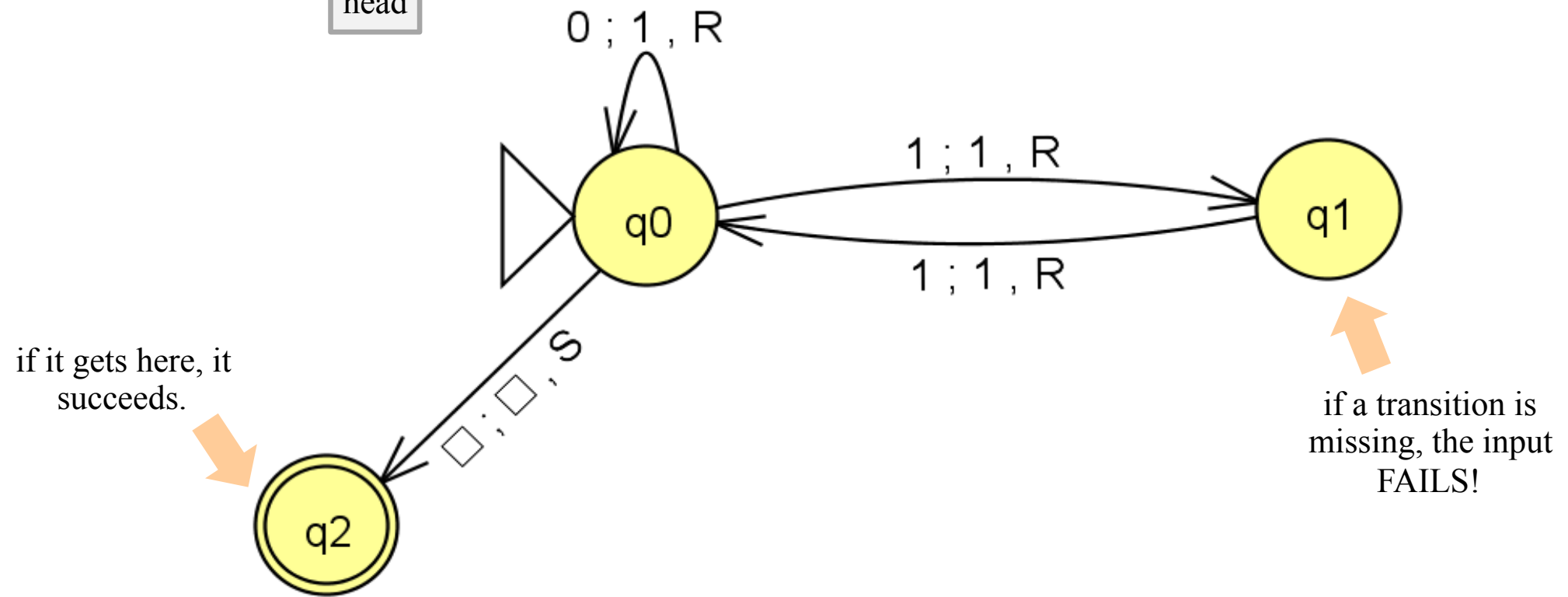
a Turing Machine rule:

**0 ; 1 , R**

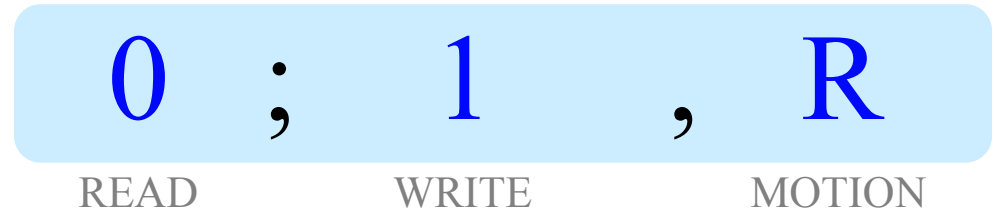
READ                  WRITE                  MOTION



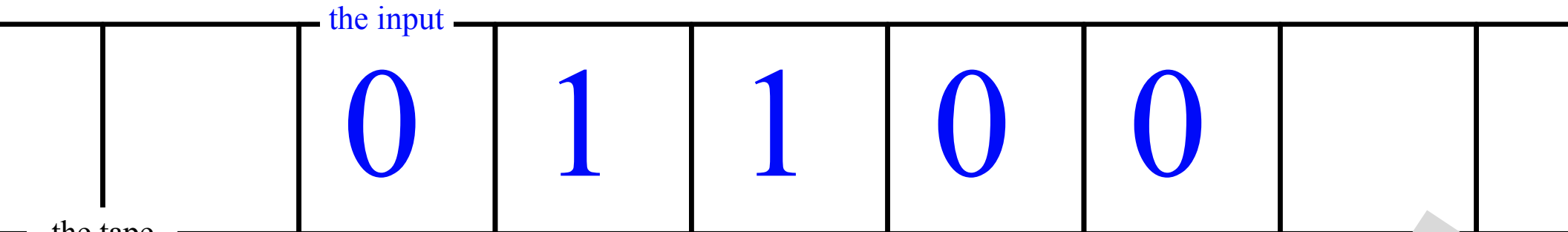
*What happens here?*



a Turing Machine rule:

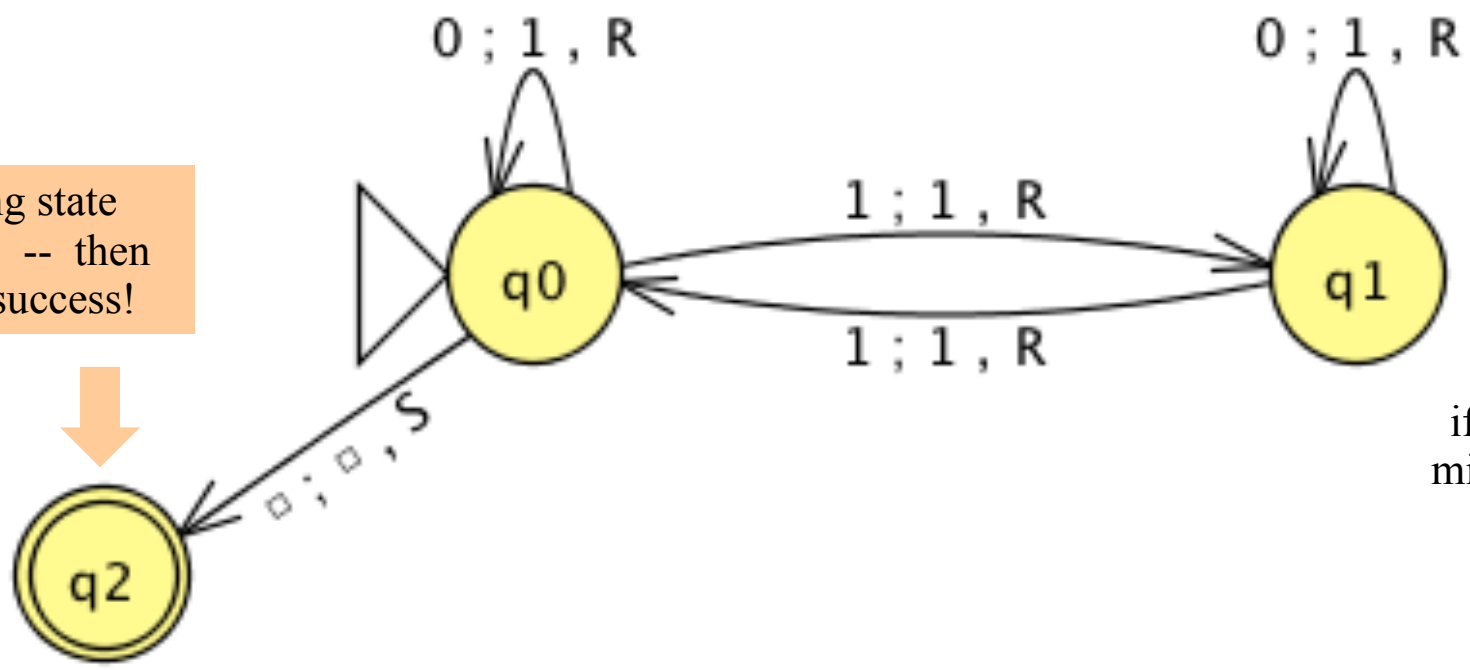


try it in JFLAP...



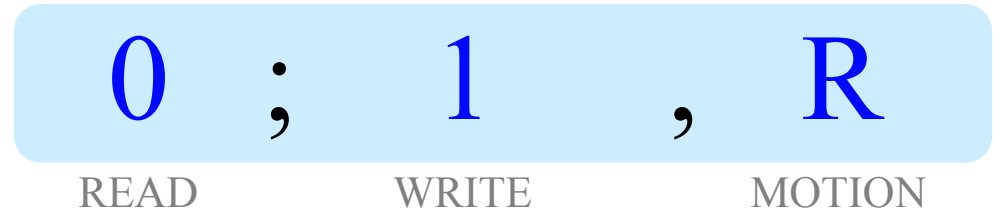
"blanks" are everywhere else

an accepting state **always halts** -- then basks in its success!



if a transition is missing, the input FAILS!

a Turing Machine rule:



try it in JFLAP...

# CS 5 spokesperson of the day!



The Imitation Game (2014)

30

PG-13 114 min - Biography | Drama | Thriller -  
25 December 2014 (USA)



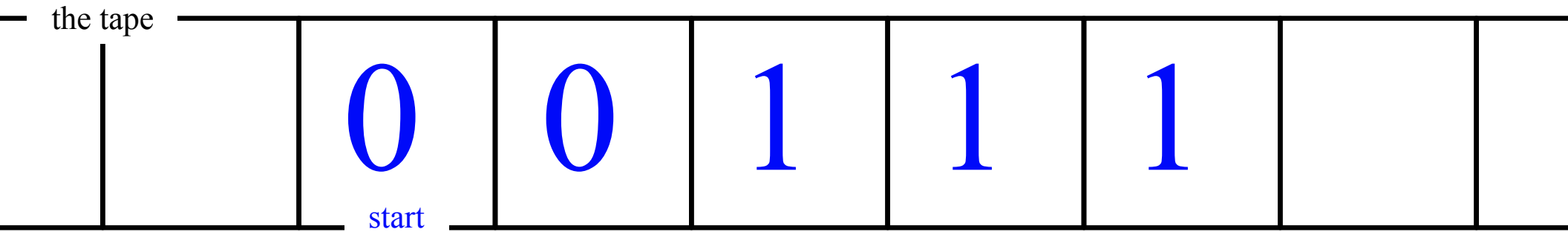
Your rating: ★★★★★★ -/10

Ratings: 8.4/10 from 8,470 users Metascore: 71/100

Reviews: 46 user | 108 critic | 31 from Metacritic.com

I want a  
1950's  
network!

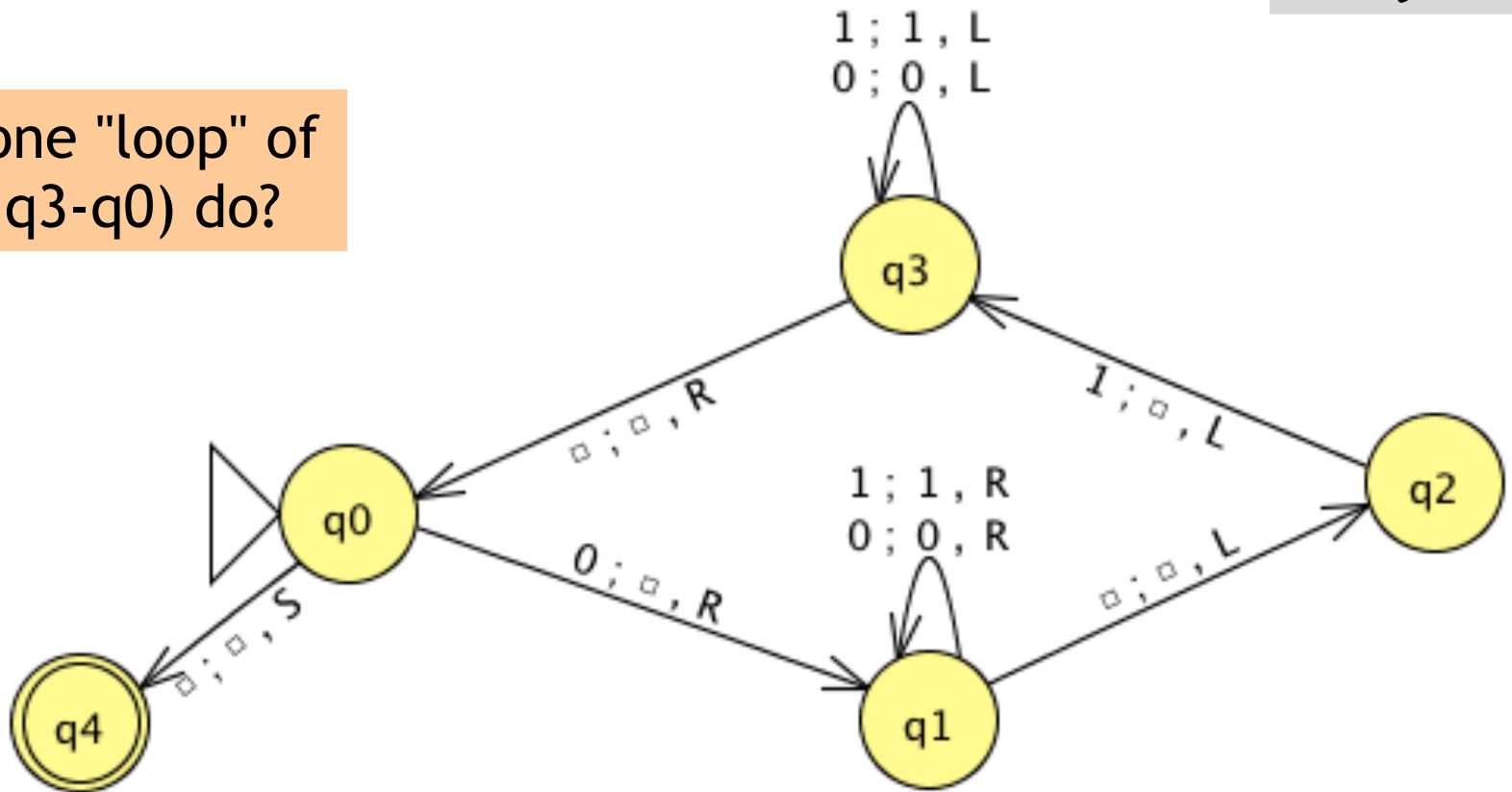




Is *this* input accepted or rejected by this TM?

*Try it!*

What does one "loop" of (q0-q1-q2-q3-q0) do?



What inputs are accepted *in general*?

**Extra:** How could you change this TM to accept *palindromes*?  
(thought experiment and ex. cr.)



# Can TMs compute *everything*?

Alan Turing says **yes...**

the tape elsewhere do not affect the behaviour of the machine. However the tape can be operated in such a way that this being one of the elementary operations usually have an innings.

Turing called them *Logical Computing Machines*

These machines will here be called 'Logical Computing Machines'. They are chiefly of interest when we wish to consider what a machine could in principle be designed to do, when we are willing to allow it both unlimited time and unlimited storage capacity.

Universal Logical Computing machines. It is possible to describe L.C.M.s in a very standard way, and to put the description into a form which can be 'understood' (i.e. applied by) a special machine. In particular it is possible to design a 'universal machine' which is an L.C.M. to which no other L.C.M. is imposed on the other. When such a machine then set going it will carry out the operations of any particular machine whose description it was given. For details the reader must refer to Turing (1).

Turing's *Intelligent Machines, 1948*

The importance of the universal machine is clear. We do not need to have an infinity of different machines doing different jobs. A single one will suffice. The engineering problem of producing various machines for various jobs is replaced by the office work of 'programming' the universal machine to do these jobs.

It is found in practice that L.C.M.s can do anything that could be described as 'rule of thumb' or 'purely mechanical'. This is sufficiently well established that it is now agreed amongst logicians that 'calculable by means of an L.C.M.' is the correct accurate rendering of such phrases. There are several mathematically equivalent but superficially very different renderings.

*So far*, all known computational devices can compute only what Turing Machines can...

some are faster than others...

Quantum computation

[http://www.cs.virginia.edu/~robins/The\\_Limits\\_of\\_Quantum\\_Computers.pdf](http://www.cs.virginia.edu/~robins/The_Limits_of_Quantum_Computers.pdf)

Molecular computation

<http://www.arstechnica.com/reviews/2q00/dna/dna-1.html>

Parallel computers



Integrated circuits



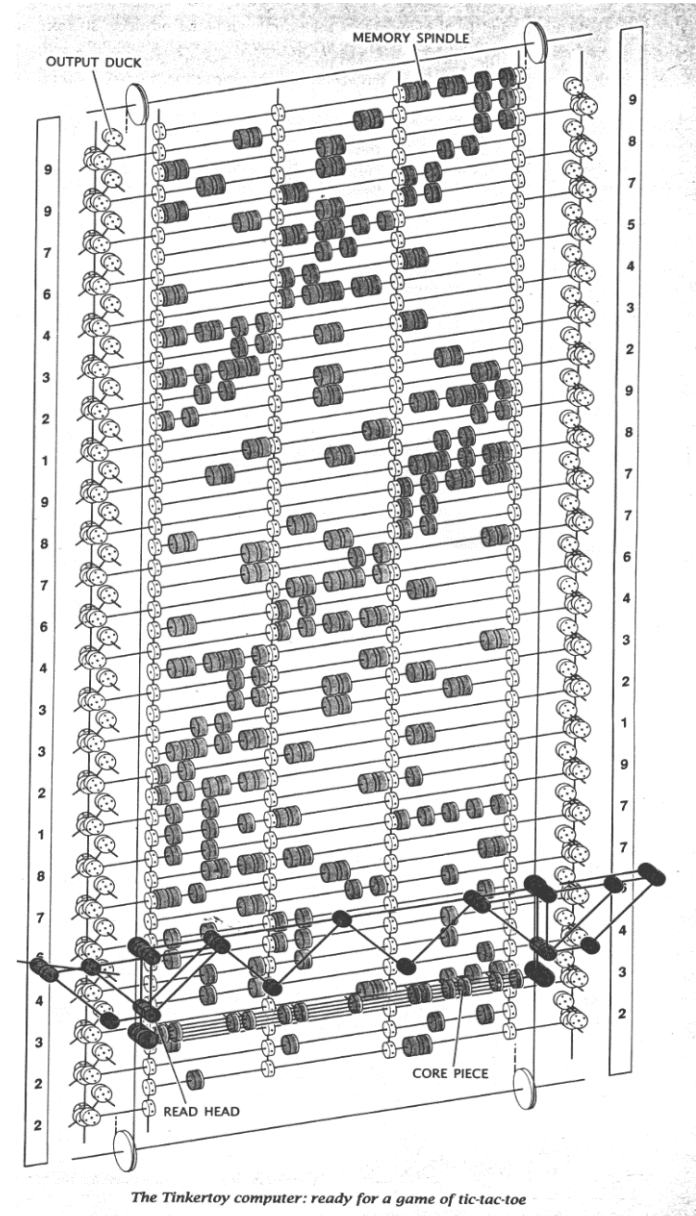
Electromechanical computation

Water-based computation

Tinkertoy computation



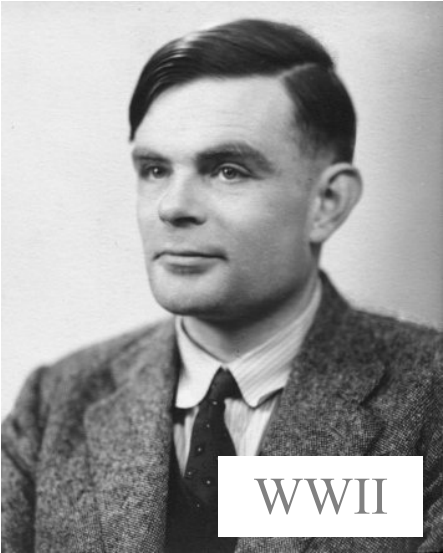
**Turing machine**





# Alan Turing

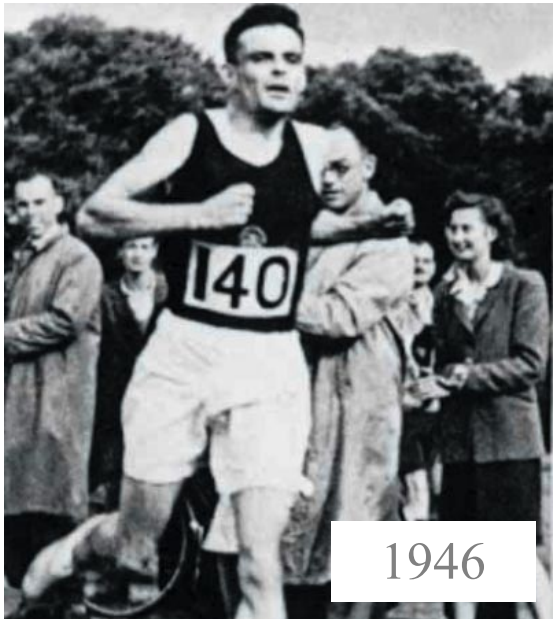
1912-1954



WWII



Enigma machine ~ The axis's encryption engine



1946

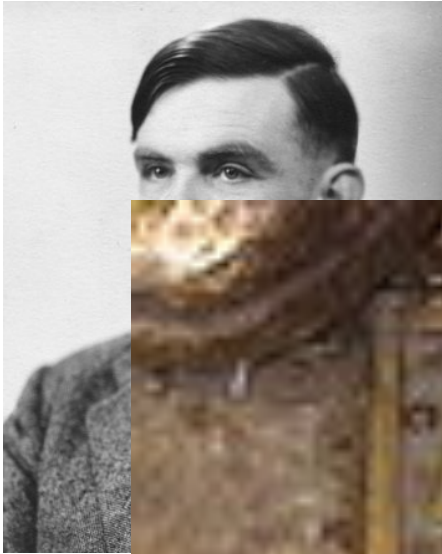


2007  
Bletchley Park

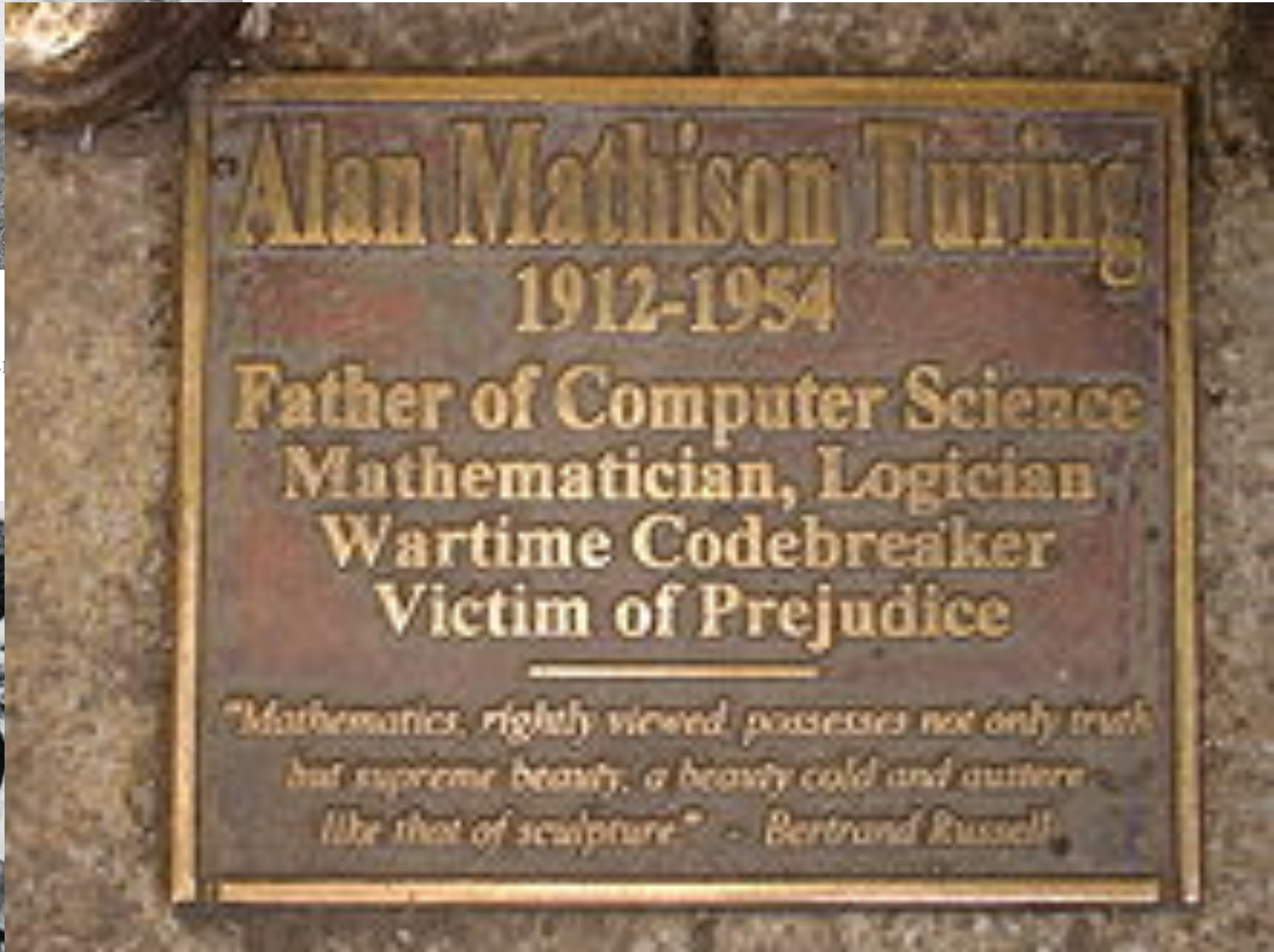


# Alan Turing

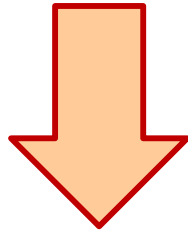
1912-1954



E



# 2012: Turing Celebration



aturningmachine.com/examplesSub.php

Counting Subtraction Busy Beaver 3 Busy Beaver 4 Programming Syntax

### Turing Machine Doing Subtraction

A Turing Machine - Subtraction

Write  
State 2 Position 4 Step 17

Although there are a number of Turing state machines that will accomplish subtraction, this method uses only ones, zeros, and blank cells. It's not that difficult to understand how a Turing machine does subtraction.

In this example, the space between the number sets separates the two sides of the equation. The machine removes matching "1"s from each side of the equation until there are no more "1"s on the right side. A count of

<http://aturningmachine.com/examplesSub.php>

<https://www.youtube.com/watch?v=aBToqFJLrI4>

## Turing machine simulator

[Back to home page](#)

This is a [Turing machine](#) simulator, written in JavaScript. To use it:

1. Load one of the example programs, or write your own in the TM Program area below.
2. Enter something in the 'Input' area - this will be initially written on the tape.
3. Click on 'Run' to start the Turing machine and run it until it halts (if ever). Click on 'Stop' to interrupt the Turing machine while it is running. Alternately, click 'Step' to run a single step of the Turing machine.
4. Click 'Reset' to restore the Turing machine to its initial state so it can be run again.

11110011111

Current state: 0 Steps: 0

Load or write a Turing program below and click 'Run'

Step Run Stop Reset Initial input: 11110011111

Turing machine program:

```
<current state> <current symbol> <new symbol> <direction> <new state>
```



# Stretch Break!

## TURING TEST

[|<](#) [< PREV](#) [RANDOM](#) [NEXT >](#) [>|](#)



[|<](#) [< PREV](#) [RANDOM](#) [NEXT >](#) [>|](#)



# Can ~~TMs~~ compute everything?

computers

Alan Turing says **No!**

ON COMPUTABLE NUMBERS, WITH AN APPLICATION TO  
THE ENTSCHEIDUNGSPROBLEM *decision* problems!

*By* A. M. TURING.

[Received 28 May, 1936.—Read 12 November, 1936.]

The “computable” numbers may be described briefly as the real numbers whose expressions as a decimal are calculable by finite means.

Although the subject of this paper is ostensibly the computable *numbers*, it is almost equally easy to define and investigate computable functions of an integral variable or a real or computable variable, computable predicates, and so forth. The fundamental problems involved are, however, the same in each case, and I have chosen the computable numbers for explicit treatment as involving the least cumbrous technique. I hope

# There are many problems computers can't solve at all !

Perhaps this is not that surprising...

- rising sea levels
- disbelief in aliens
- losing to your own Connect4 (at 0 ply!)
- towel folding! (well, *fast* towel folding...)





# Unprogrammable *functions?*

There are

well-defined  
mathematical  
functions

that no

computer  
program

can compute  
*even with any  
amount of memory!*

or TM

functions

**programs**

$$f(x) = \begin{cases} 1 & \text{if } x \text{ is odd} \\ 0 & \text{if } x \text{ is even} \end{cases}$$

```
def prog1(x):  
    return x%2
```

# Unprogrammable *functions?*

There are

There are  
many more  
of these ...

mathematical functions

functions

that no

com  
pro

than  
these!

programs

*memory!*

programs

$$f(x) = \begin{cases} 1 & \text{if } x \text{ is odd} \\ 0 & \text{if } x \text{ is even} \end{cases}$$

```
def prog1(x):  
    return x%2
```

# functions

## int - bool

$$f_A(x) = 1$$

$$f_B(x) = \begin{cases} 1 & \text{if } x \text{ is odd} \\ 0 & \text{if } x \text{ is even} \end{cases}$$

$$f_C(x) = \begin{cases} 1 & \text{if } x \text{ is } 0, 1, \text{ or } 2 \\ 0 & \text{otherwise} \end{cases}$$

These are "*int-bool*" mathematical functions.

They're also sometimes called "*integer predicates*."

- Input is an integer,  $x \geq 0$
- Output is 0/1 (*boolean or bit*)

...even if you restrict your functions to be totally discrete!

# int - bool programs

## Example programs

- Input is one integer,  $x \geq 0$
- Output is 0/1 (*boolean or bit*)

If programs look different they are different – *even if they compute the same function!*

```
def prog1 (x) :  
    return x%2
```

```
def prog2 (x) :  
    return x<3
```

```
def prog3 (x) :  
    return 1
```

```
def prog4 (x) :  
    return len(str(x+42))>1
```

all int inputs:  
 $x \geq 0$

... and allow ANY programs at all ~ even syntax errors

Let's match!

# functions

$$f_A(x) = 1$$

$$f_B(x) = \begin{cases} 1 & \text{if } x \text{ is odd} \\ 0 & \text{if } x \text{ is even} \end{cases}$$

$$f_C(x) = \begin{cases} 1 & \text{if } x \text{ is } 0, 1, \text{ or } 2 \\ 0 & \text{otherwise} \end{cases}$$

1. Match each program with the function it computes.
2. There are three different functions on the left side -- how many *different programs* are in the right side?

How - or why - is the set of **all functions** larger than the set of **all programs**?

# programs

```
def prog1(x):  
    return x%2
```

all int inputs:  
 $x \geq 0$

```
def prog2(x):  
    return x<3
```

```
def prog3(x):  
    return 1
```

```
def prog4(x):  
    return len(str(x+42))>1
```

```
def prog5(x):  
    return x in [0,1,2]
```

```
def prog6(x):  
    if x<2: return x  
    else: return prog6(x-2)
```

*Worksheet!*

# functions

$$f_A(x) =$$

$$f_B(x) =$$

$$f_C(x) =$$

There are  
many more  
of these ...

mathematical functions

$\begin{cases} 1 & \text{if } x \text{ is } 0, 1, \text{ or } 2 \\ 0 & \text{otherwise} \end{cases}$

1. Match each program with the function it computes.
2. There are three different functions on the left side -- how many *different programs* are in the right side?

How - or why - is the set of **all functions** larger than the set of **all programs**?

# programs

```
def prog1(x):  
    return x
```

```
def prog2(x):  
    return x
```

```
def prog3(x):  
    return 1
```

```
def prog4(x):  
    return len(str(x+42))>1
```

```
def prog5(x):  
    return x in [0,1,2]
```

```
def prog6(x):  
    if x<2: return x  
    else: return prog6(x-2)
```

than  
these!

programs

Quiz Name(s): \_\_\_\_\_

# Uncomputable *functions*?

There are

well-defined  
mathematical  
functions

that no

computer  
program

can compute  
*even with any  
amount of memory!*

or TM<sup>TM</sup>

*Why?*

There are  
many more  
of these ...

mathematical functions

than  
these!

programs

$\mathbb{R}$

vs.

$\mathbb{N}$

# Programs are "like" integers...

```
def alien( x ):  
    if x == 42:  
        return True  
    else:  
        return not \  
alien(x+1)
```

## programs

*For each program, there is an integer.*

*For each integer, there is a "program."*

*This is true:  
**but how?***

at least a string!  
some have syntax errors...



# Programs are integers (and vice-versa)

```
def alien( x ):  
    if x == 42:  
        return True  
    else:  
        return not \  
alien(x+1)
```

**programs** =  $\mathbb{N}$  Positive integers

Every program is a **string**.

Every string is just a sequence of **bits**

Every sequence of bits is also an **int!**

from progs to ints ~ and *back...*

```
7 t.py - C:\Users\Owner\Desktop\t.py
File Edit Format Run Options Windows Help
#
# Python converters from int to program (and back)
#
def prog( i ):
    """ return the program whose int is i """
    # convert to a string (just a base-128 int!)
    if i <= 0: return ''
    last_char = chr( i%128 )
    return prog( i/128 ) + last_char

def intify( prog ):
    """ return the int whose program is prog """
    # convert to an int (just interpret as base-128!)
    if prog == '': return 0
    last_char = prog[-1]
    return 128*intify( prog[:-1] ) + ord( last_char )

# to run a string: (1) code = compile( p, 'str', 'exec' )
#                  (2) exec( code )
Ln: 21 Col: 42
```